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The Abdus Salam
International Centre
for Theoretical Physics

Collins fragmentation functions at BABAR and BESIII



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ON BEHALF OF BESIII AND BABAR COLLABORATIONS

TMD_e2015 - A PATH TOWARDS TMD EXTRACTION

2-4 SEPTEMBER 2015 TRIESTE - ITALY



Outline

- ❖ **Introduction**
 - ❖ The Collins effect
 - ❖ The BaBar and BESIII experiments
- ❖ **Collins asymmetries for $\pi\pi$ pairs**
 - ❖ BaBar results
 - ❖ BESIII preliminary results
- ❖ **BaBar preliminary results: Collins asymmetries for KK and $K\pi$ hadron pairs**
- ❖ **Summary and conclusions**

Introduction: the Collins effect

Our understanding of the hadronic physics depends strongly on what we know about the parton distributions functions (PDFs) and **fragmentation functions** (FFs)

- Universal
- Non-perturbative objects

Transverse Momentum Dependent (TMD) FFs \Rightarrow to study the spin-dependent observables

- when only spinless hadrons (π , K) are considered, we have:

$$q^\uparrow \rightarrow hX: \quad D_1^{q^\uparrow}(z, \mathbf{P}_\perp; s_q) = D_1^q(z, P_\perp) + \frac{P_\perp}{zM_h} \overline{H_1^{\perp q}}(z, P_\perp) \mathbf{s}_q \cdot (\mathbf{k}_q \times \mathbf{P}_\perp)$$

Unpolarized FF

Collins FF [NPB 396, 161 (1993)]: chiral-odd function, related to the probability that a transversely polarized quark (q^\uparrow) fragments into a spinless hadron

Physics motivation:

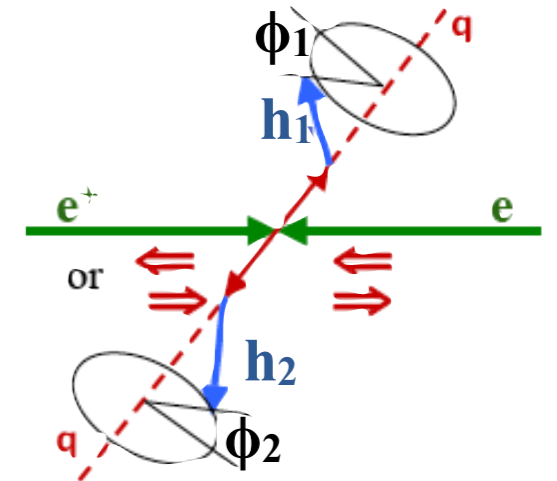
- e^+e^- annihilation experiments are the most clean environment to study fragmentation processes
- evolution of TMD objects
- Global analysis (PRD 78,032011 (2007); PRD 87,094019 (2013), PRD 91,014034 (2015)):
 - combines Semi Inclusive Deep Inelastic Scattering (SIDIS) and e^+e^- data
 - extraction of H_1^\perp and transversity parton distributions h_1 for the “u” and “d” quarks

Collins effect in e^+e^- annihilation

In $e^+e^- \rightarrow q\bar{q}$, spins unknown, but $s_q \parallel s_{\bar{q}}$ whic transverse spin component $\sim \sin^2\theta$

- exploit this correlation by using hadrons in opposite jets
- define **favored** ($u \rightarrow \pi^+$, $d \rightarrow \pi^-$) and **disfavored** ($d \rightarrow \pi^+$, $u \rightarrow \pi^-$, $s(\bar{s}) \rightarrow \pi^\pm$) FFs

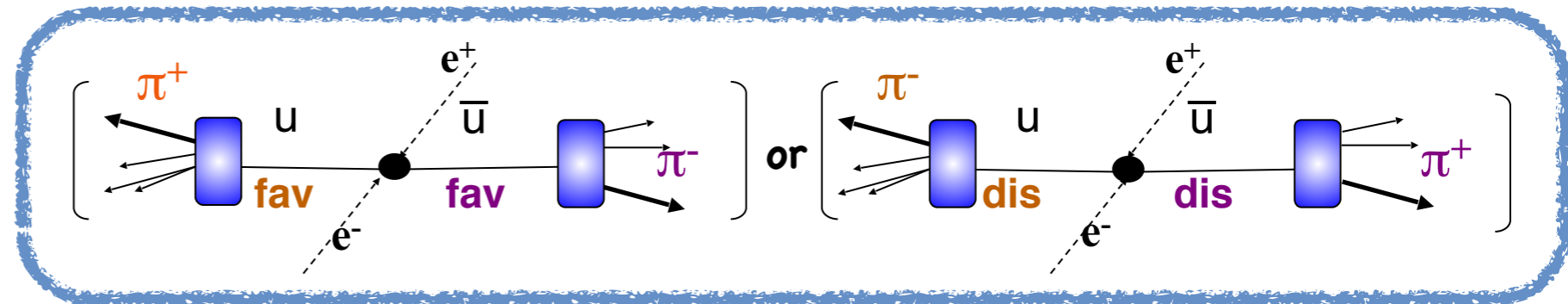
$$e^+e^- \rightarrow q\bar{q} \rightarrow h_1 h_2 X \quad (q=u,d,s) \Rightarrow \sigma \propto \cos(\phi_1 + \phi_2) H_1^\perp(h_1) \times H_1^\perp(h_2)$$



**Azimuthal modulation wrt the quark spin direction:
Collins effect (or Collins asymmetry)**

Example: Unlike $\pi\pi$ pairs (U)

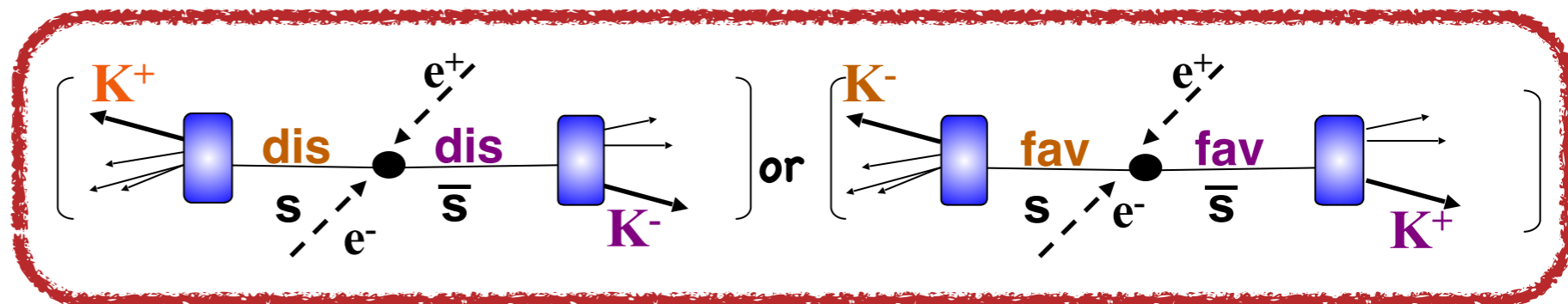
Collins asymmetry for $\pi\pi$



Example: Unlike KK pairs (U)

