

Charm Physics at BESIII

(Leptonic and semi-leptonic D decays)



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Hefei, Anhui, China**

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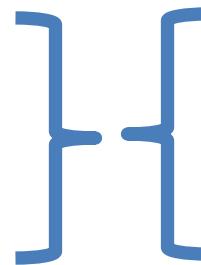
■ Introduction

■ Data Sample

■ $D^+ \rightarrow \mu^+ \nu$

■ $D^0 \rightarrow K(\pi)^- e^+ \nu$

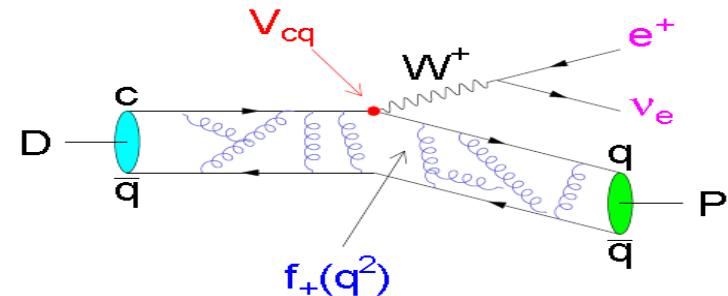
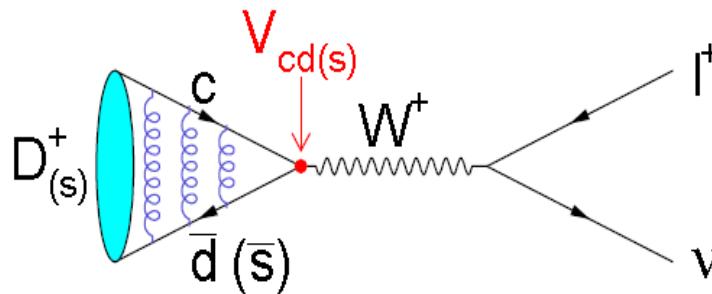
■ Summary

- 
- What happen in the past 26 years?
 - Precision measurements at BESIII
 - Opportunity in the next 20 years?

I would like to thank Prof. Steve Olsen for his helpful suggestions to improve my slides!

Why they are important?

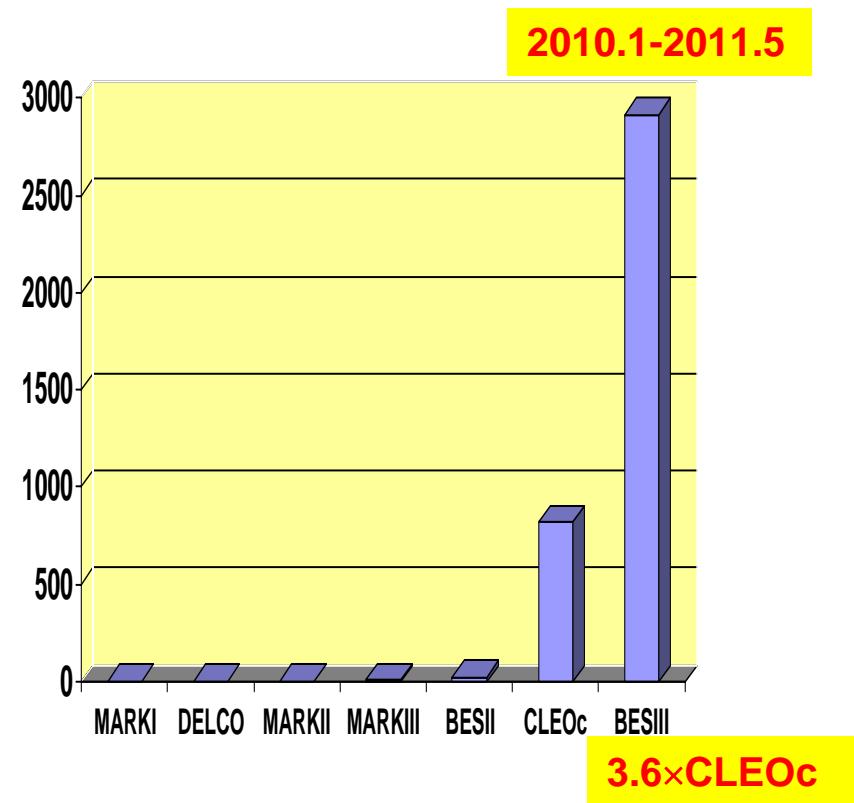
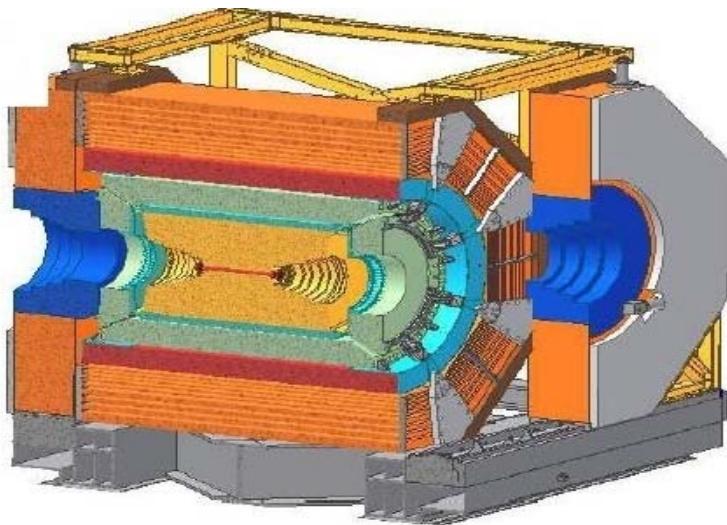
Leptonic and semi-leptonic D decays are ideal window to probe for weak and strong effects



- Precision measurements of decay constants f_{D+} , f_{Ds+} , form factors $f_+^{D \rightarrow K(\pi)}(q^2)$ of semi-leptonic decays of $D_{(s)}$ mesons will calibrate LQCD calculations at higher accuracy. Once they pass experimental tests, the precisely LQCD calculated f_D/f_B , f_{Ds}/f_{Bs} and $f_+^{D \rightarrow K(\pi)}(0)/f_+^{B \rightarrow K(\pi)}(0)$ will be helpful for measurements in B decays
- Recently improved LQCD calculations on $f_{D(s)+}$ [0.5(0.5)%], $f_+^{D \rightarrow K(\pi)}(0)$ [2.4(4.4)%] provide good chance to precisely measure the CKM matrix element $|V_{cs(d)}|$, which are important for the unitarity test of the CKM matrix and search for NP beyond the SM

Data Sample

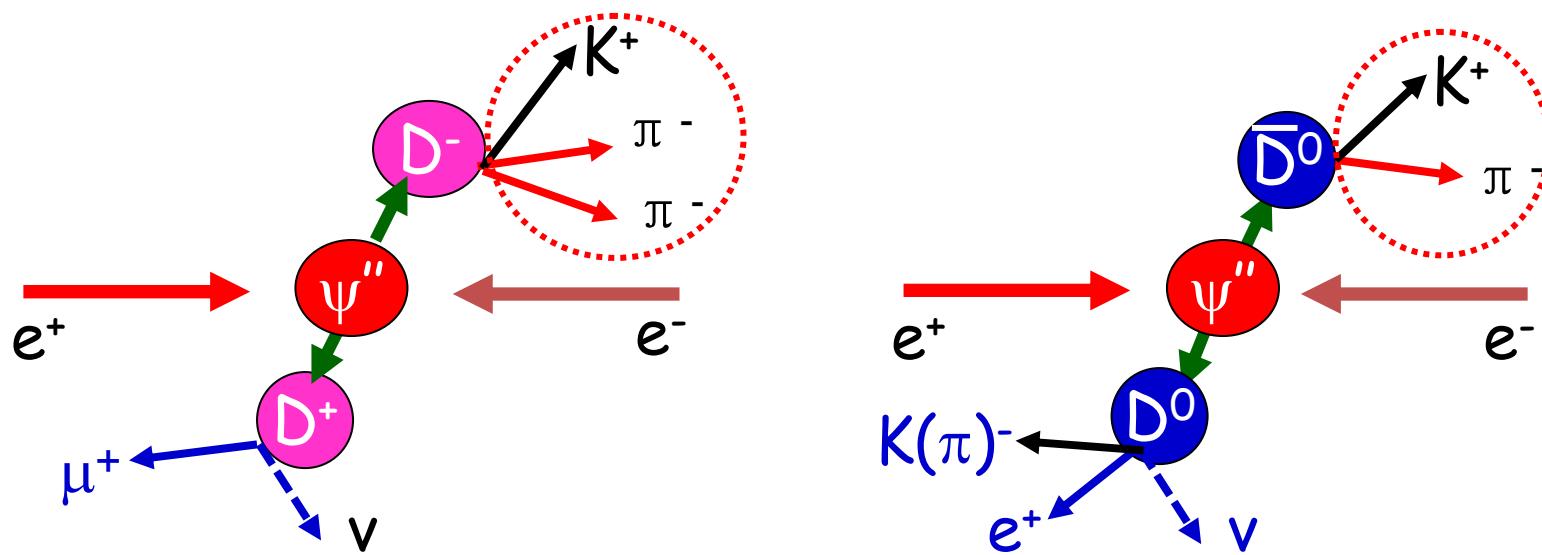
2.92 fb^{-1} data were taken around 3.773 GeV



Singly Tagged \bar{D}^0 and D^- Mesons

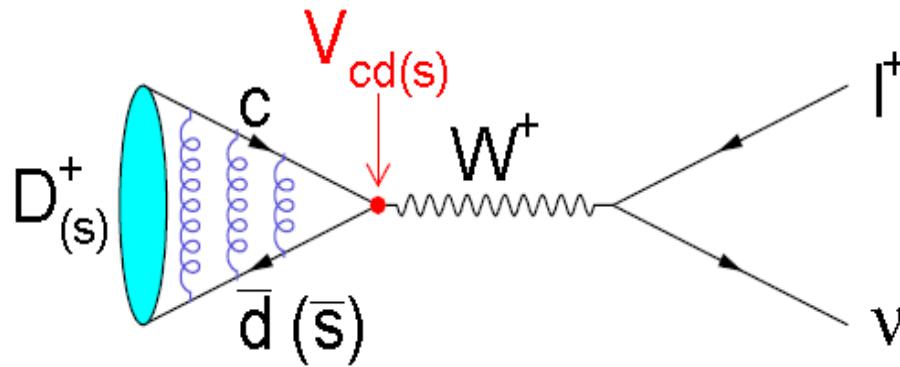
$D^0\bar{D}^0$ and D^+D^- are produced in pair at $\psi(3770)$

Singly tagged \bar{D}^0 and D^- mesons are reconstructed by hadron decays with large branching fraction and less combinatorial backgrounds



At the recoil side of singly tagged \bar{D}^0 and D^- mesons, leptonic and semi-leptonic decays can be studied

D⁺ Leptonic Decays



In the SM:

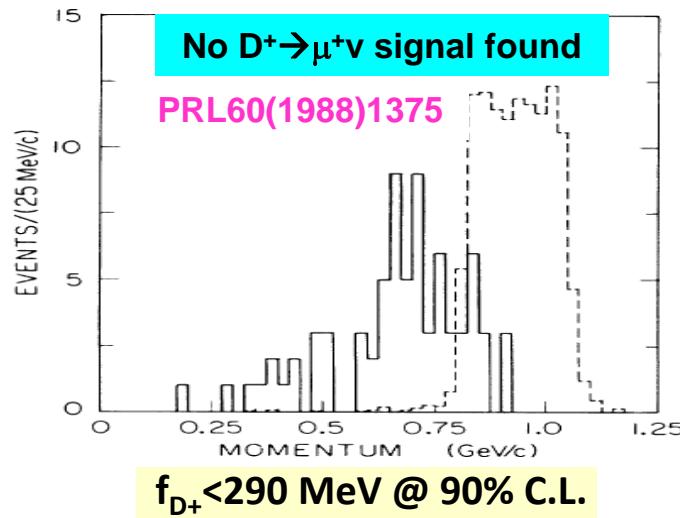
$$\Gamma(D_{(s)}^+ \rightarrow \ell^+ \nu_\ell) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_\ell^2 m_{D_{(s)}^+} \left(1 - \frac{m_\ell^2}{m_{D_{(s)}^+}^2}\right)^2$$

Bridge to precisely measure

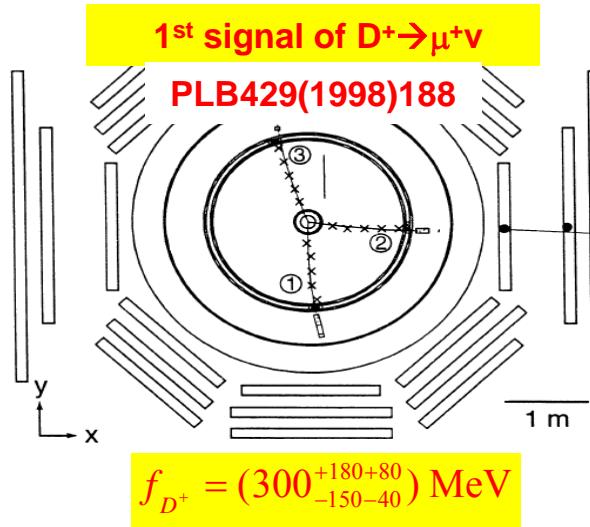
- Decay constant $f_{D(s)+}$ with input $|V_{cd(s)}|^{CKMfitter}$
- CKM matrix element $|V_{cd(s)}|$ with input $f^{LQCD}_{D(s)+}$

Progress of Measuring f_{D^+} in past 26 years

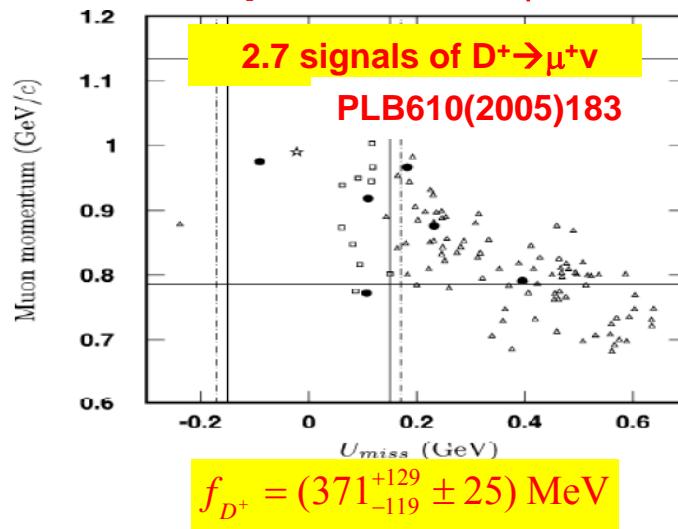
- MARKIII, 9.6 pb⁻¹ at ψ''