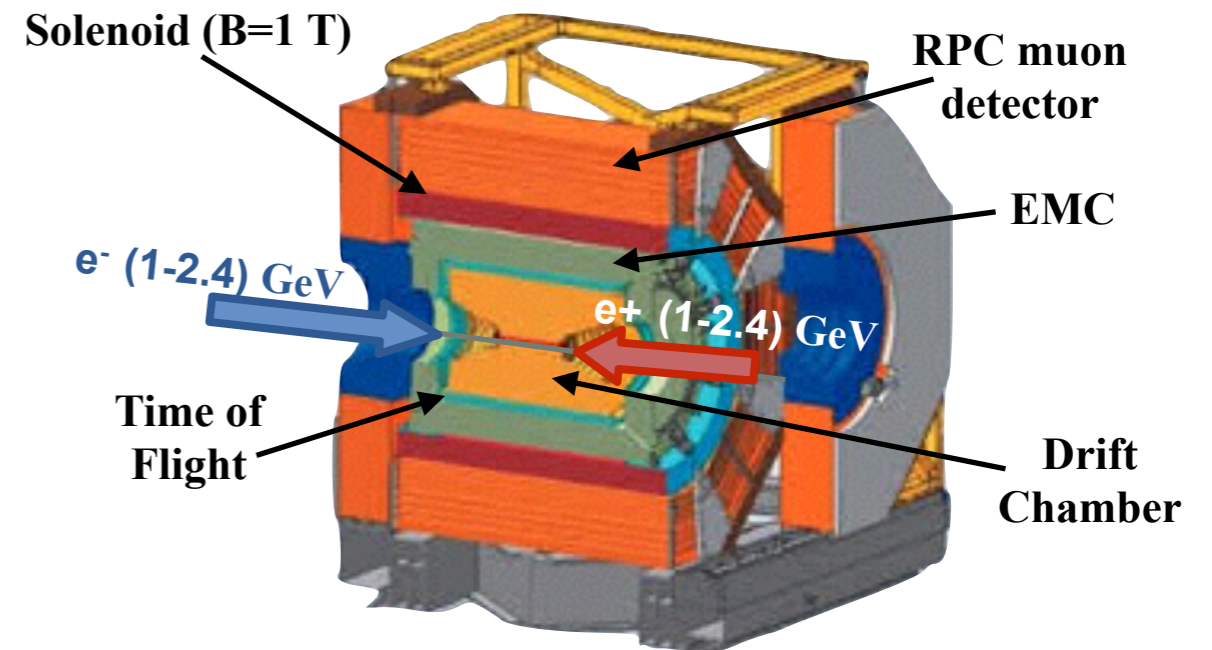
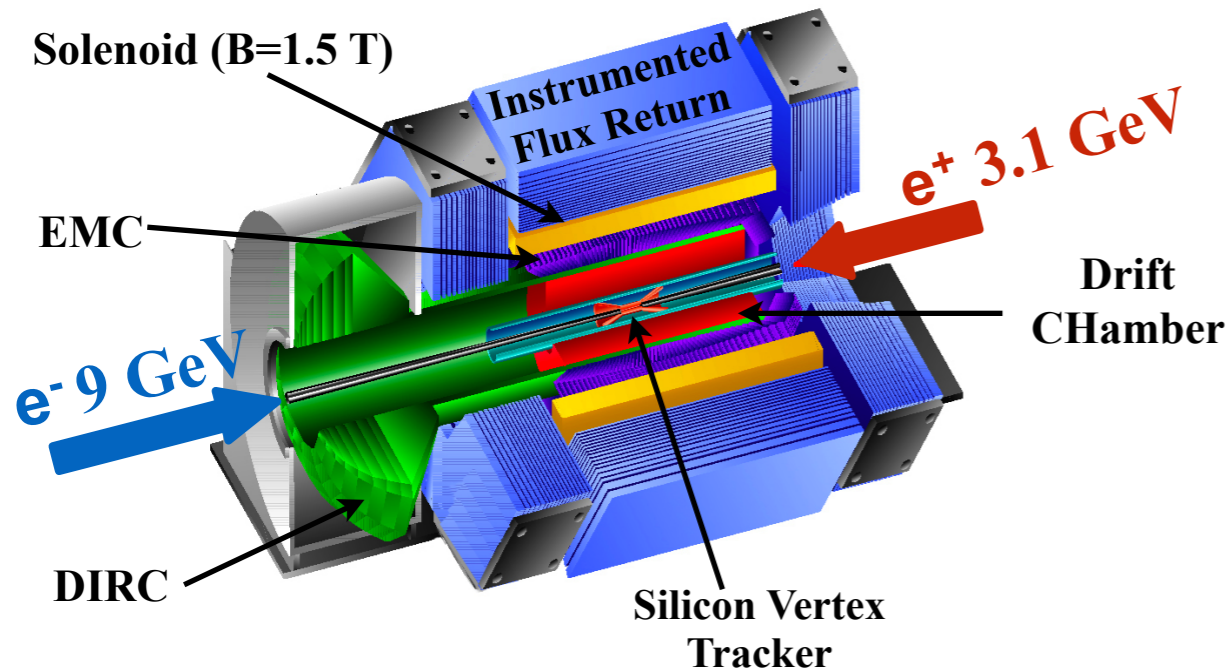
Collins asymmetry for KK :

Favored contribution to the fragmentation of the strange quark



Collins asymmetries for KK pairs not yet available: only BaBar preliminary results

The BaBar and BESIII detectors



- PEP-II storage ring
 - **asymmetric** e^+e^- collider operating at the $\Upsilon(4S)$ resonance ($\sqrt{s}=10.58$ GeV)
 - High Energy Ring (HER): 9.0 GeV e^-
 - Low Energy Ring (LER): 3.1 GeV e^+
 - c.m.-lab boost, $\beta\gamma \approx 0.56$
- High luminosity: $\mathcal{L} \sim 468 \text{ fb}^{-1}$ used here

NIM A479, 1 (2002),
update: NIM A729, 615 (2013)

- Beijing Electron Positron Collider II (BEPCII)
 - **Symmetric** e^+e^- collider
 - Beam energy: 1-2.3 GeV
 - 2008: test run
 - 2009-today: BESIII physics runs
- Luminosity: $\mathcal{L} \sim 62 \text{ pb}^{-1}$ @ 3.65 GeV used here (below open charm threshold)

NIM A614, 345 (2010)

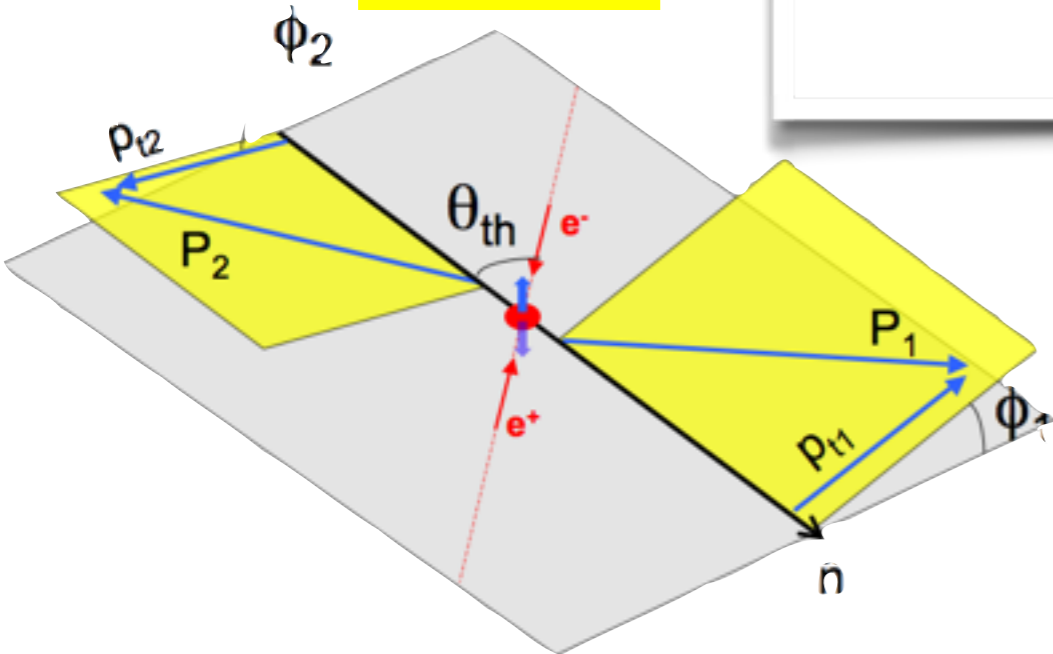
Reference frames

RF12

$$\frac{d\sigma(e^+e^- \rightarrow h_1h_2X)}{d\Omega dz_1 dz_2 d\phi_1 d\phi_2} = \sum_{q,\bar{q}} \frac{3\alpha^2 e_q^2}{Q^2} z_1^2 z_2^2 \left[(1 + \cos^2\theta) D_1^{q,(0)}(z_1) \bar{D}_1^{q,(0)}(z_2) + \sin^2(\theta) \cos(\phi_1 + \phi_2) H_1^{\perp,(1),q}(z_1) \bar{H}_1^{\perp,(1),q}(z_2) \right]$$

All quantities in e^+e^- center of mass

θ : angle between the e^+e^- axis and the thrust axis;
 $\phi_{1,2}$: azimuthal angles between $P_{h1(h2)}$ and the scattering plane

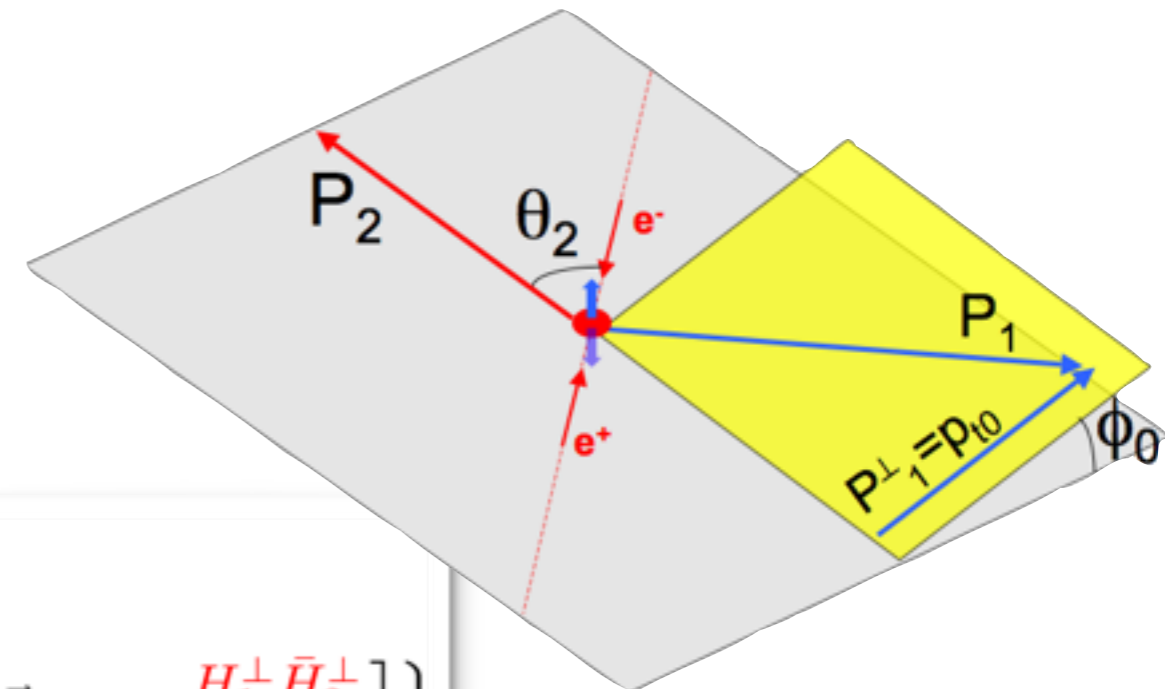


θ_2 : angle between the e^+e^- axis and P_{h2} ;
 ϕ_0 : angle between the plane spanned by P_{h2} and the e^+e^- axis, and the direction of P_{h1} perpendicular to P_{h2} .

All quantities in e^+e^- center of mass

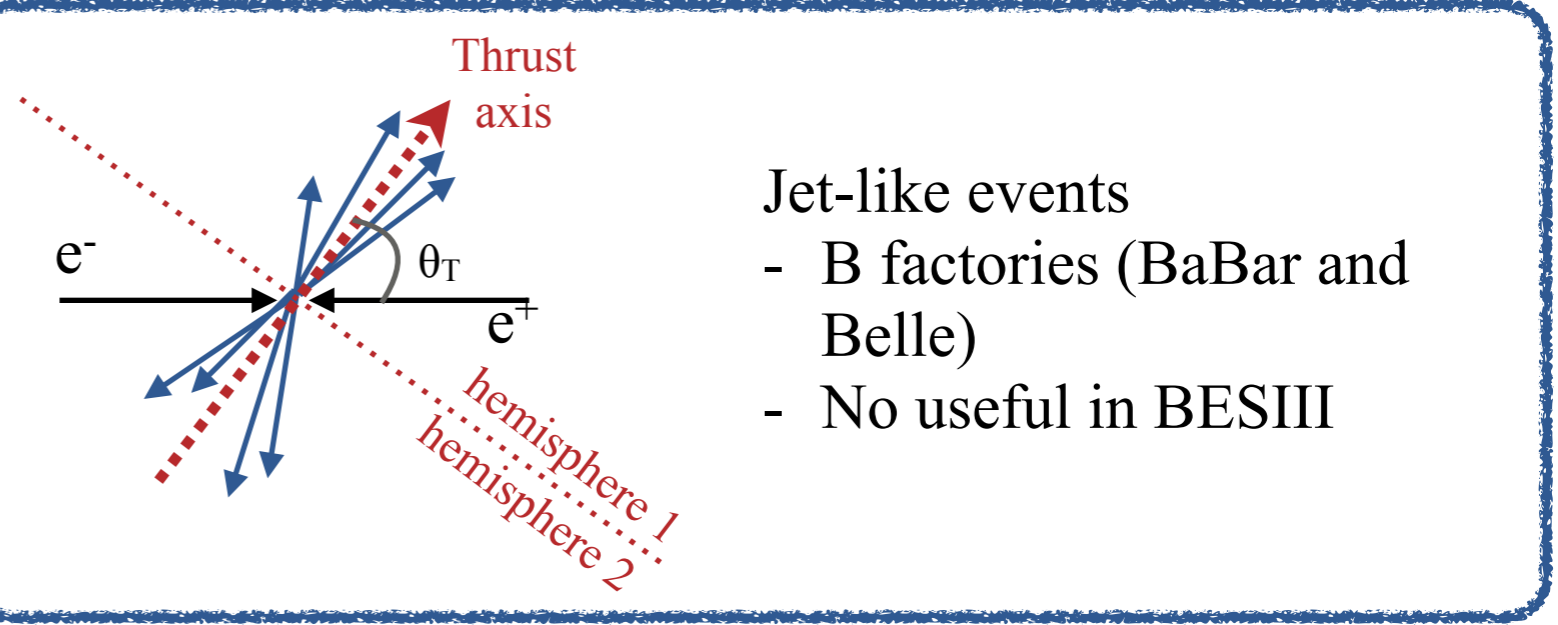
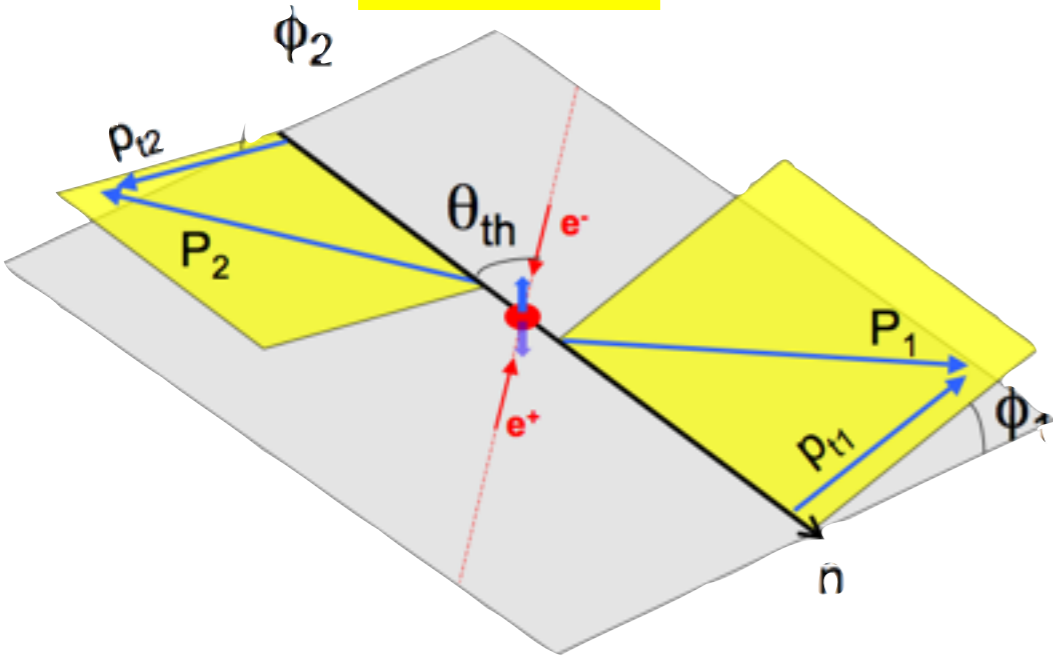
$$\frac{d\sigma(e^+e^- \rightarrow h_1h_2X)}{d\Omega dz_1 dz_2 d^2\vec{q}_T} = \frac{3\alpha^2}{Q^2} z_1^2 z_2^2 \left\{ A(y) \mathcal{F}[D_1 \bar{D}_2] + B(y) \cos(2\phi_0) \mathcal{F} \left[(2\hat{h} \cdot \vec{k}_T \hat{h} \cdot \vec{p}_T - \vec{k}_T \cdot \vec{p}_T) \frac{H_1^\perp \bar{H}_2^\perp}{M_1 M_2} \right] \right\}$$

RF0



Reference frames

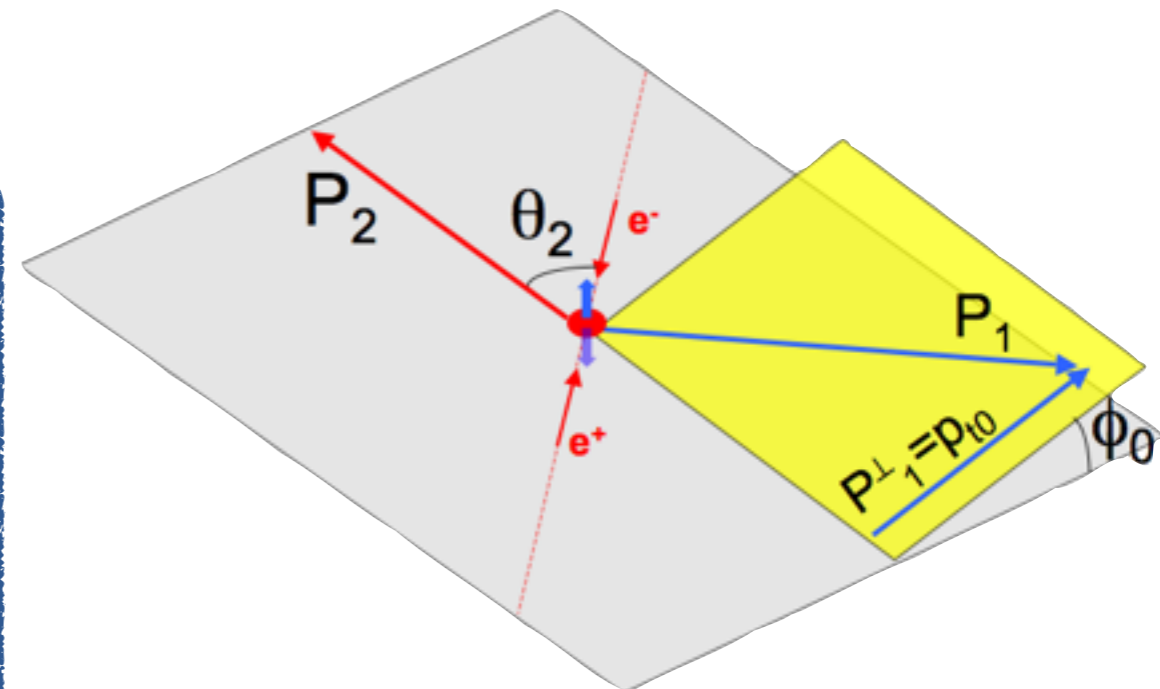
RF12



Jet-like events

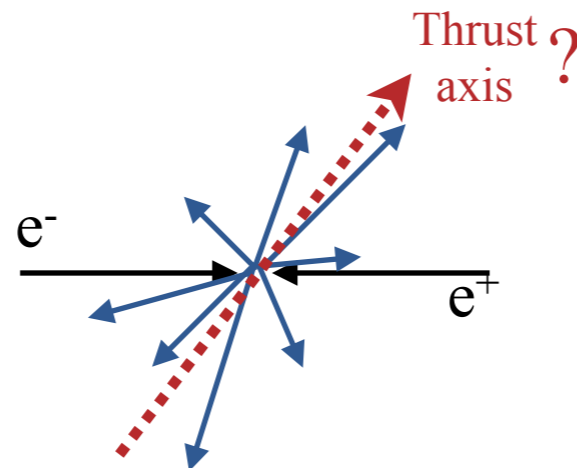
- B factories (BaBar and Belle)
- No useful in BESIII