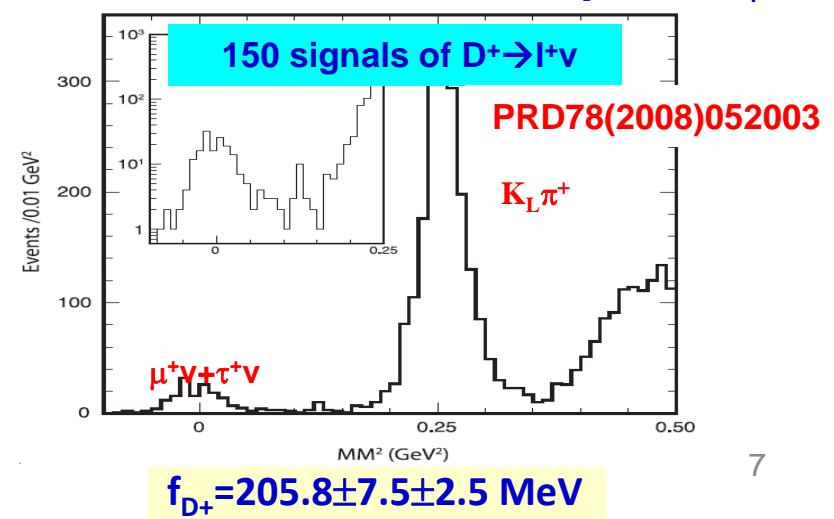
- BESI, 22.3 pb⁻¹ at 4.03 GeV



- BESII, 33 pb⁻¹ data at ψ''

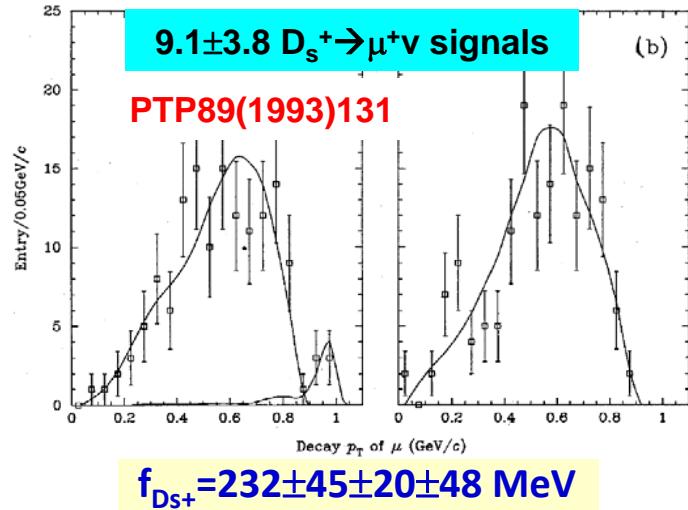


- 2004-2008, CLEO-c, 818 pb⁻¹ at ψ''

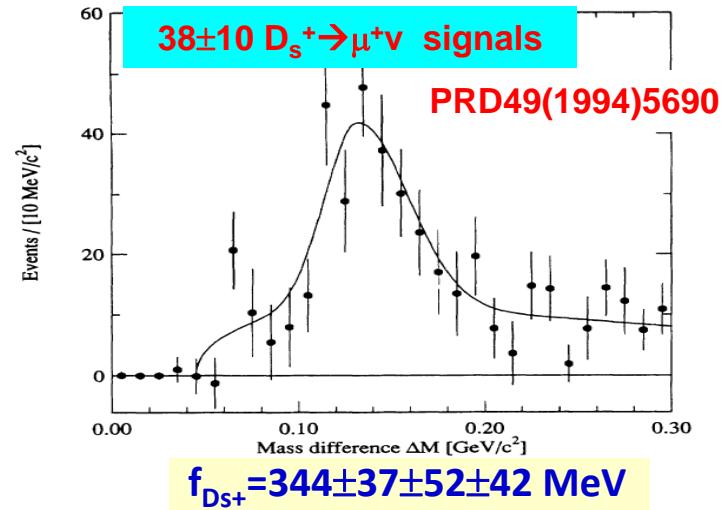


Progress of Measuring $f_{D_s^+}$ in past 21 years

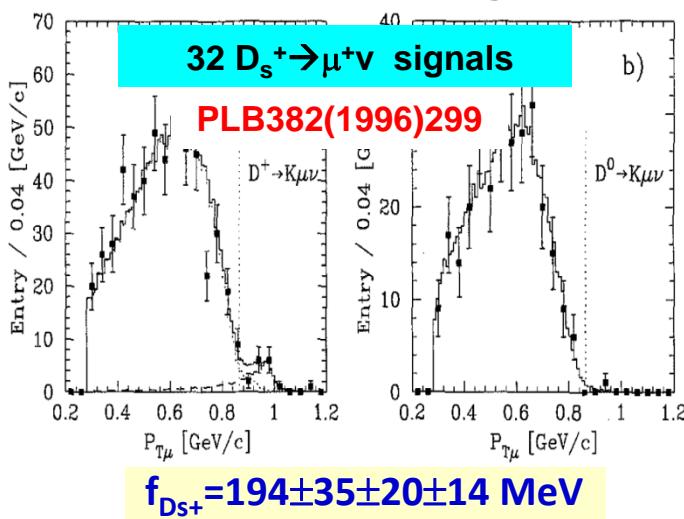
■ WA75, Fixed target experiment



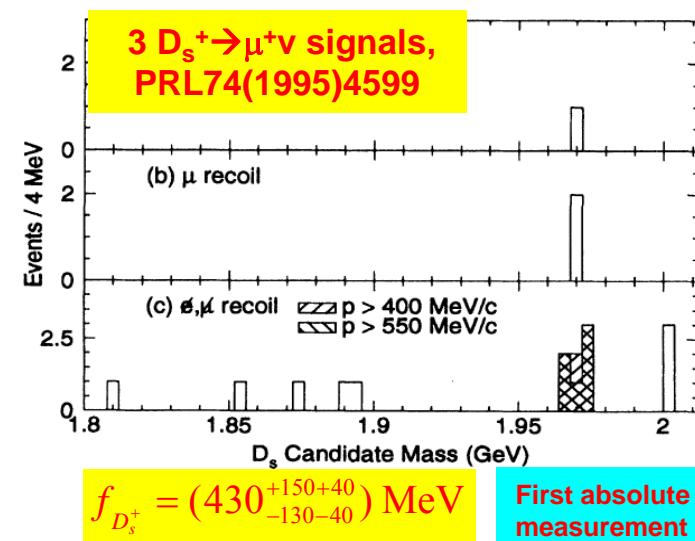
■ CLEOII, 2.13 fb⁻¹ at 10.6 GeV



■ E653, Fermilab fixed target experiment

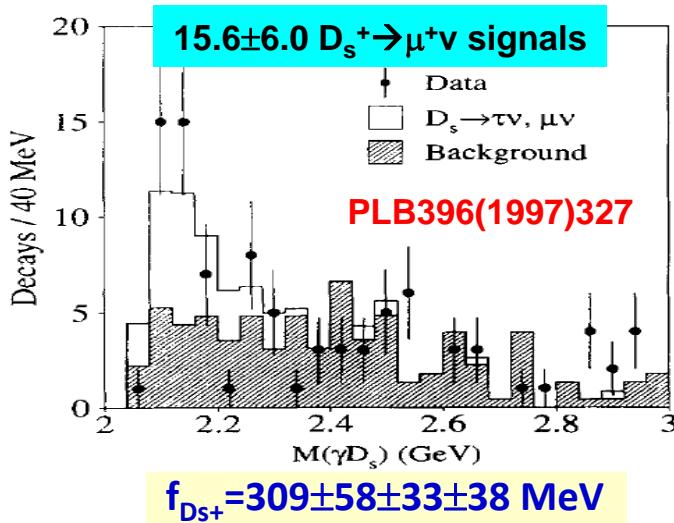


■ BESI, 22.3 pb⁻¹ at 4.03 GeV

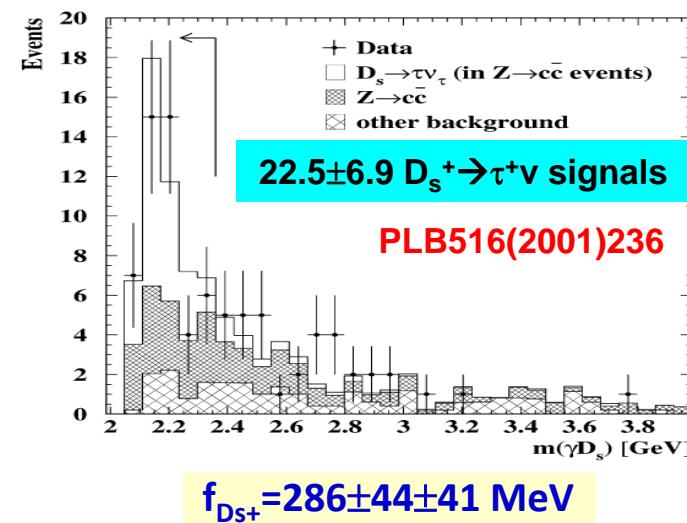


Progress of Measuring $f_{D_{s+}}$ in past 21 years

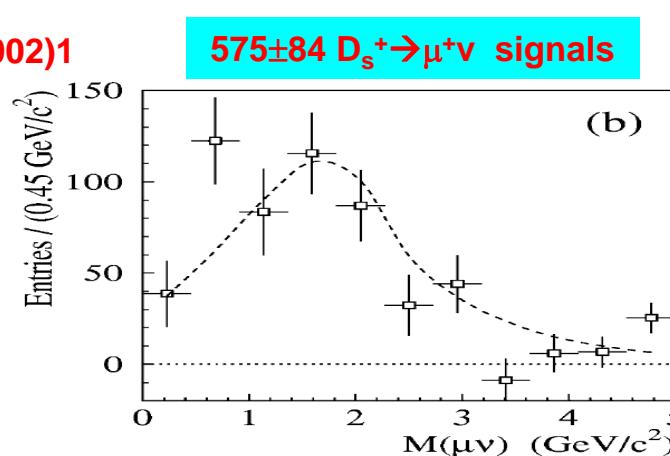
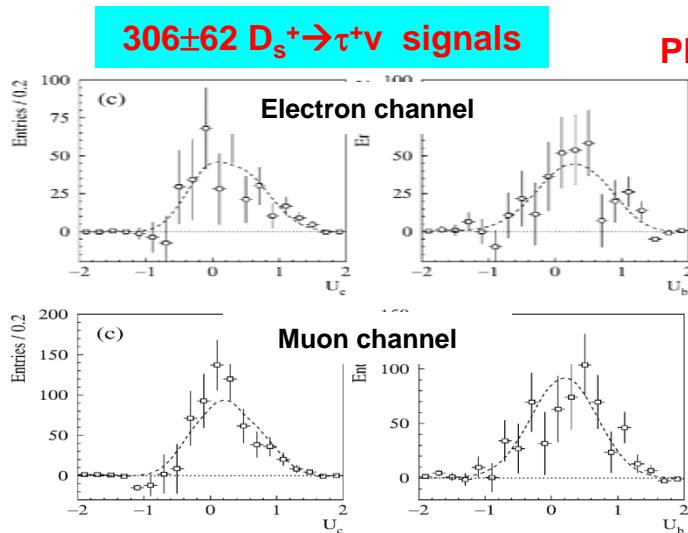
- L3, $Z \rightarrow q\bar{q}$, 49.6 pb^{-1} at 91.2 GeV



- OPAL, $3.9 \times 10^6 e^+e^- \rightarrow q\bar{q}$



- ALPHA, $3.97 \times 10^6 Z$ hadronic decay



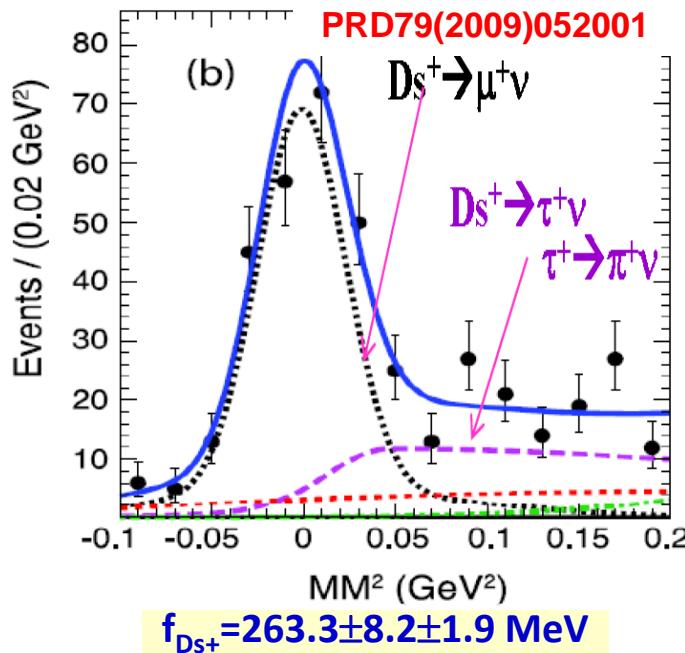
Progress of Measuring $f_{D_s^+}$ in past 21 years

■ CLEO-c, 600 pb⁻¹ at 4.17 GeV

Absolute measurement

$235 \pm 14 D_s^+ \rightarrow \mu^+ \nu + \tau^+ \nu$ signals

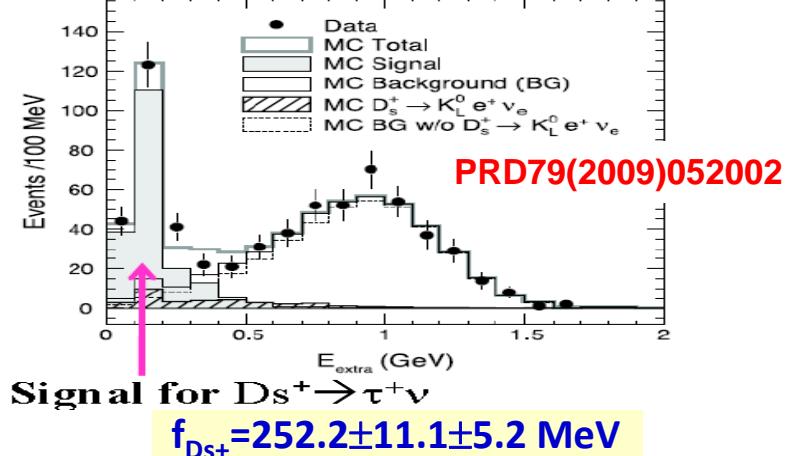
$126 \pm 16 D_s^+ \rightarrow \tau^+ \nu$ signals