RF0



The only frame used in BESIII

- low center of mass energy: more spherical events
- Jet-like topology ensured by requiring $\theta_{h1h2} > 120^\circ$



Analysis Strategy

- ❖ Event and track selection
- ❖ Construction of spinless hadron pairs
 - ❖ KK , $K\pi$, $\pi\pi$ for BaBar
 - ❖ $\pi\pi$ for BESIII
- ❖ Measure of the azimuthal angles ϕ_1 and ϕ_2 in RF12 (BaBar), and ϕ_0 in RF0 (BaBar and BESIII)
- ❖ Construction of the normalized raw distributions for like (L), Unlike (U) and Charged (C=U+L) hadron pairs: $R^i=N^i(\phi)/\langle N \rangle$
- ❖ Calculation of the ratios of normalized distributions: U/L and U/C
 - ❖ fit to these distributions with the function $b+a\cdot\cos(x)$
- ❖ Evaluation of background contributions and extraction of the Collins asymmetries

BaBar RESULTS (PRD90,052003):

- ❖ RF12 and RF0
- ❖ A^{UL} and A^{UC}
- ❖ (z_1, z_2) bins, where $z_{1,2}=2E_h/\sqrt{s}$, (p_{t1}, p_{t2}) and p_0 bins, $\sin^2\theta/(1+\cos^2\theta)$, and 2D analysis: (z_1, z_2) vs. (p_{t1}, p_{t2})
- ❖ **NEW PRELIMINARY ([arXiv:1506.05864](#))**
 KK and $K\pi$ asymmetries vs. (z_1, z_2)

BESIII PRELIMINARY RESULTS:

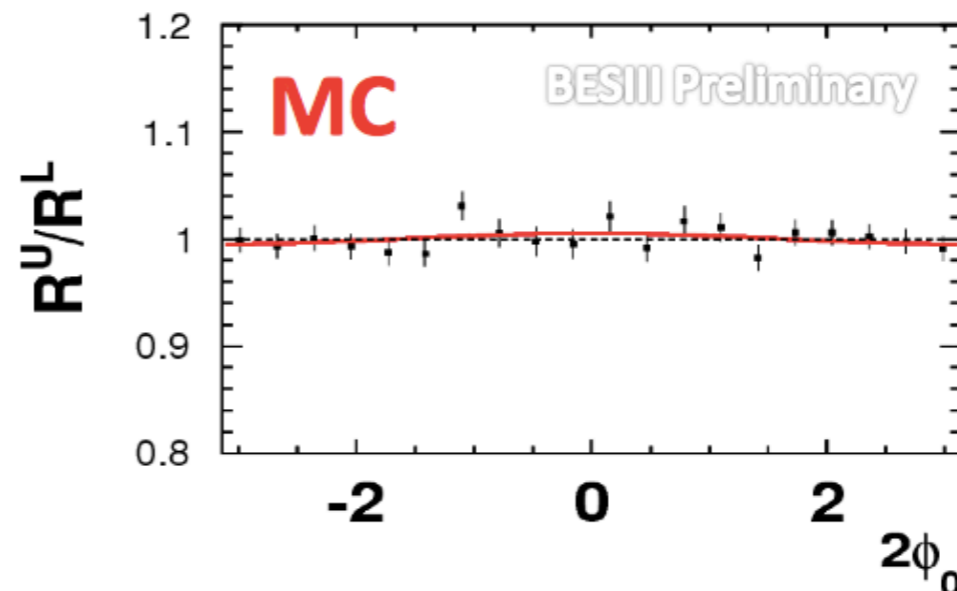
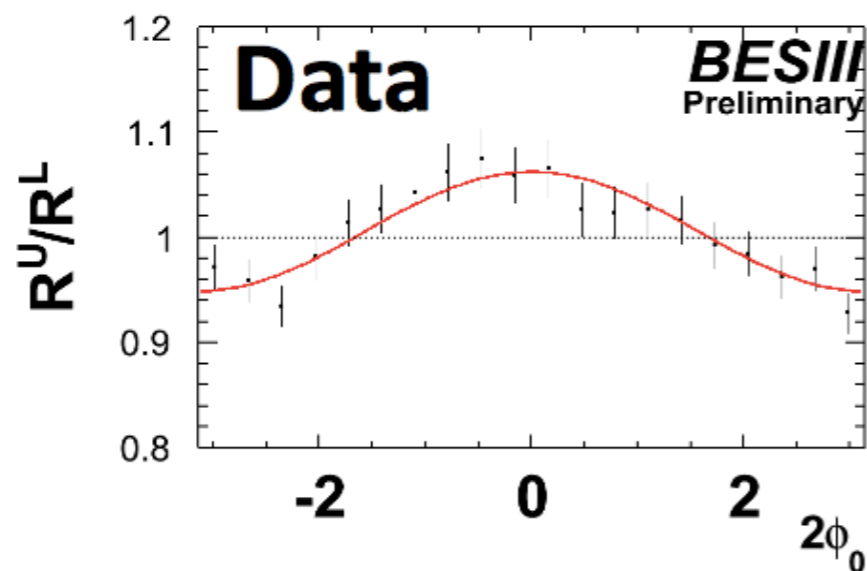
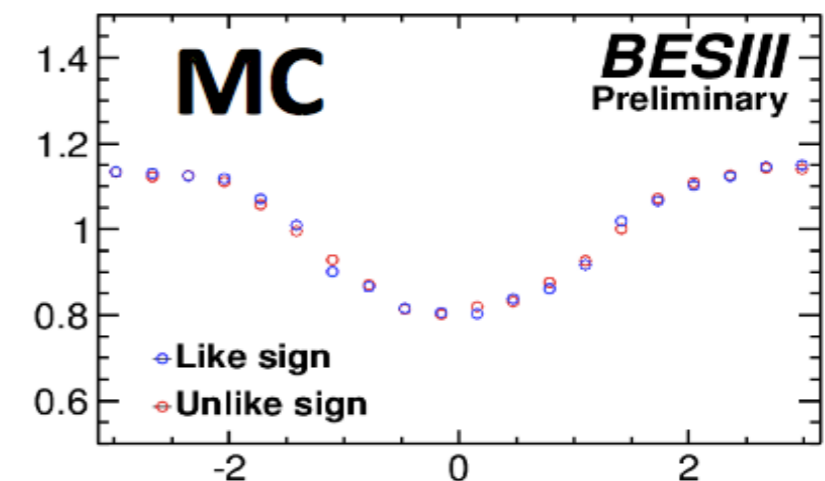
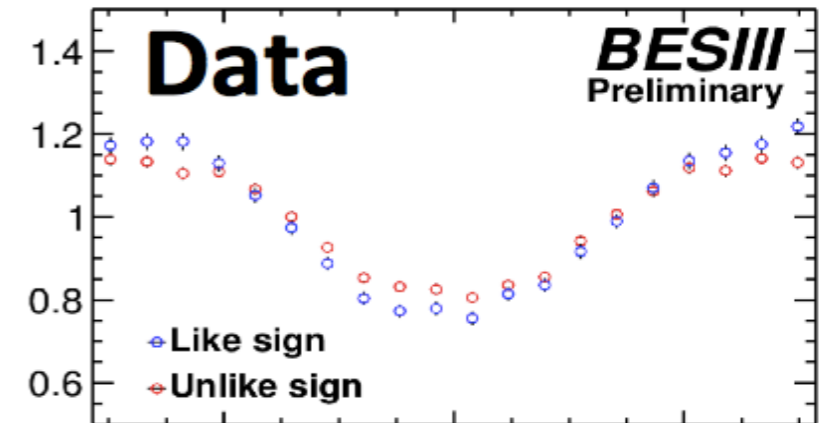
- ❖ [arXiv:1507.06824](#)
- ❖ RF0
- ❖ A^{UL} and A^{UC}
- ❖ (z_1, z_2) bins, where $z_{1,2}=2E_h/\sqrt{s}$, (p_{t1}, p_{t2}) and p_0 bins, $\sin^2\theta/(1+\cos^2\theta)$

Measurement of Collins effect

- Normalized azimuthal distribution for hadron pair with same charge (L), opposite charge (U), and the sum of the two samples (C)
- Collins effect is not simulated in uds-MC \rightarrow strong azimuthal MC modulation principally due to the detector acceptance
- nonzero Collins effect in data sample \rightarrow different combinations of fav and dis FF for L, U, and C

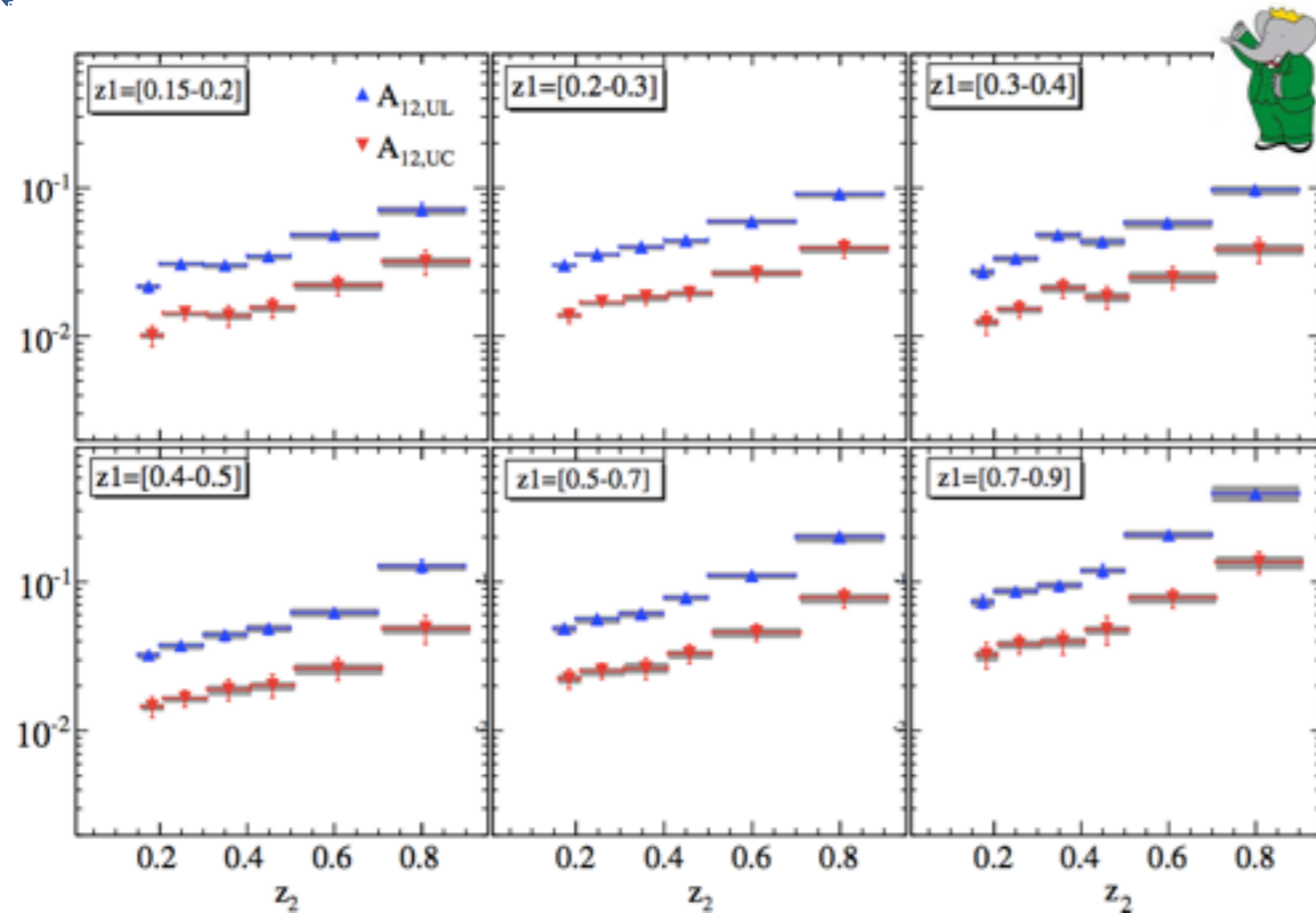
*Double ratio of U/L and U/C normalized distributions:
Collins effect measured by fitting the double ratio
distributions with the function $B+A\cdot\cos(\phi_i)$*

RF0: $\pi\pi$ pairs

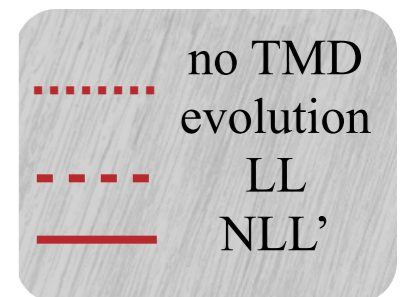
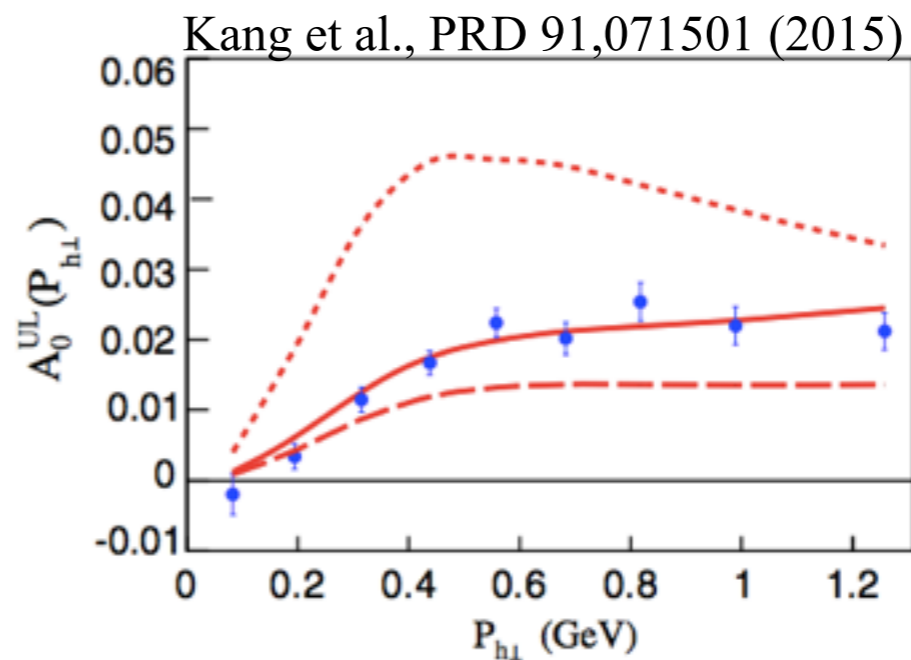
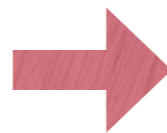
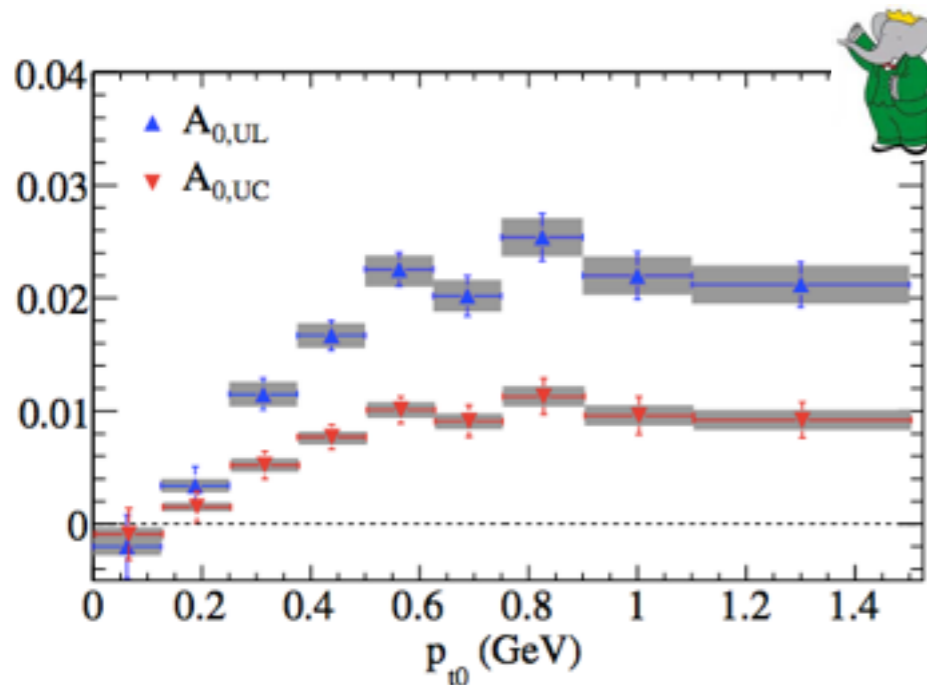


BaBar results for $\pi\pi$ pairs

PRD 90,052003 (2014)