Improved statistical
and systematic errors

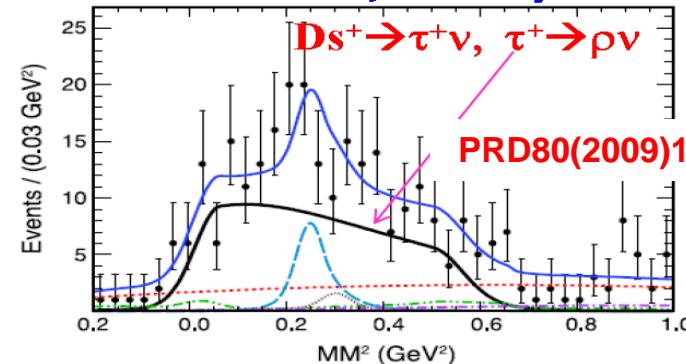
$181 \pm 16 D_s^+ \rightarrow \tau^+ \nu$ signals

$D_s^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow e^+ \nu \nu$



$155 \pm 17 D_s^+ \rightarrow \tau^+ \nu$ signals

$D_s^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \rho \nu$

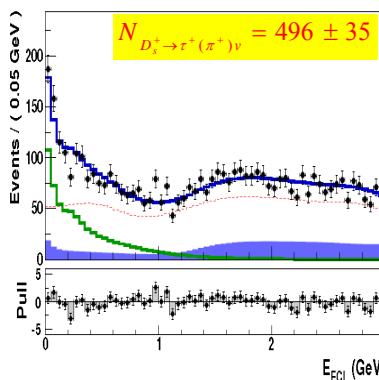
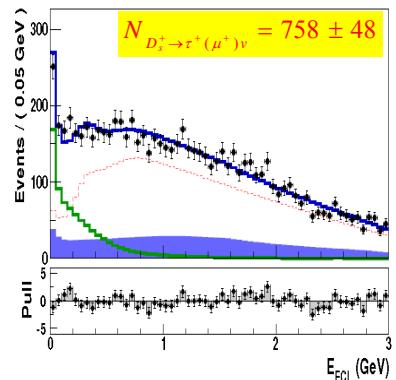
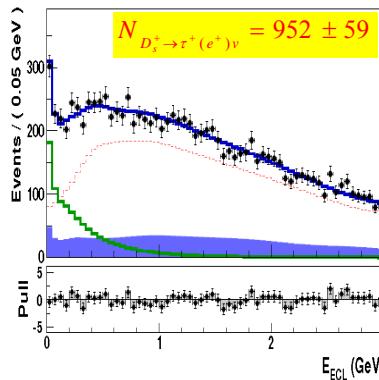
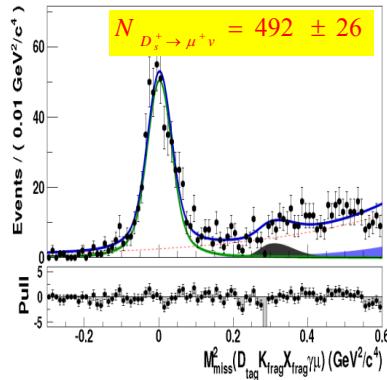


$f_{D_s^+} = 257.8 \pm 13.3 \pm 5.2 \text{ MeV}$

Progress of Measuring $f_{D_{s+}}$ in past 21 years

■ Belle, 913 fb^{-1} at 10.58 GeV

$$e^+ e^- \rightarrow c\bar{c} \rightarrow D_{\text{tag}} K_{\text{frag}} X_{\text{frag}} D_s^{*-}$$



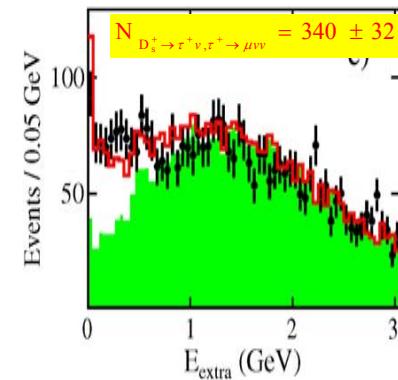
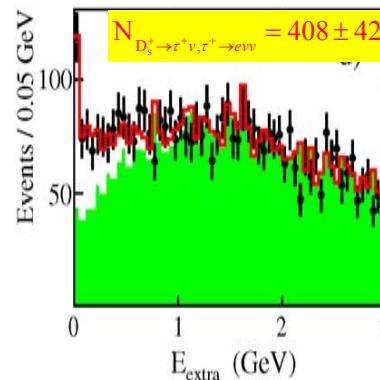
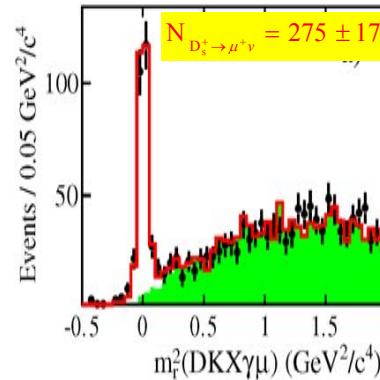
$$f_{D_{s+}} = 255.5 \pm 4.2 \pm 5.1 \text{ MeV}$$

2698 signals, JHEP1309(2013)129

■ Babar, 521 fb^{-1} at 10.58 GeV

Absolute measurements

$$e^+ e^- \rightarrow DKXD_s^{*-}$$



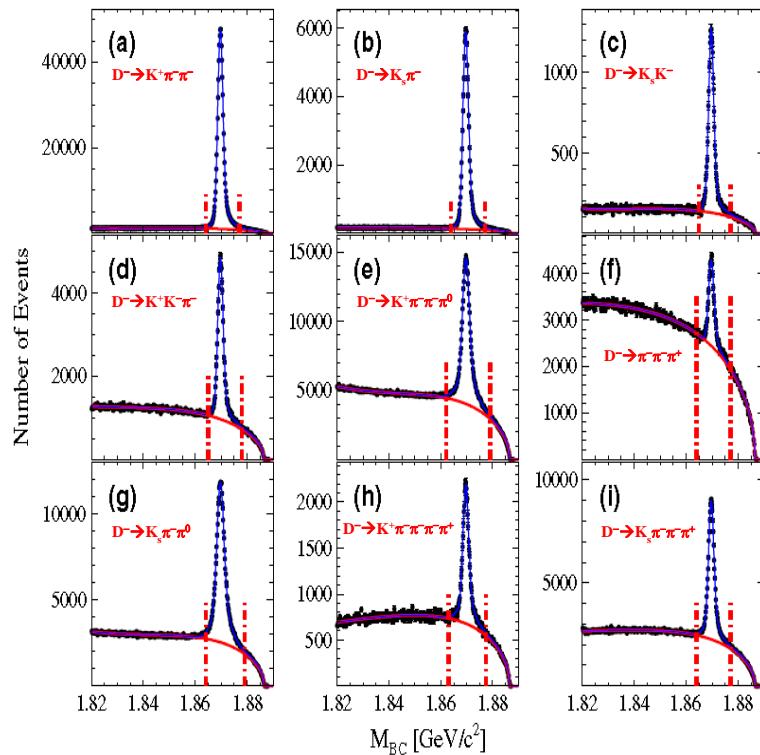
$$f_{D_{s+}} = 258.6 \pm 6.4 \pm 7.5 \text{ MeV}$$

1023 signals, PRD82(2010)091103

Better statistical but worse systematic errors at B factory

Improved $B[D^+ \rightarrow \mu^+ \nu]$, f_{D^+} and $|V_{cd}|$ at BESIII

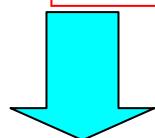
$e^+e^- \rightarrow \psi(3770) \rightarrow D^+D^-$



$$N_{D^+_{\text{tag}}} = (170.31 \pm 0.34) \times 10^4$$

$$B[D^+ \rightarrow \mu^+ \nu] = (3.71 \pm 0.19 \pm 0.06) \times 10^{-4}$$

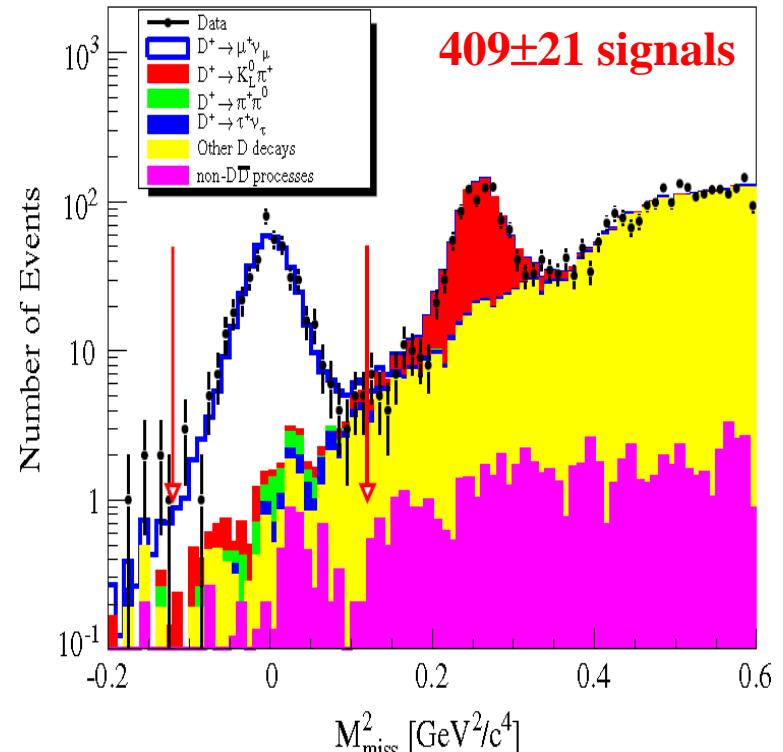
Input t_{D^+} , m_{D^+} , m_{μ^+} on PDG
and $|V_{cd}|$ of CKM-Fitter



BESIII

$$f_{D^+} = (203.2 \pm 5.3 \pm 1.8) \text{ MeV}$$

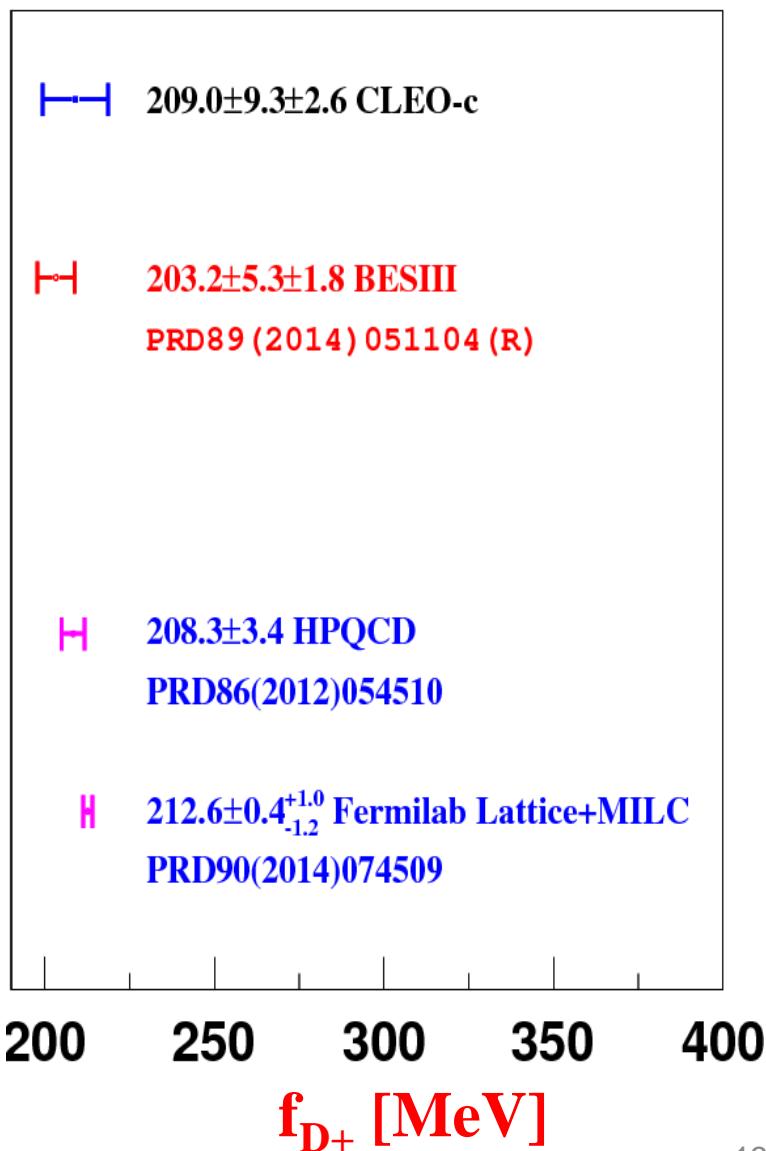
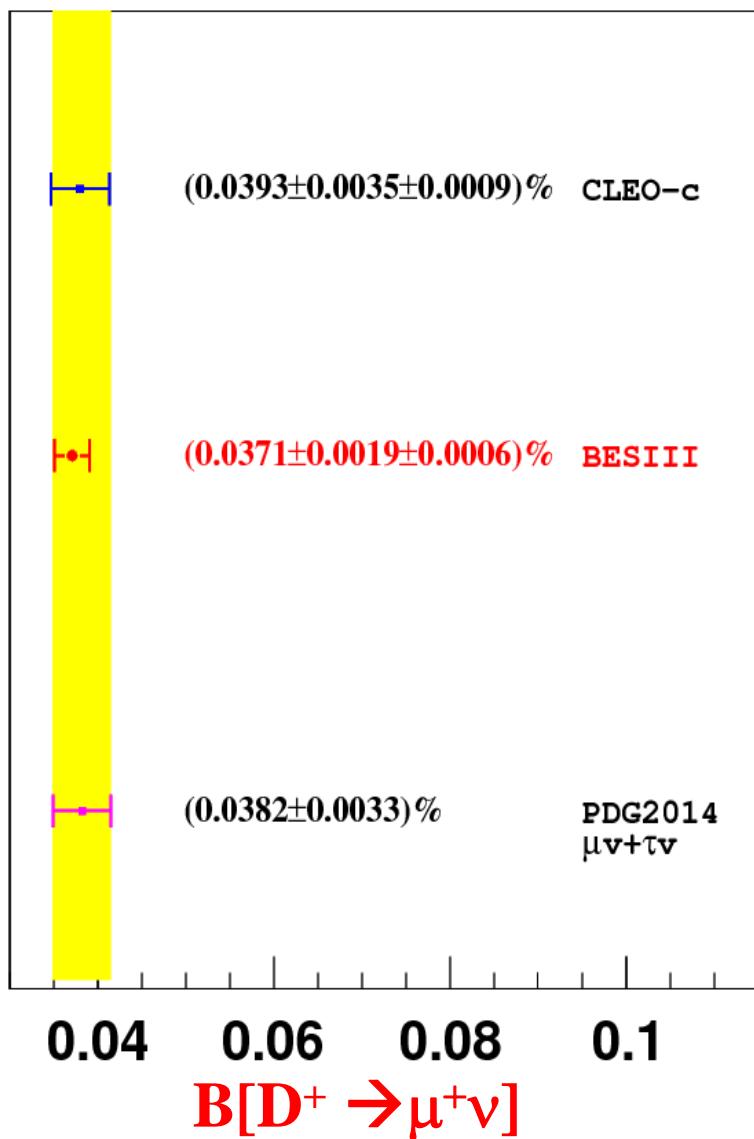
2.92 fb^{-1} data@ 3.773 GeV
PRD89(2014)051104R