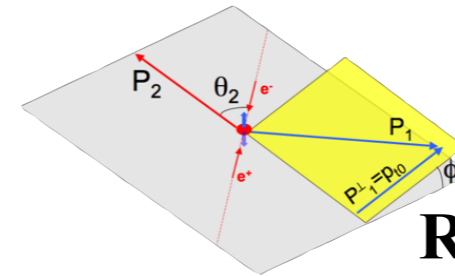
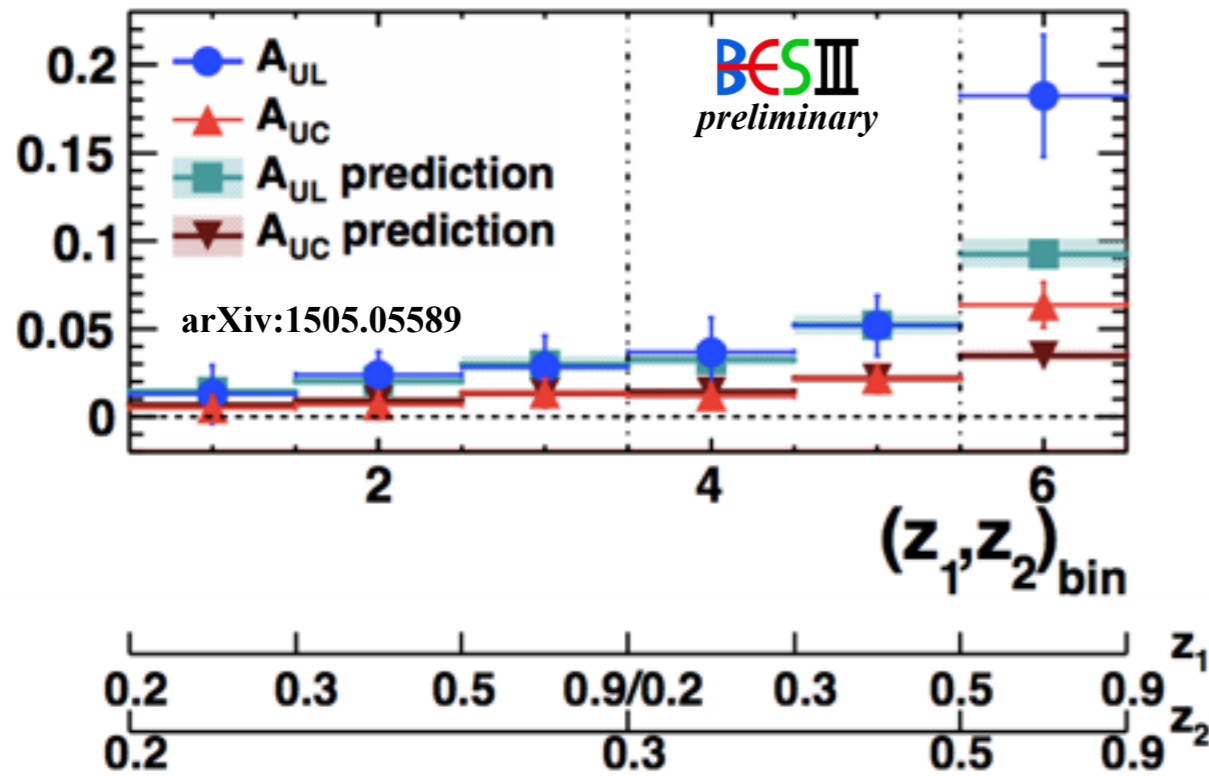
- Collins asymmetry measured as function of
 - 6×6 bins of pion fractional energy (similar behavior in RF0, for both UL and UC)
 - 4×4 bins of (p_{t1}, p_{t2}) in RF12
 - 9 bins of p_{t0} in RF0
 - asymmetry vs. $\sin^2\theta_{th}/(1+\cos^2\theta_{th})$ and $\sin^2\theta_2/(1+\cos^2\theta_2)$



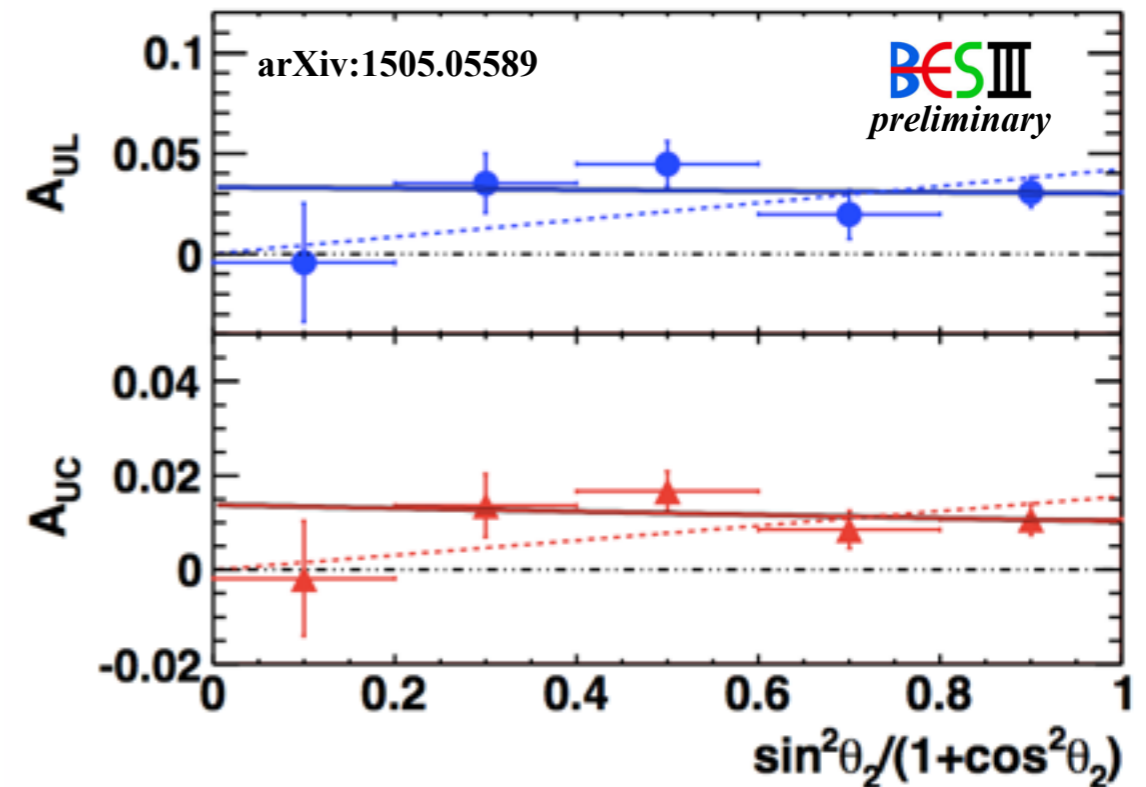
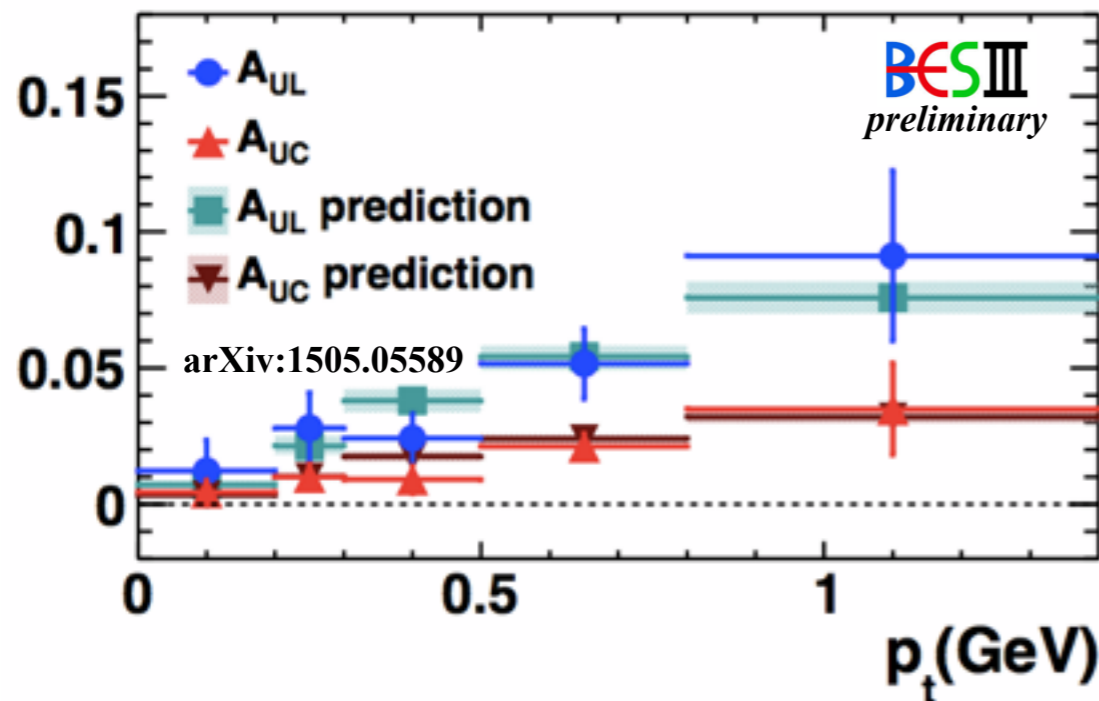
BESIII preliminary results