Input t_{D^+} , m_{D^+} , m_{μ^+} on PDG and
LQCD calculated $f_{D^+} = 207 \pm 4$
MeV[PRL100(2008)062002]

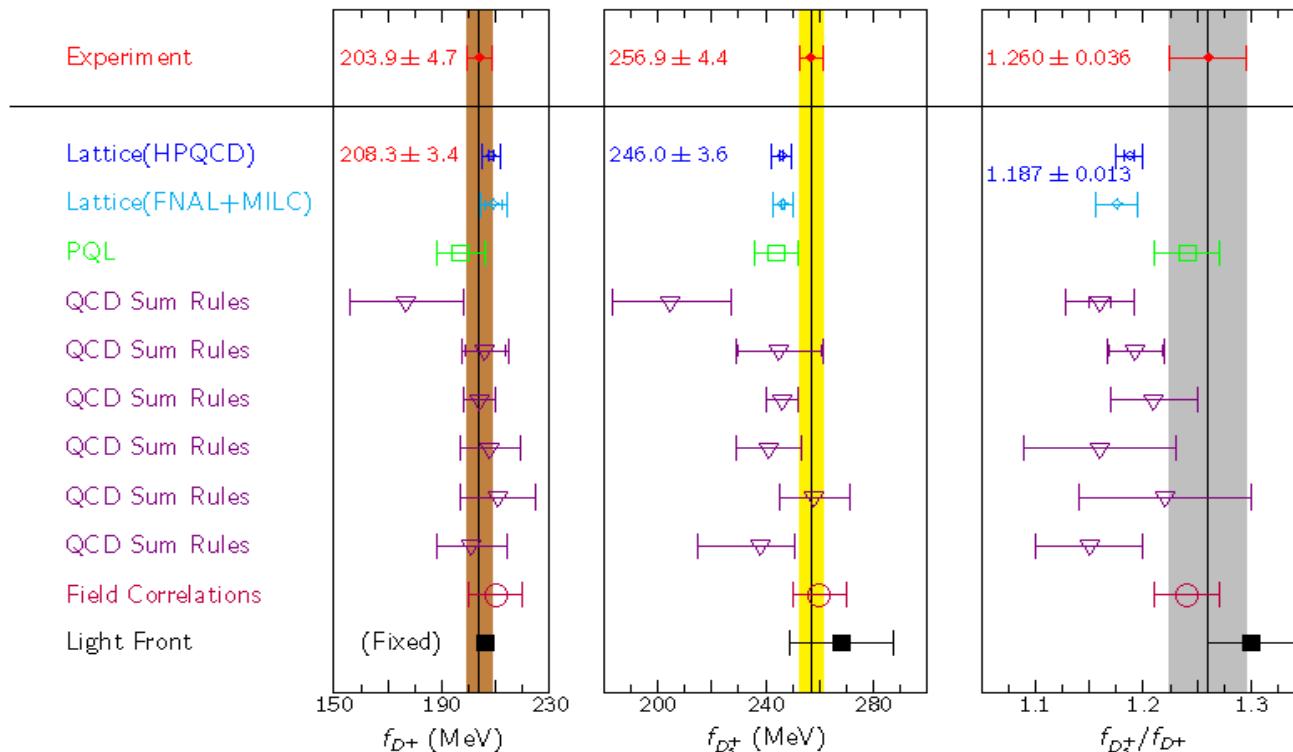
$$|V_{cd}| = 0.2210 \pm 0.0058 \pm 0.0047$$

Comparisons of $B[D^+ \rightarrow \mu^+ \nu_\mu]$ and f_{D^+}



Comparisons of Existing f_{D+} , $f_{D_{s+}}$ and $f_{D+}:f_{D_{s+}}$

Taken from Gang Rong's talk at CKM2014



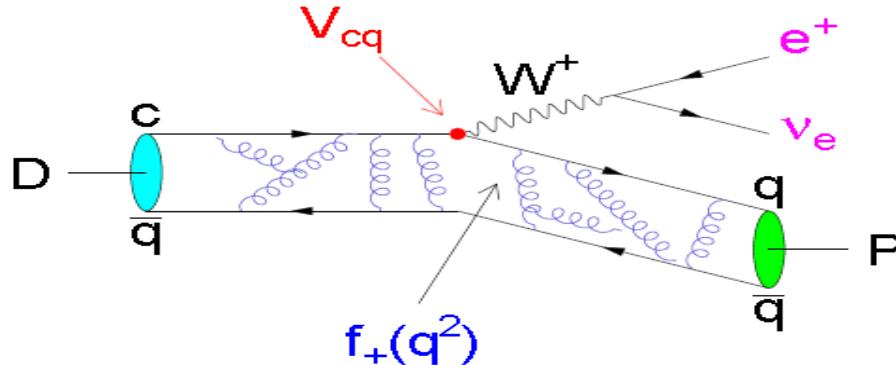
- Precisions of the LQCD calculations of f_{D+} , $f_{D_{s+}}$, $f_{D+}:f_{D_{s+}}$ reach 0.5%, 0.5% and 0.3%, which are challenging the experiments

- The experimentally measured and the theoretically calculated f_{D+} , $f_{D_{s+}}$, $f_{D+}:f_{D_{s+}}$ differ by about 2σ

	Experiments	Femilab Lattice+MILC (2014)		HPQCD (2012)	
	Averaged	Expected	Δ	Expected	Δ
f_{D+} (MeV)	203.9 ± 4.7	$212.6 \pm 0.4^{+1.0}_{-1.2}$	1.8σ	208.3 ± 3.4	0.8σ
$f_{D_{s+}}$ (MeV)	256.9 ± 4.4	$249.0 \pm 0.3^{+1.1}_{-1.5}$	1.7σ	246.0 ± 3.6	1.4σ
$f_{D+}:f_{D_{s+}}$	1.260 ± 0.036	$1.1712 \pm 0.0010^{+0.0029}_{-0.0032}$	2.5σ	1.187 ± 0.013	1.9σ

- Improving measurement with larger data sample is necessary!

Semi-leptonic Decay $D^0 \rightarrow K(\pi) e^+ \nu$



Differential rates:
$$\frac{d\Gamma}{dq^2} = X \frac{G_F^2 |V_{cd(s)}|^2}{24\pi^3} p^3 |f_+(q^2)|^2$$

Bridge to precisely measure:

■ **Form factors $f_+^{D \rightarrow K(\pi)}(0)$ with input $|V_{cd(s)}|_{\text{CKMfitter}}$**

– Single pole form

$$f_+(q^2) = \frac{f_+(0)}{1 - \frac{q^2}{M_{\text{pole}}^2}}$$

– Modified pole model

$$f_+(q^2) = \frac{f_+(0)}{(1 - \frac{q^2}{M_{\text{pole}}^2})(1 - \alpha \frac{q^2}{M_{\text{pole}}^2})}$$

– ISGW2 model

$$f_+(q^2) = f_+(q_{\max}^2) \left(1 + \frac{r_{\text{ISGW2}}^2}{12} (q_{\max}^2 - q^2)\right)^{-2}$$

– Series expansion model

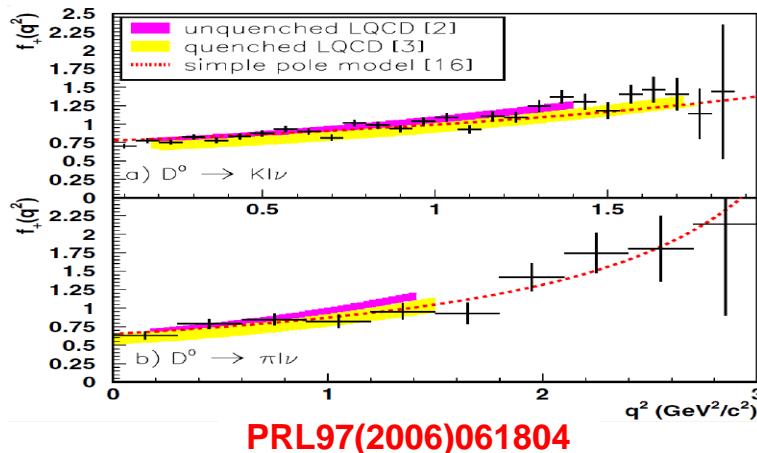
$$f_+(t) = \frac{1}{P(t)\Phi(t, t_0)} a_0(t_0) \left(1 + \sum_{k=1}^{\infty} r_k(t_0) [z(t, t_0)]^k\right)$$

■ **CKM matrix element $|V_{cs(d)}|$ with input $f_+^{\text{LQCD}, D \rightarrow K(\pi)}(0)$**

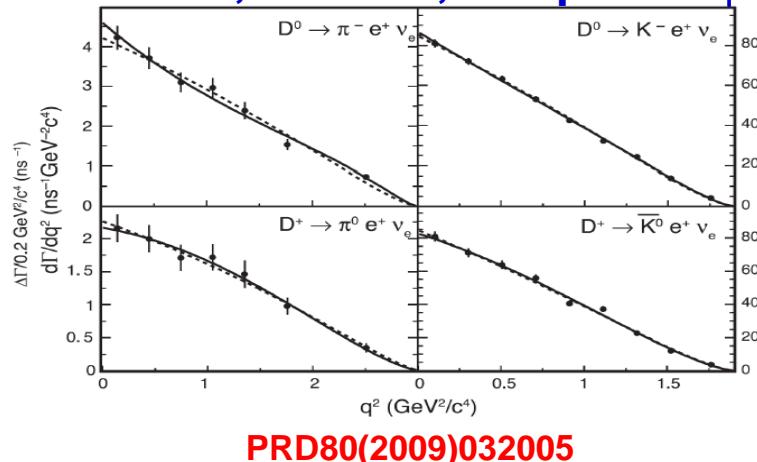
Progress of Extracting $f_+^{D \rightarrow K(\pi)}(0) |V_{cs(d)}|$

During the past 26 years, studies of $D \rightarrow K(\pi)\ell^+\nu$ are made by MARKIII, E691, CLEO, CLEOII, BESII, FOCUS, BELLE, Babar and CLEO-c

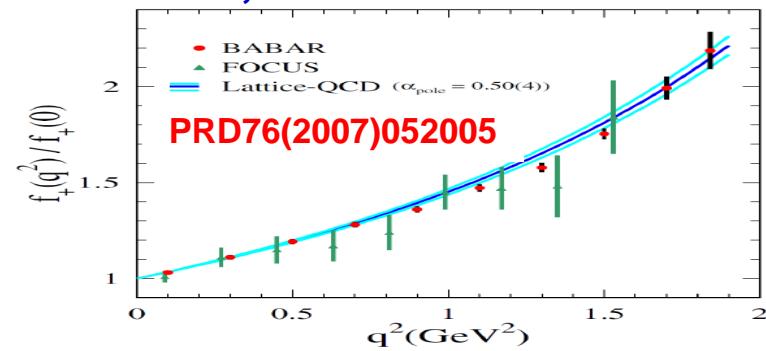
■ BELLE, 282 fb^{-1} at 10.58 GeV



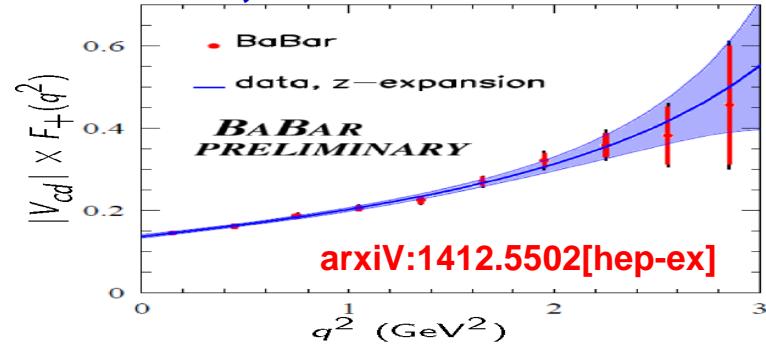
■ 2004-2009, CLEO-c, 818 pb^{-1} at ψ''



■ Babar, 75 fb^{-1} at 10.58 GeV



■ Babar, 347.2 fb^{-1} at 10.58 GeV

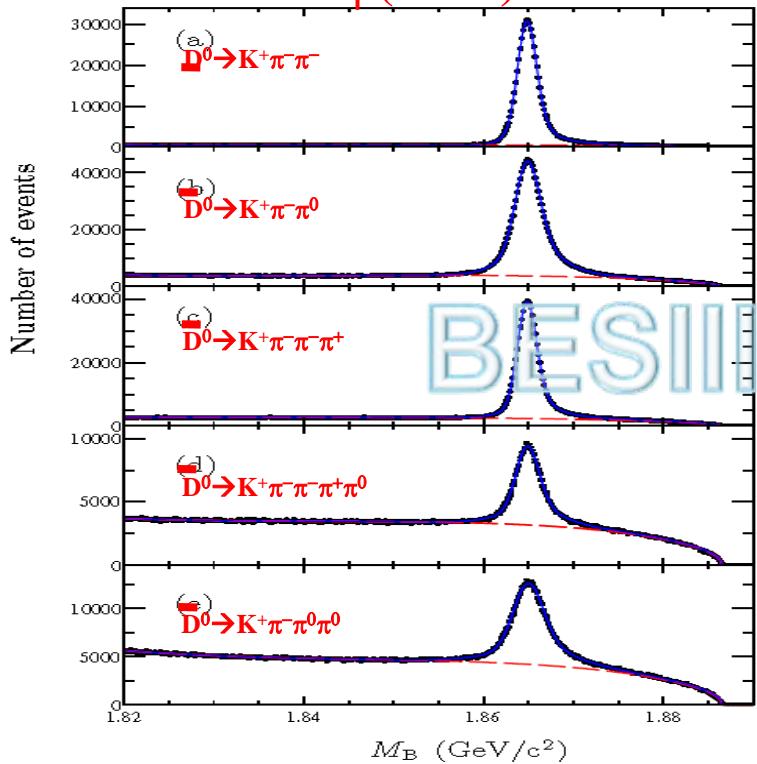


Before 2010, the LQCD calculated $f_+^{D \rightarrow K(\pi)}(0)$ precision is at 10% level, thus limiting $|V_{cs(d)}|$ measurement

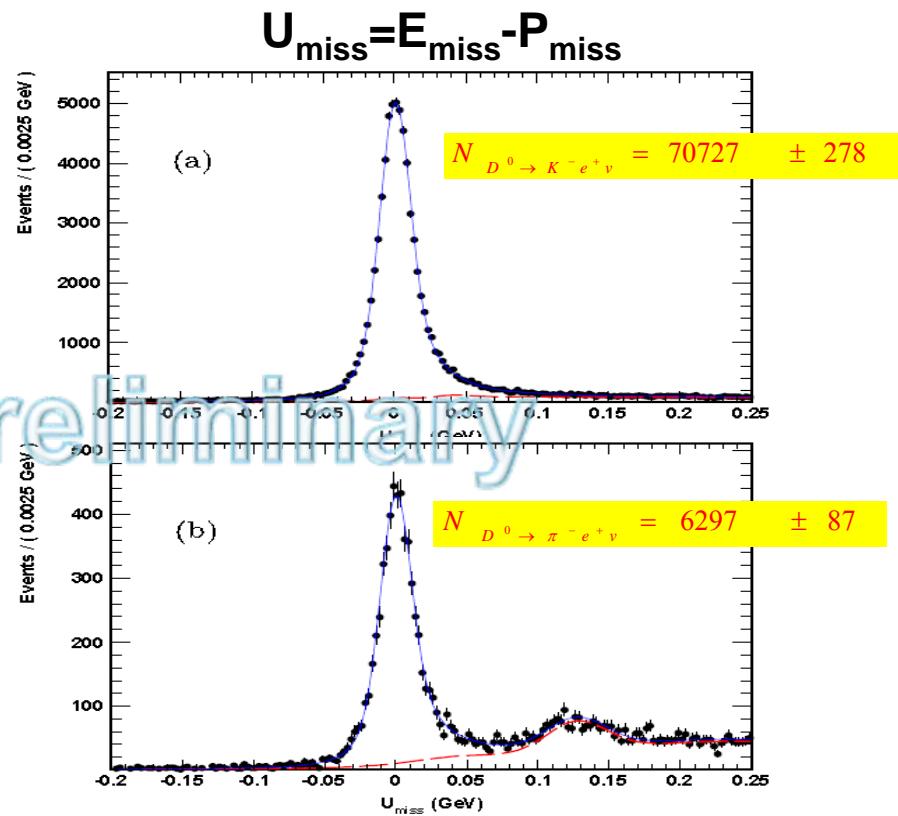
Improved $B[D^0 \rightarrow K(\pi)^- e^+ v]$ at BESIII

2.92 fb⁻¹ data@ 3.773 GeV

$e^+e^- \rightarrow \psi(3770) \rightarrow D^0\bar{D}^0$



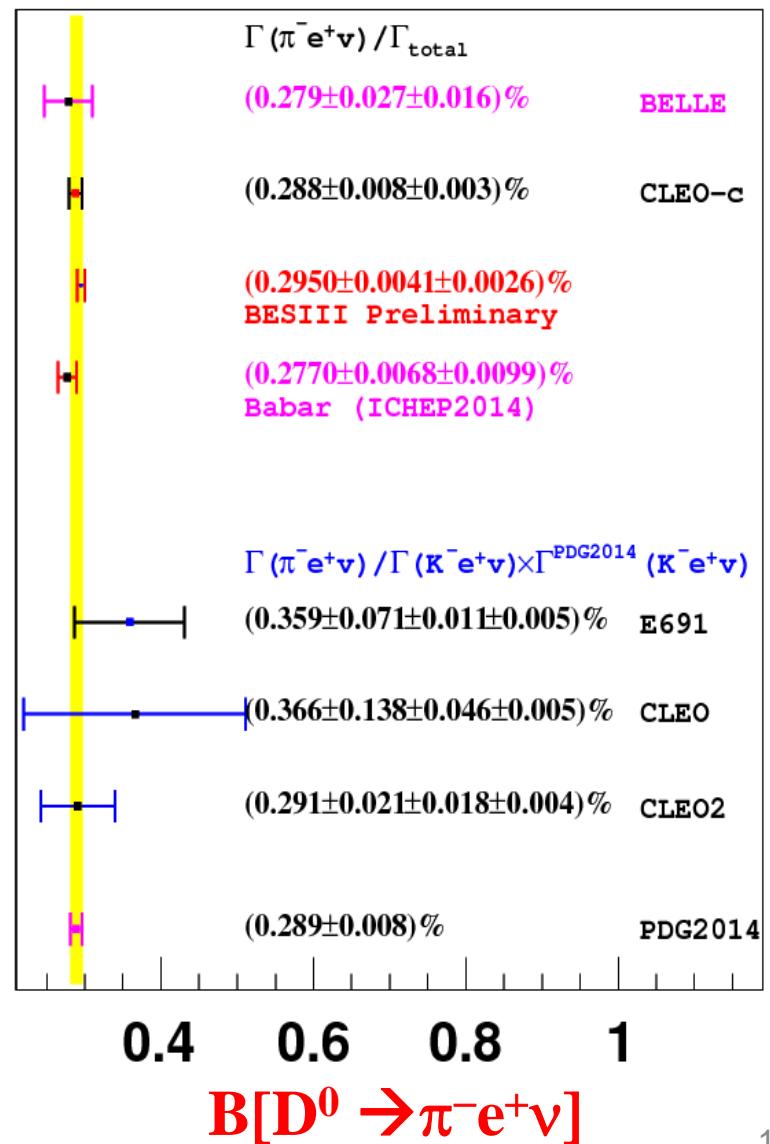
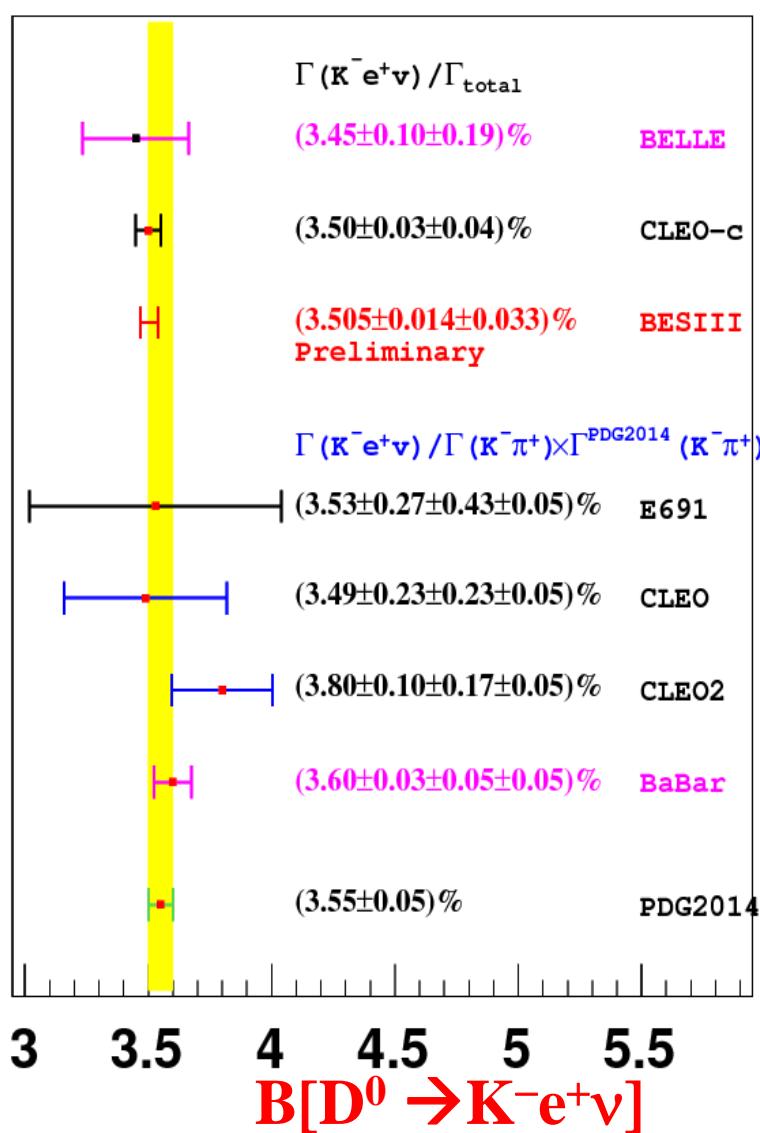
$$N_{\bar{D}^0 \text{ tag}} = (279.33 \pm 0.37) \times 10^{-4}$$



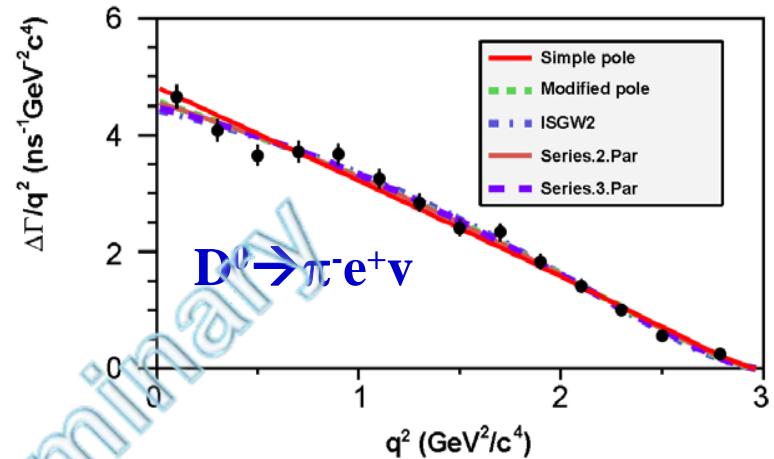
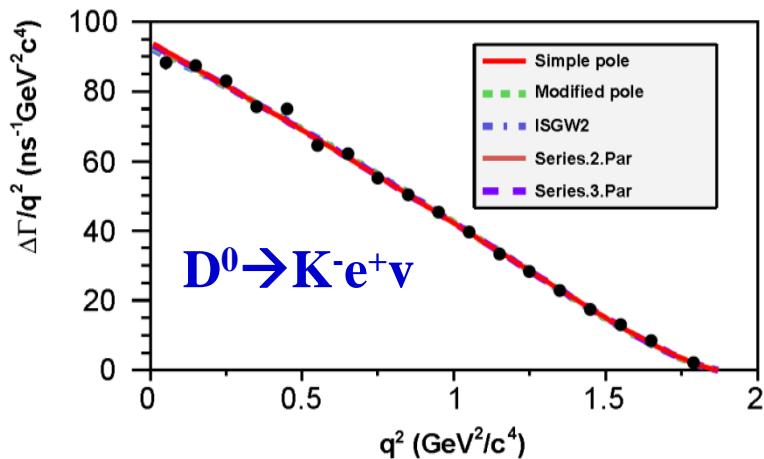
$$B_{D^0 \rightarrow K^- e^+ v} = (3.505 \pm 0.014 \pm 0.033)\%$$

$$B_{D^0 \rightarrow \pi^- e^+ v} = (0.2950 \pm 0.0041 \pm 0.0026)\%$$

Comparisons of $B[D^0 \rightarrow K^-(\pi^-)e^+\nu]$

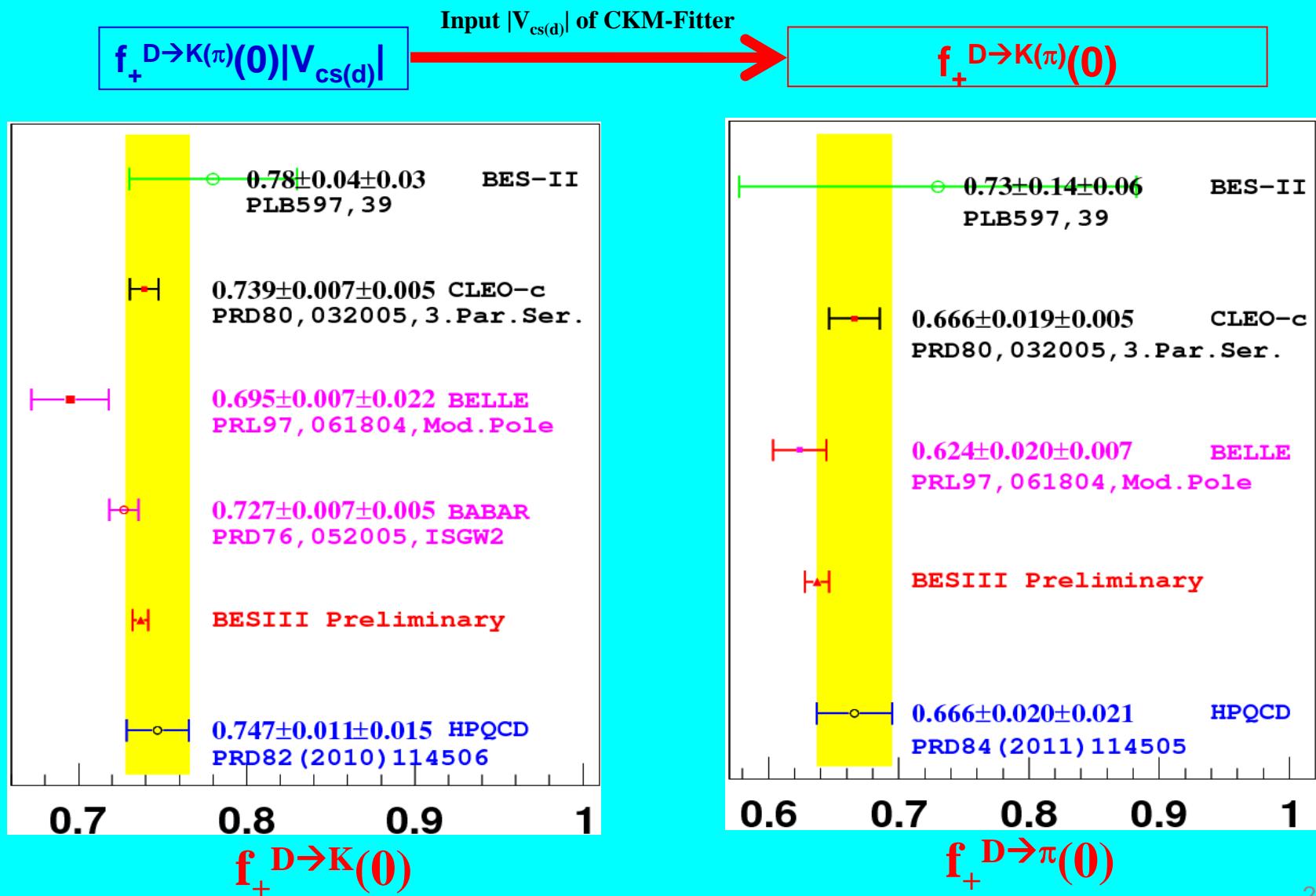


Extracted Parameters of Form Factors



		$D^0 \rightarrow K^- e^+ \bar{\nu}$		$D^0 \rightarrow \pi^- e^+ \bar{\nu}$
Simple Pole	$f_K^+(0) V_{cs} $	$0.7209 \pm 0.0022 \pm 0.0033$	$f_\pi^+(0) V_{cd} $	$0.1475 \pm 0.0014 \pm 0.0005$
	M_{pole}	$1.9207 \pm 0.0103 \pm 0.0069$	M_{pole}	$1.9114 \pm 0.0118 \pm 0.0038$
Mod. Pole	$f_K^+(0) V_{cs} $	$0.7163 \pm 0.0024 \pm 0.0034$	$f_\pi^+(0) V_{cd} $	$0.1437 \pm 0.0017 \pm 0.0008$
	α	$0.3088 \pm 0.0195 \pm 0.0129$	α	$0.2794 \pm 0.0345 \pm 0.0113$
ISGW2	$f_K^+(0) V_{cs} $	$0.7139 \pm 0.0023 \pm 0.0034$	$f_\pi^+(0) V_{cd} $	$0.1415 \pm 0.0016 \pm 0.0006$
	r_{ISGW2}	$1.6000 \pm 0.0141 \pm 0.0091$	r_{ISGW2}	$2.0688 \pm 0.0394 \pm 0.0124$
Series.2.Par	$f_K^+(0) V_{cs} $	$0.7172 \pm 0.0025 \pm 0.0035$	$f_\pi^+(0) V_{cd} $	$0.1435 \pm 0.0018 \pm 0.0009$
	r_1	$-2.2278 \pm 0.0864 \pm 0.0575$	r_1	$-2.0365 \pm 0.0807 \pm 0.0260$
Series.3.Par	$f_K^+(0) V_{cs} $	$0.7196 \pm 0.0035 \pm 0.0041$	$f_\pi^+(0) V_{cd} $	$0.1420 \pm 0.0024 \pm 0.0010$
	r_1	$-2.3331 \pm 0.1587 \pm 0.0804$	r_1	$-1.8434 \pm 0.2212 \pm 0.0690$
	r_2	$3.4223 \pm 3.9090 \pm 2.4092$	r_2	$-1.3871 \pm 1.4615 \pm 0.4677$