arXiv:1507.06824

Submitted on PRL



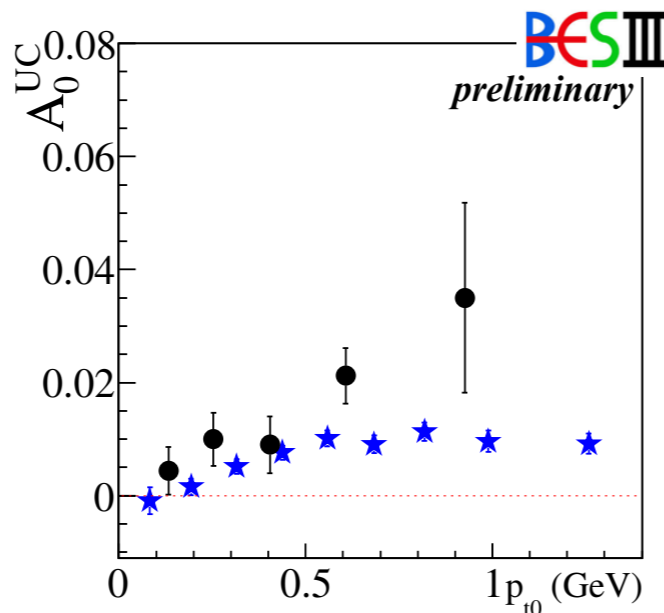
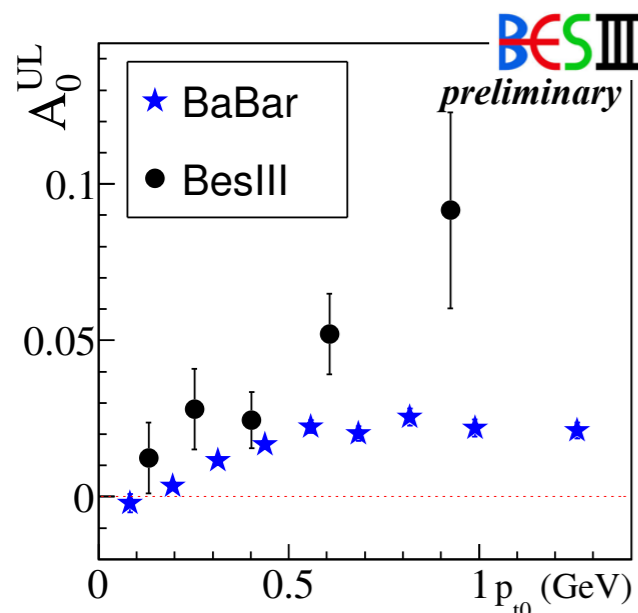
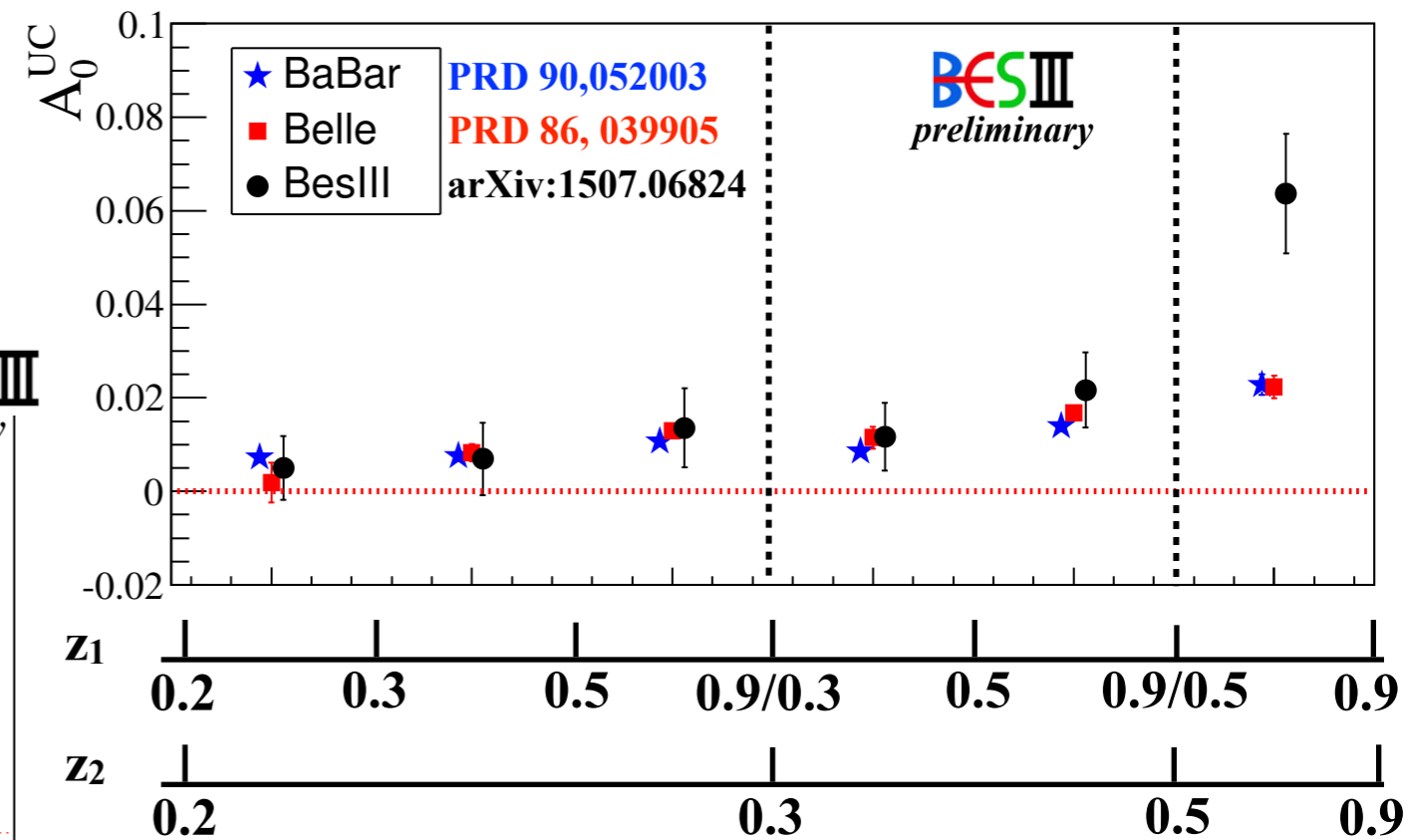
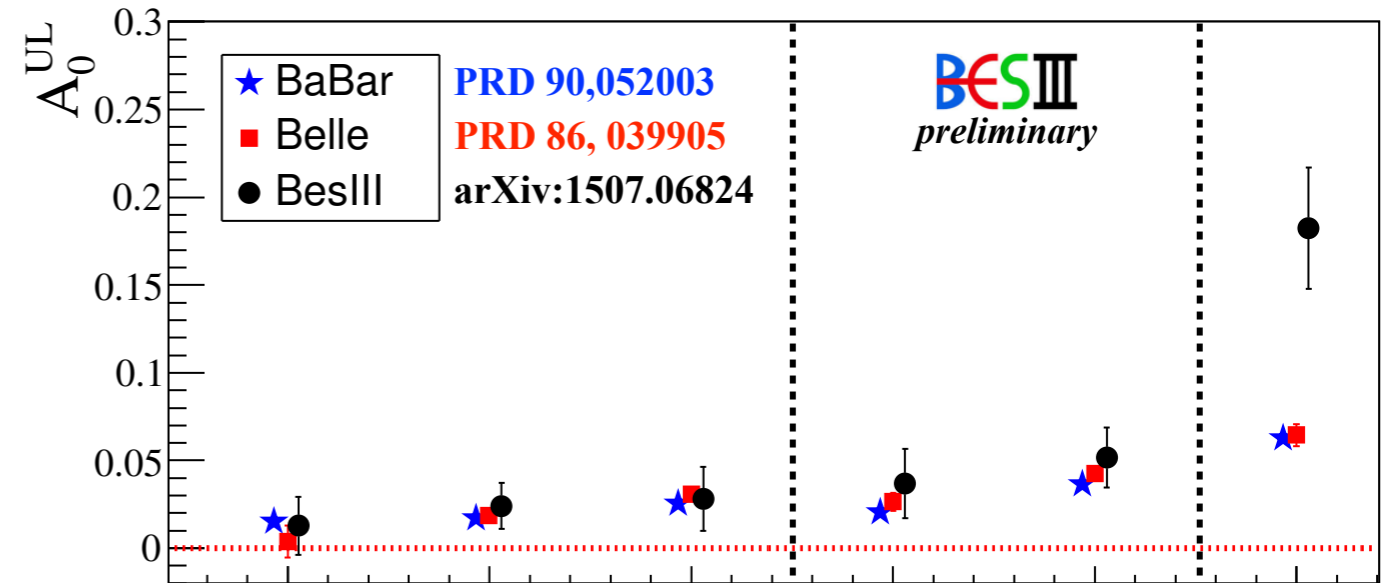
- Collins asymmetry measured as function of
 - 6 symmetric (z_1, z_2) bins
 - 5 bins of p_{t0}
 - asymmetry vs. $\sin^2\theta_2/(1+\cos^2\theta_2)$
 - comparison with prediction reported in arXiv: 1505.05589



Asymmetries comparison in RF0

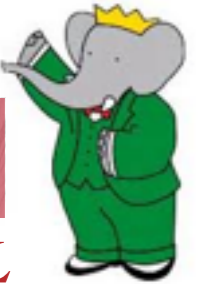
Comparison between different results obtained at different Q^2 :