Improved Form factor $f_+^{D \rightarrow K(\pi)(0)}$ at BESIII



Improved $|V_{cs(d)}|$ at BESIII

Method 1

$$B[D_{(s)}^+ \rightarrow l^+ \nu]$$

Input t_{D_s} , m_{D_s} , m_{μ^+} on PDG and
LQCD calculated $f_{D(s)+}$

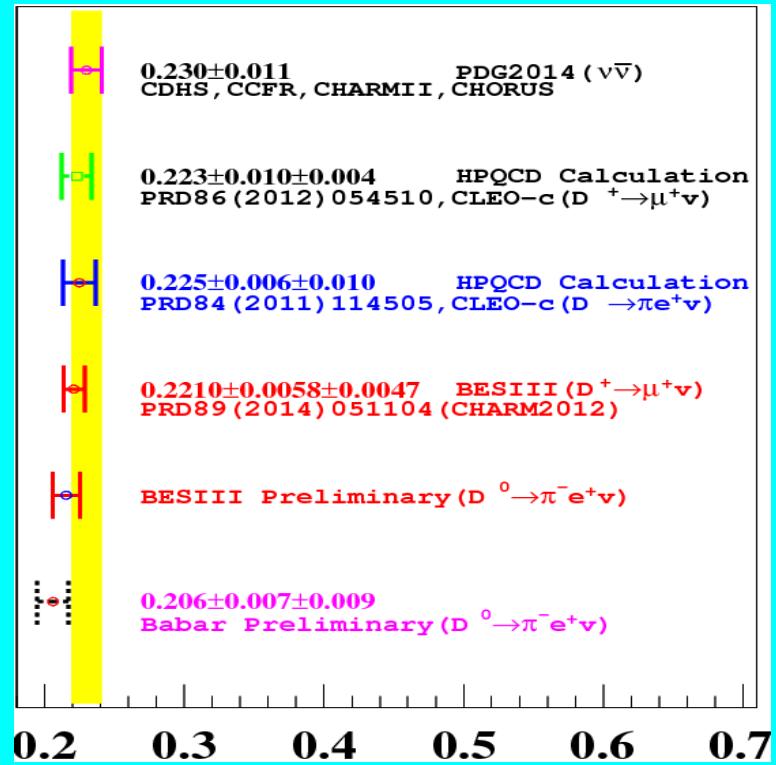
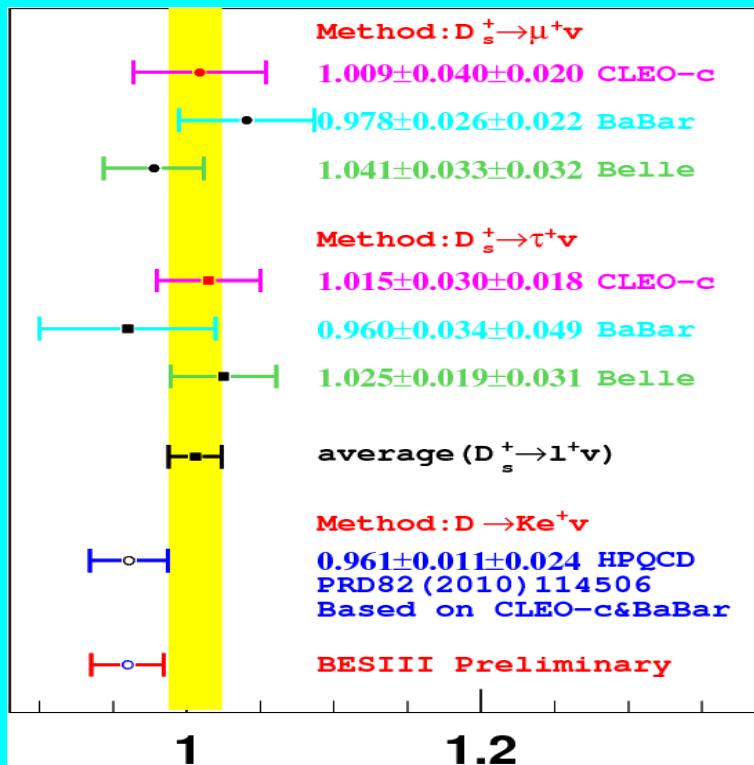
$$|V_{cd(s)}|$$

Method 2

$$f_+^{D \rightarrow K(\pi)}(0) |V_{cs(d)}|$$

Input $f_+^{D \rightarrow K(\pi)}(0)$ of LQCD

$$|V_{cs(d)}|$$



Method 2 suffers larger theoretical uncertainty in $f_+^{D \rightarrow K(\pi)}(0)$ [2.4(4.4)%]

Summary of BESIII results

- With 2.92 fb^{-1} data taken at 3.773 GeV by BESIII, we study the leptonic decay of $D^+ \rightarrow \mu^+ \nu$ and the semi-leptonic decay $D^0 \rightarrow K(\pi) e^+ \nu$
- We provide improved measurement of decay constant f_{D^+} and form factor $f_+^{D \rightarrow K(\pi)}(q^2)$, which are important to test and calibrate LQCD calculations accurately
- We provide improved measurement of CKM matrix element $|V_{cs(d)}|$, which is important for unitarity test of the CKM matrix
- BESIII will take 3 fb^{-1} data at 4.17 GeV in 2016, improved measurement of $f_{D_s^+}$ and $|V_{cs}|$ by $D_s^+ \rightarrow l^+ \nu$ is expected in the near future

Why HIEPA is expected?

Leptonic decay $D_{(s)}^+ \rightarrow l^+ \nu$

- Measurement of $f_{D(s)+}$ and $|V_{cd(s)}|$ is limited by data size
- More precise $f_{D+}, f_{Ds+}, f_{D+}:f_{Ds}$ is expected
 1. Challenge from LQCD calculation with 0.5%, 0.5% and 0.3% precisions
 2. $\sim 2\sigma$ difference between experiment and theoretical calculation

Semi-leptonic decay $D^0 \rightarrow K(\pi) e^+ \nu$

- Measurement of $f_+^{D \rightarrow \pi}(0)$ is limited by data size
- Measurement of $|V_{cs(d)}|$ is limited by $f_+^{\text{LQCD}, D \rightarrow K(\pi)}(0)$

Improving $|V_{cs(d)}|, f_{D(s)+}, f_+^{D \rightarrow K(\pi)}(0)$ statistical
precisions by an order of magnitude at HIEPA?

Prospects at HIEPA?

Opportunity: If we have 300 fb^{-1} data at 3.773 GeV and 300 fb^{-1} data at $4.17/4.03 \text{ GeV}$, what precisions we can reach?

Roughly estimate based on BESIII and CLEO-c experiments

	Systematic error	Statistical error		
		$\sim 3 \text{ fb}^{-1}$	12 fb^{-1}	300 fb^{-1}
$\Delta f_{D+}/f_{D+}$	$\sim 0.9\%^{\text{BESIII}}$	2.6%	1.3%	0.26%
$\Delta f_{D_s+}/f_{D_s+}$	$\sim 1.5\%^{\text{CLEO-c}}$	$1.1\%/2.0\%$	$0.6\%/1.0\%$	$0.11\%/0.20\%$
$\Delta f_{D \rightarrow K}/f_{D \rightarrow K}$	$\sim 0.5\%^{\text{BESIII}}$	0.35%	0.18%	0.04%
$\Delta f_{D \rightarrow \pi}/f_{D \rightarrow \pi}$	$\sim 0.7\%^{\text{BESIII}}$	1.26%	0.63%	0.13%
$ V_{cs} ^{D_s+ \rightarrow l+v}$	$\sim 2.0\%^{\text{CLEO-c}}$	$1.8\%/3.0\%$	$0.9\%/1.5\%$	$0.18\%/0.30\%$
$ V_{cs} ^{D^0 \rightarrow K-e+v}$	$2.5\%^{\text{BESIII}}(2.4\%^{\text{LQCD}})$	0.35%	0.18%	0.04%
$ V_{cd} ^{D+ \rightarrow \mu+\nu}$	$2.1\%^{\text{BESIII}}(1.9 \rightarrow 0.5\%^{\text{LQCD}})$	2.6%	1.3%	0.26%
$ V_{cd} ^{D^0 \rightarrow \pi-e+\nu}$	$4.5\%^{\text{BESIII}}(4.4\%^{\text{LQCD}})$	1.26%	0.63%	0.13%

Challenges:

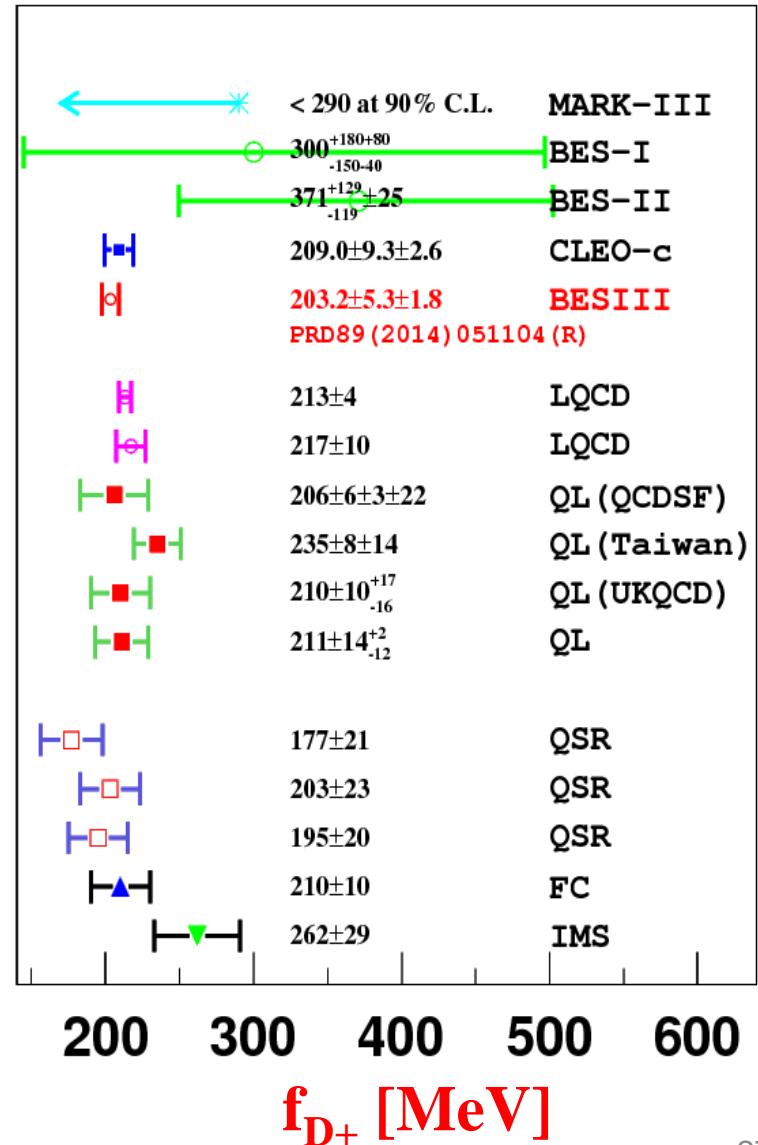
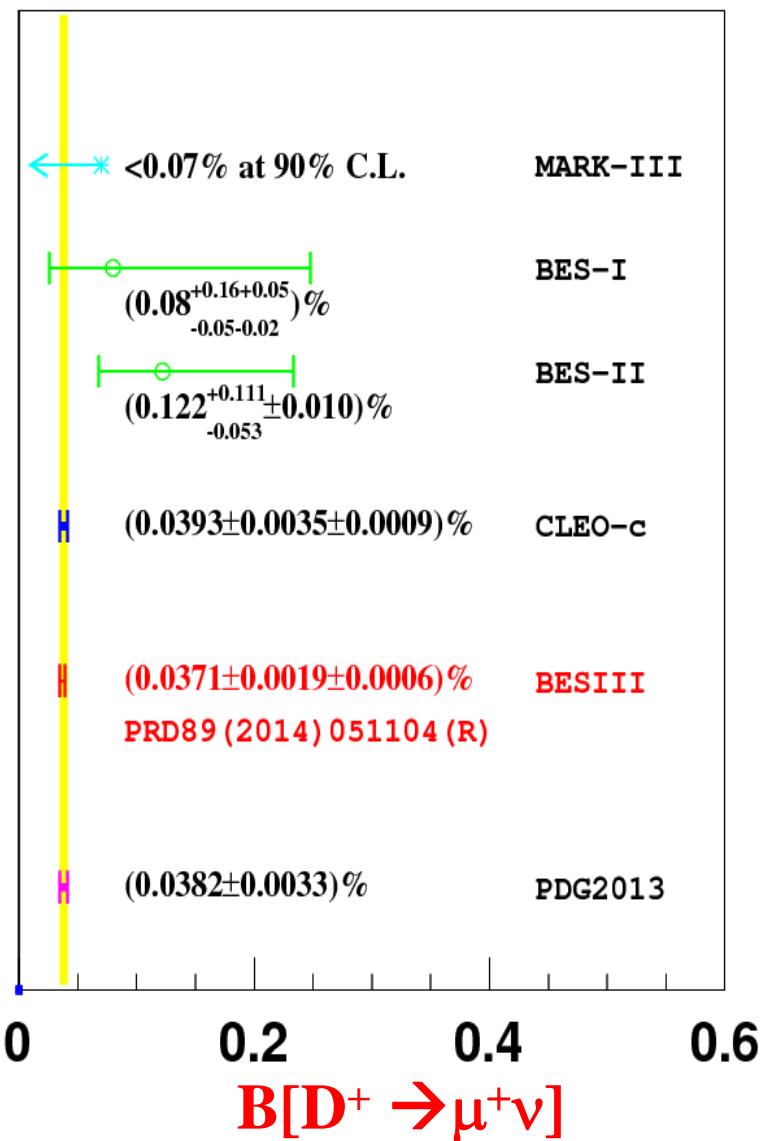
- Measuring $|V_{cs(d)}|$ by $D \rightarrow K(\pi)e^+\nu$ will be limited by LQCD calculation precision of $f_+^{D \rightarrow K(\pi)}(0)$, whether it can reach 0.5% level?

- Measuring f_{D_s+} and $|V_{cs}|$ will be limited by systematic error of selecting $D_s^+ \rightarrow l^+\nu$, whether it can reach 1.0% level?

Thank you!

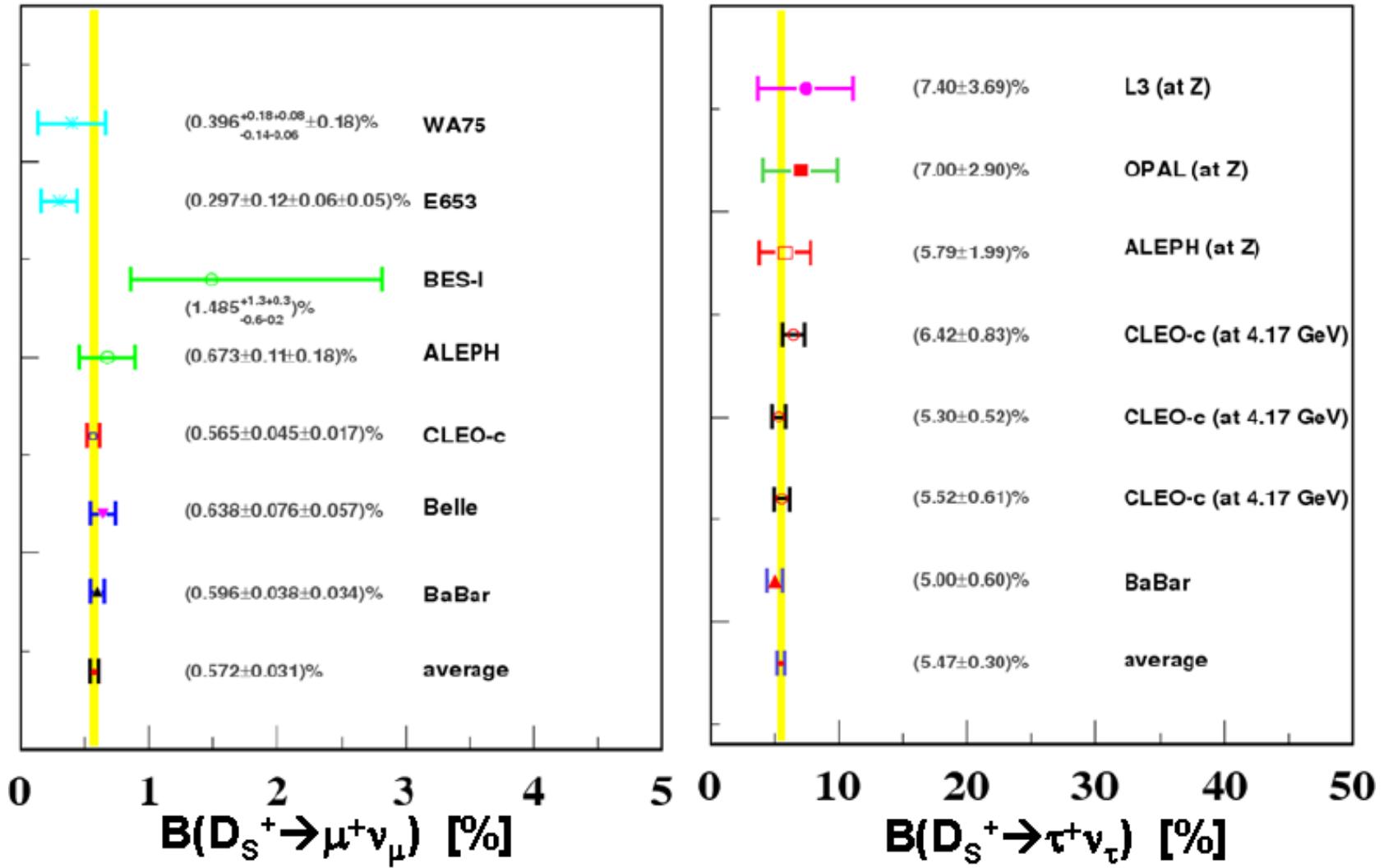
Back-up slides

Comparisons of $B[D^+ \rightarrow \mu^+ \nu_\mu]$ and f_{D^+}



Comparisons of $B[D_{(s)}^+ \rightarrow l^+ \nu]$

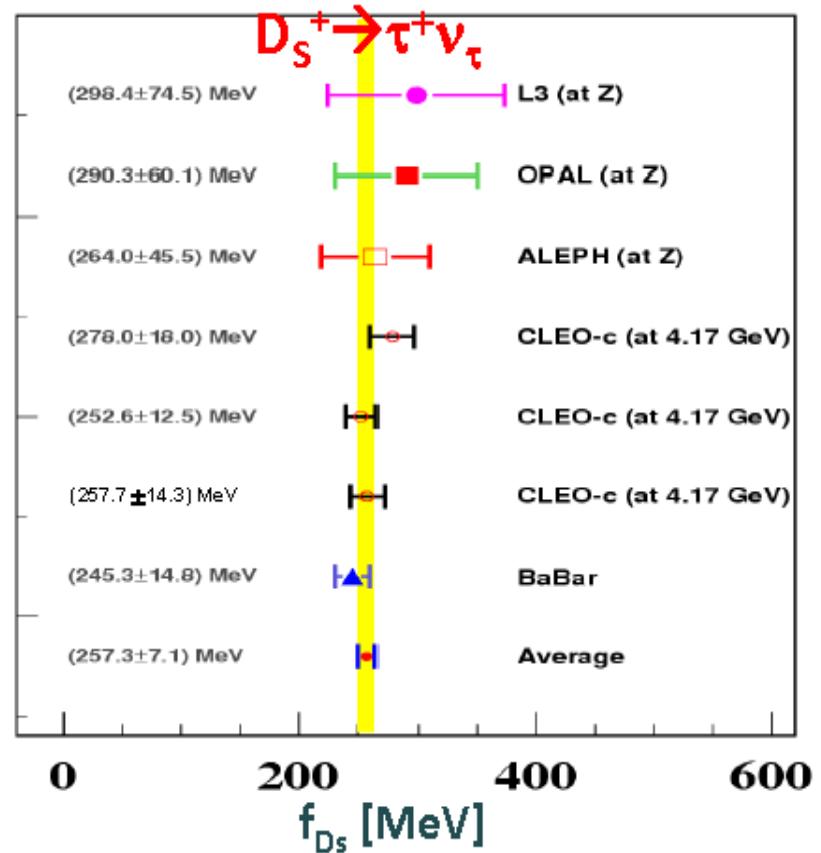
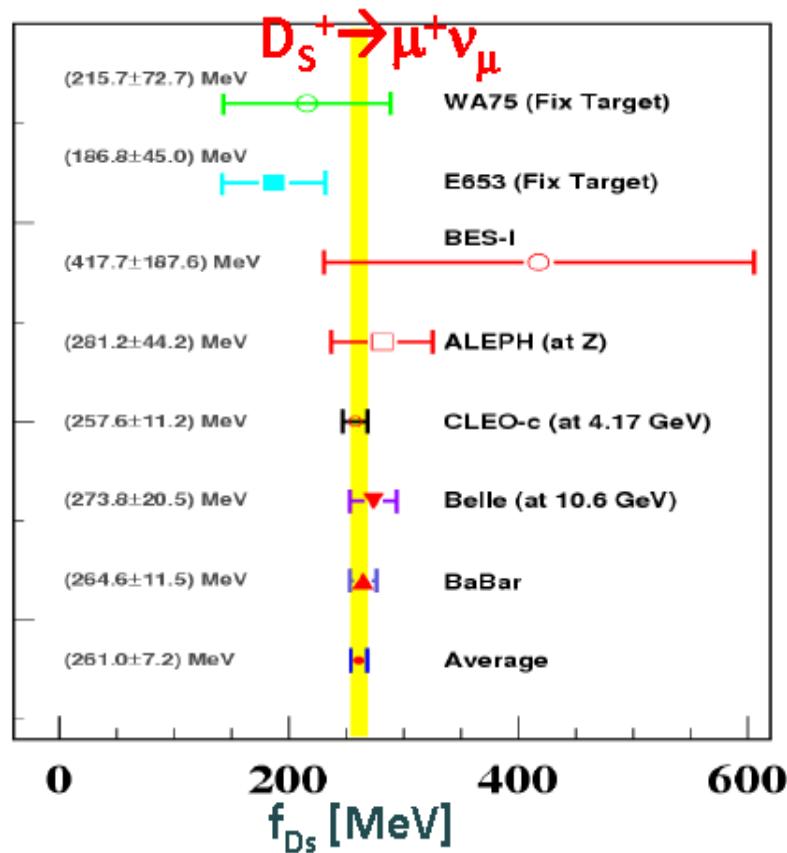
Taking from Gang Rong's talk at CHARM2012



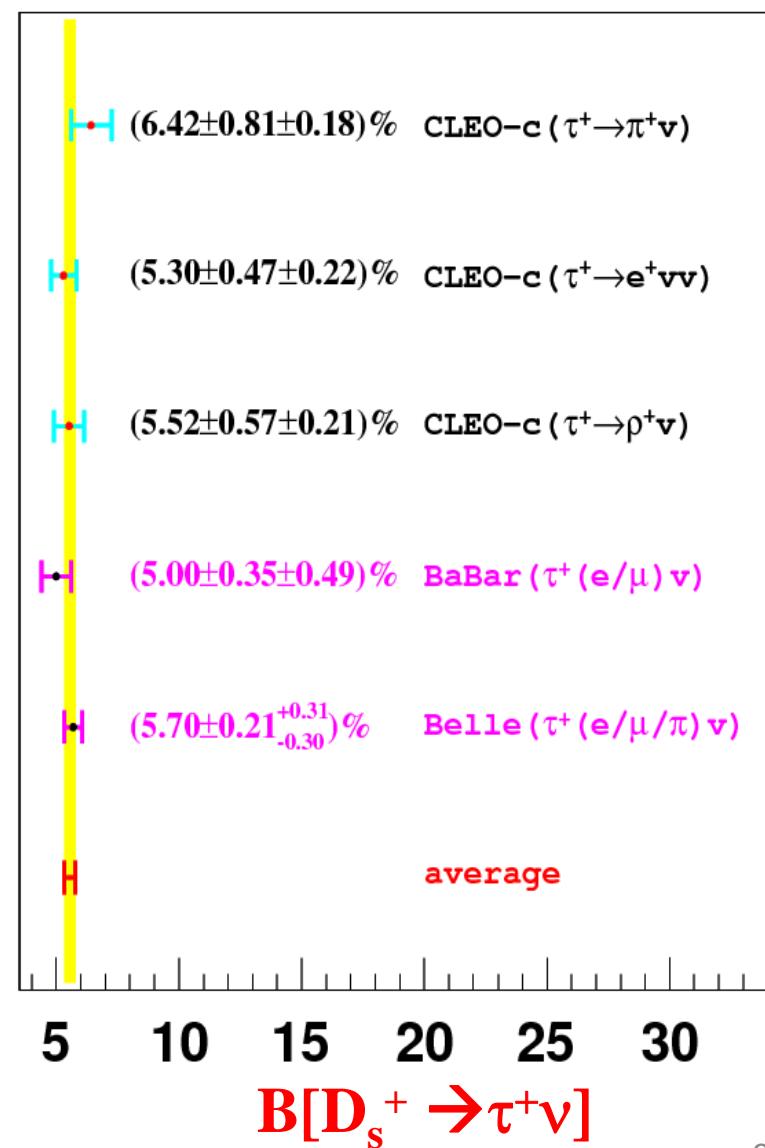
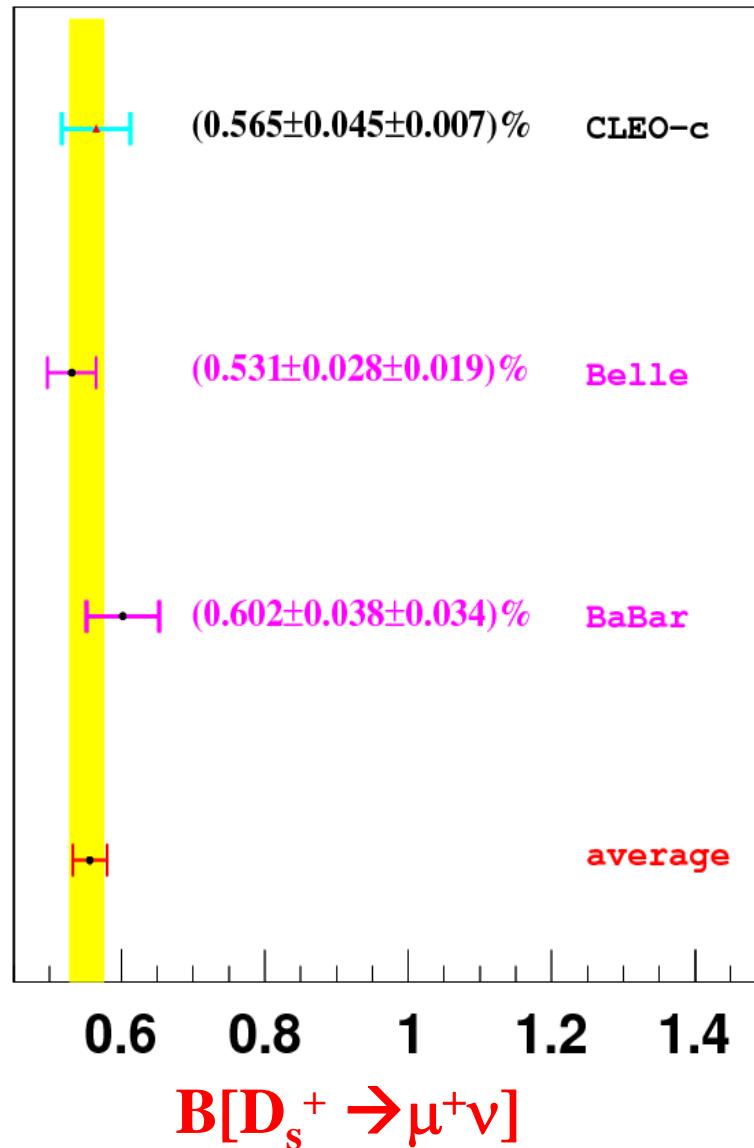
Comparisons of $B[D_{(s)}^+ \rightarrow l^+ \nu]$ and $f_{D_s^+}$

Taking from Gang Rong's talk at CHARM2012

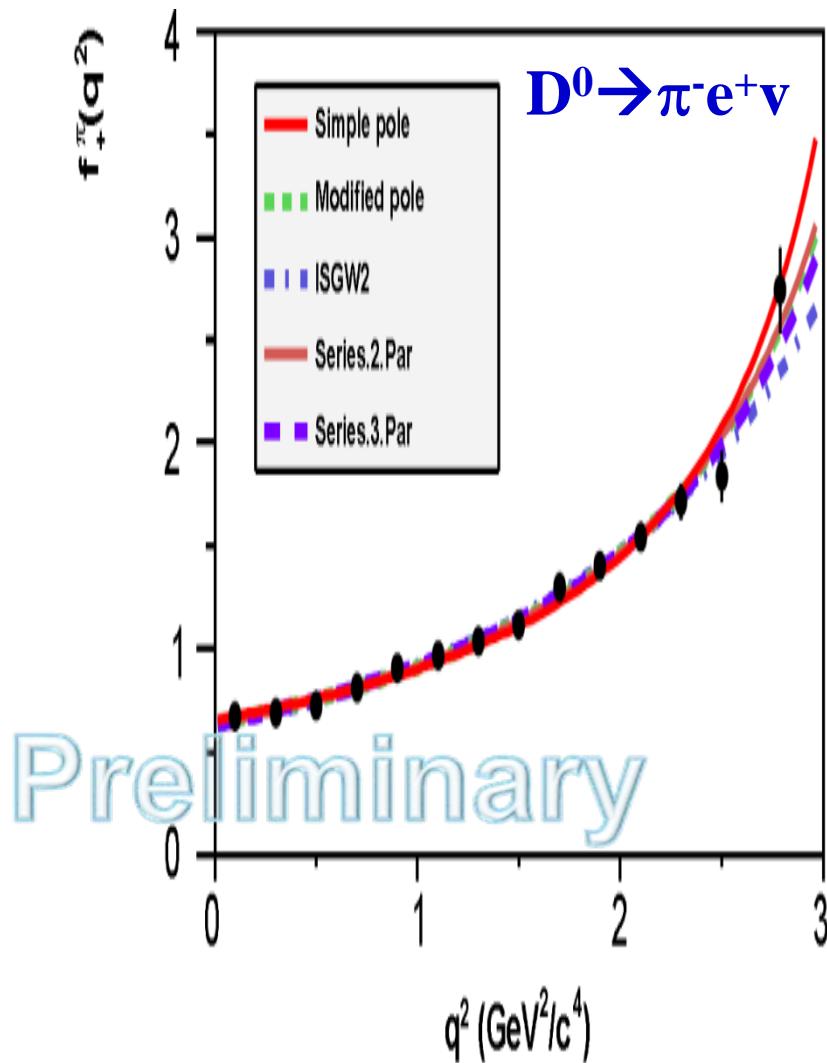
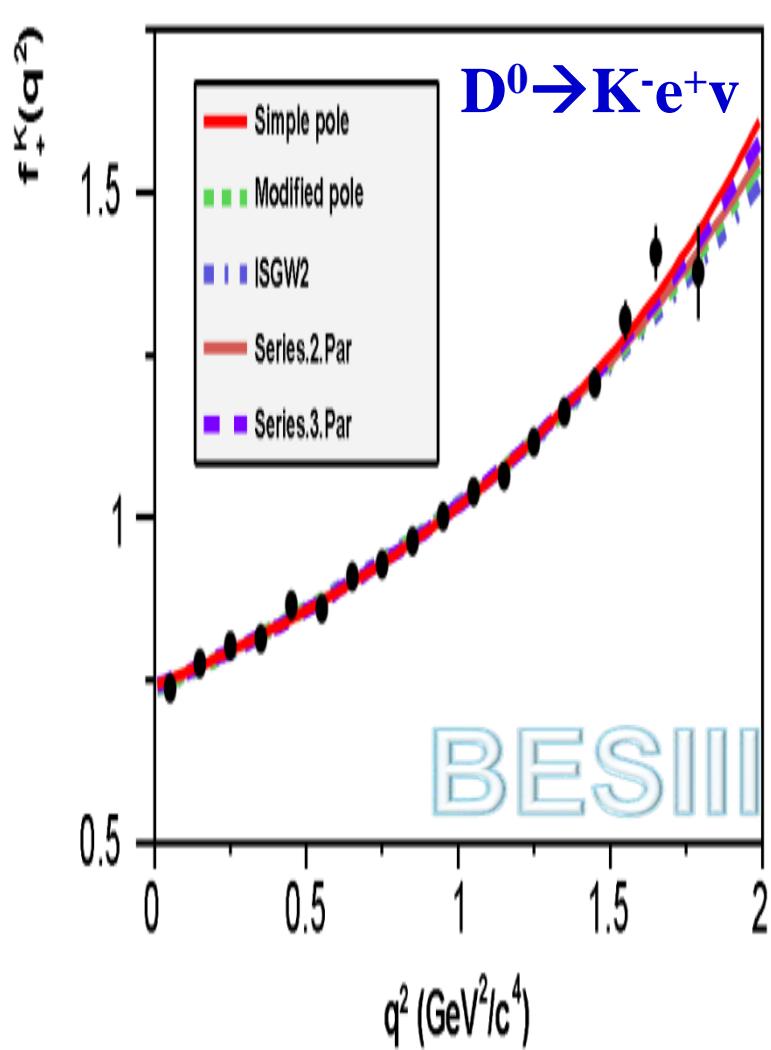
Based on the measured branching fractions of D_s^+ leptonic decays (after radiative correction), and with inputs of D_s^+ mass, lepton mass, D_s^+ lifetime and $|V_{cs}|=0.97345$ from CKMfitter, we calculate the f_{D_s} .



Comparisons of existing $B[D_s^+ \rightarrow \mu^+\nu]$

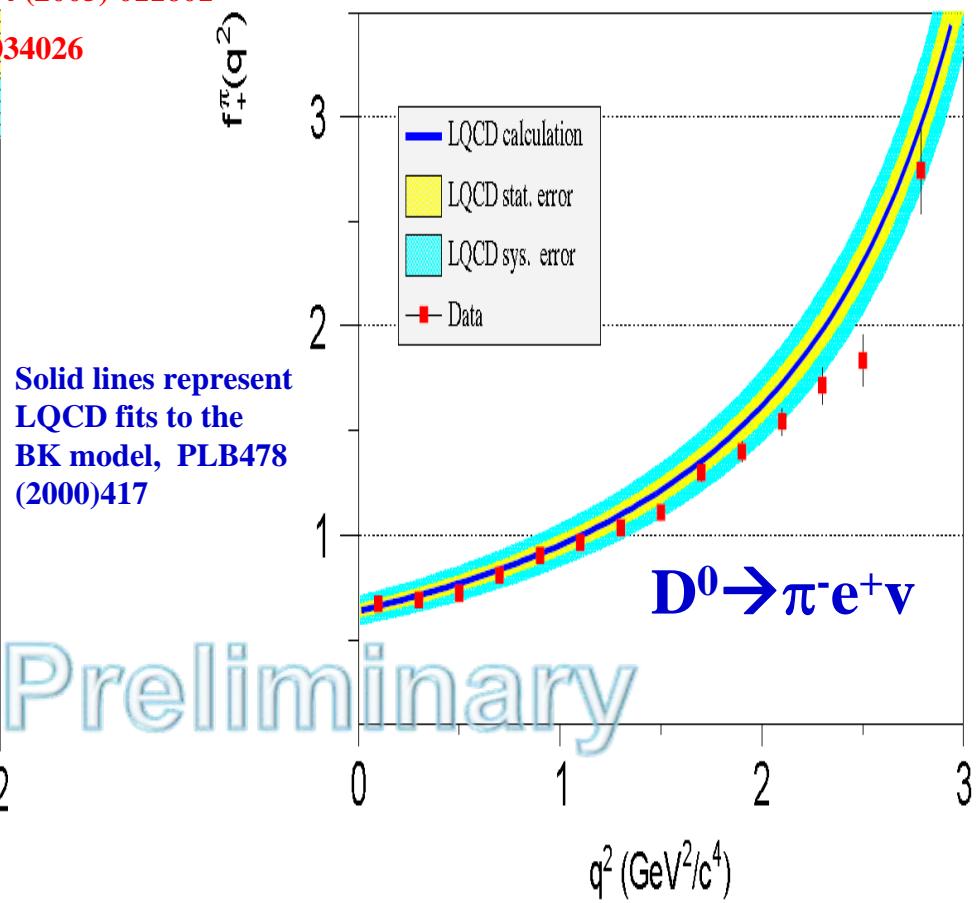
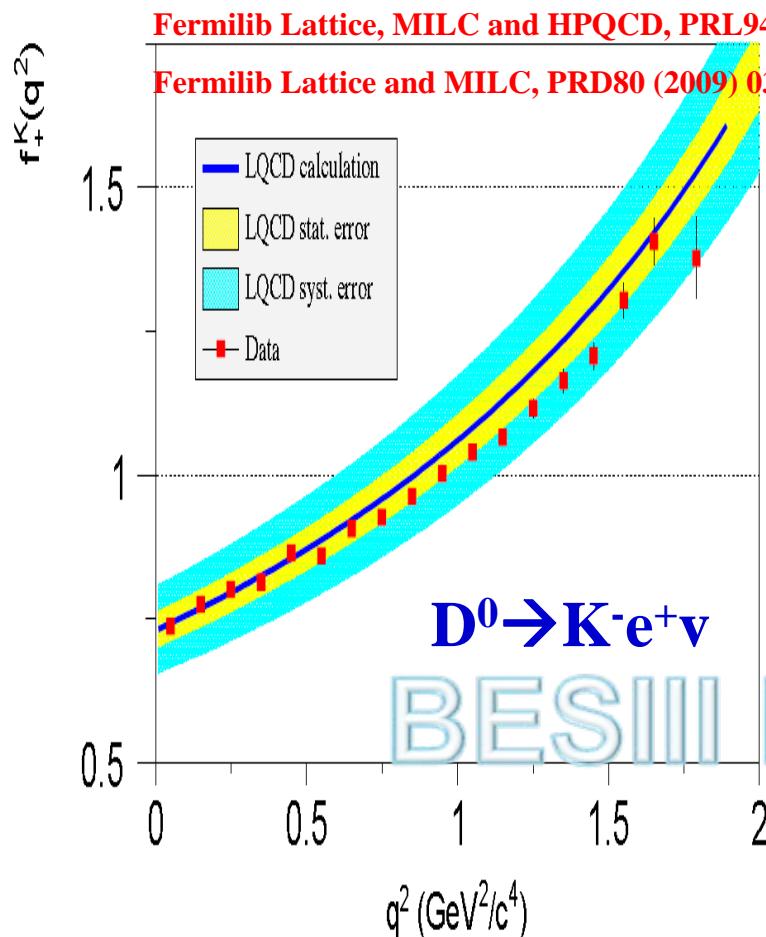


Projections on Form Factors $f_{+}^{K(\pi)}(q^2)$



Comparisons of Form Factors

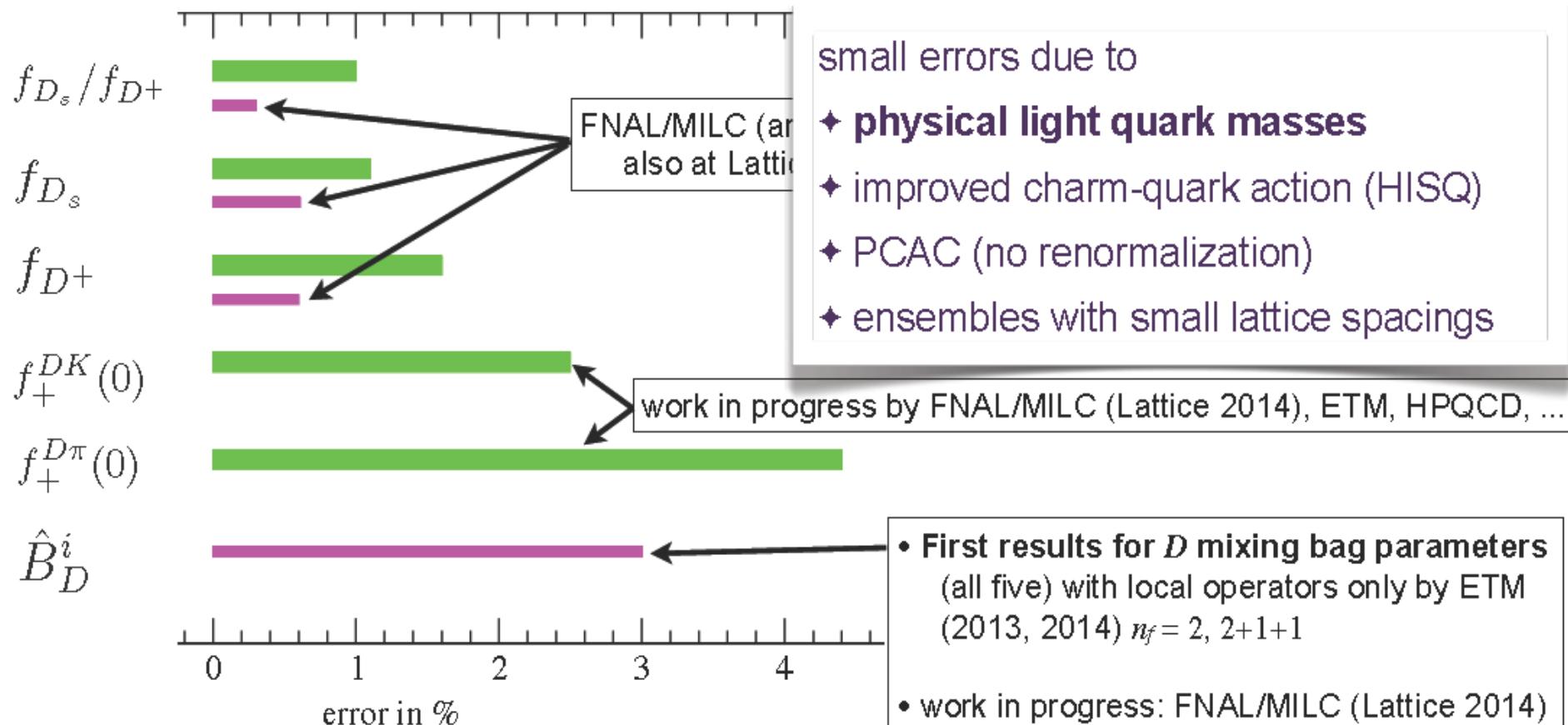
Experimental data calibrate LQCD calculation



Progress in LQCD Calculation

Taking from Aida X. El-Khadra's talk at Beauty2014

errors (in %) comparison: **FLAG-2 averages** vs. **new results**



review by C. Bouchard @ Lattice 2014