- **BaBar and Belle @ $Q^2 \sim 110 \text{ GeV}^2$**
- **BESIII @ $Q^2 \sim 13 \text{ GeV}^2$**
- BaBar and Belle results that fall in the larger BESIII z-bins are averaged taking into account the statistical and systematic uncertainties
- Good agreement between different data set for low z
- BESIII larger asymmetries in the last z-bins: consistent with the prediction reported in *arXiv:1505.05589*



arXiv:1506.05864

Submitted on PRL



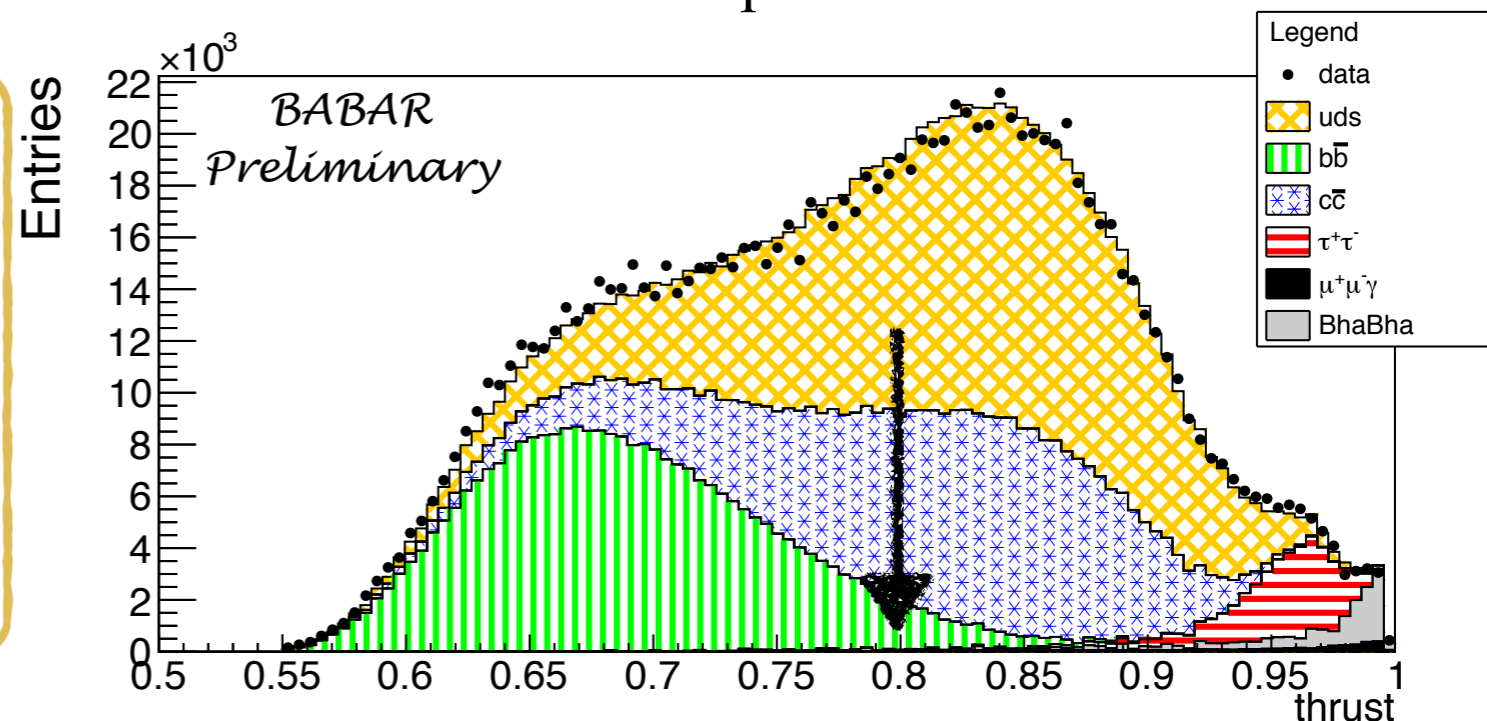
New BaBar Preliminary Result: Collins asymmetries for KK and $K\pi$ hadron pairs

Event and track selection

More stringent cuts optimized in order to reduce biases on the KK pairs

EVENT SELECTION

- Number of charged tracks > 2
- Selection of two jets topology: thrust > 0.8
- $|\cos\theta_{\text{thrust}}| < 0.6$
- Visible energy $E_{\text{vis}} > 11 \text{ GeV}$
- Most energetic photon $E_{\gamma} < 2 \text{ GeV}$



Thrust axis: charged tracks + neutral candidates; thrust axis direction chosen random

TRACK SELECTION

- Electrons and muons veto
- K and π in the DIRC acceptance region
- K/ π fractional energy z : $0.15 < z < 0.9$
- Opening angle $\theta_{h\text{-thrust}}$ of hadron with respect to the thrust axis $< 45^\circ$
- $Q_t < 3.5 \text{ GeV}$, where Q_t is the transverse momentum of the virtual photon in the two hadrons center-of-mass energy

Extraction of KK , $K\pi$ and $\pi\pi$ asymmetries

GOAL: simultaneous extraction of the asymmetries corrected for backgrounds and K/π misidentification for each interval of fractional energy

- 3 samples: KK , $K\pi$, $\pi\pi$
- we fit independently the double ratio distributions of the three samples

$$A_{KK}^{meas} = F_{uds}^{KK} \cdot (\xi_{KK}^{(KK)} A_{KK} + \xi_{K\pi}^{(KK)} A_{K\pi} + \xi_{\pi\pi}^{(KK)} A_{\pi\pi}) + F_{c\bar{c}}^{KK} \cdot (\xi_{KK}^{(KK)c\bar{c}} A_{KK}^{ch} + \xi_{K\pi}^{(KK)c\bar{c}} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(KK)c\bar{c}} A_{\pi\pi}^{ch})$$

$$A_{KK}^{D^*} = f_{uds}^{KK} \cdot (\xi_{KK}^{(KK)D^*} A_{KK} + \xi_{K\pi}^{(KK)D^*} A_{K\pi} + \xi_{\pi\pi}^{(KK)D^*} A_{\pi\pi}) + f_{c\bar{c}}^{KK} \cdot (\xi_{KK}^{(KK)c\bar{c}-D^*} A_{KK}^{ch} + \xi_{K\pi}^{(KK)c\bar{c}-D^*} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(KK)c\bar{c}-D^*} A_{\pi\pi}^{ch})$$

1. Background sources:

- mainly from $e^+e^- \rightarrow c\bar{c}$ events (more than 30%); smaller contribution from $B\bar{B}$, $\tau^+\tau^-$ ($A_{bb} \sim A_{\tau} \sim 0$)
 - we construct a D^* -enhanced MC and data control samples
 - we calculate from MC the fraction ($F(f)_{sig/bkg}^{hh}$) of hadron pairs coming from signal (uds) and background events ($c\bar{c}$, $B\bar{B}$, $\tau^+\tau^-$)

2. K/π misidentification:

- we evaluate from MC the fraction ($\xi_{hh}^{(hh)}$) that a given hadron pair is reconstructed as KK , $K\pi$, or $\pi\pi$ pair
- fractions evaluated in all samples used in the analysis: uds ($\xi_{hh}^{(hh)}$), D^* -uds ($\xi_{hh}^{(hh)D^*}$), $c\bar{c}$ ($\xi_{hh}^{(hh)c\bar{c}}$), $c\bar{c}-D^*$ ($\xi_{hh}^{(hh)c\bar{c}-D^*}$)

Simultaneous extraction of asymmetry

Three samples (KK, K π , $\pi\pi$) + background + K/ π misidentification \Rightarrow **system of six equations and six unknown parameters**

$$A_{KK}^{meas} = F_{uds}^{KK} \cdot (\xi_{KK}^{(KK)} A_{KK} + \xi_{K\pi}^{(KK)} A_{K\pi} + \xi_{\pi\pi}^{(KK)} A_{\pi\pi}) + F_{c\bar{c}}^{KK} \cdot (\xi_{KK}^{(KK)c\bar{c}} A_{KK}^{ch} + \xi_{K\pi}^{(KK)c\bar{c}} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(KK)c\bar{c}} A_{\pi\pi}^{ch})$$


$$A_{K\pi}^{meas} = F_{uds}^{K\pi} \cdot (\xi_{KK}^{(K\pi)} A_{KK} + \xi_{K\pi}^{(K\pi)} A_{K\pi} + \xi_{\pi\pi}^{(K\pi)} A_{\pi\pi}) + F_{c\bar{c}}^{K\pi} \cdot (\xi_{KK}^{(K\pi)c\bar{c}} A_{KK}^{ch} + \xi_{K\pi}^{(K\pi)c\bar{c}} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(K\pi)c\bar{c}} A_{\pi\pi}^{ch})$$

$$A_{\pi\pi}^{meas} = F_{uds}^{\pi\pi} \cdot (\xi_{KK}^{(\pi\pi)} A_{KK} + \xi_{K\pi}^{(\pi\pi)} A_{K\pi} + \xi_{\pi\pi}^{(\pi\pi)} A_{\pi\pi}) + F_{c\bar{c}}^{\pi\pi} \cdot (\xi_{KK}^{(\pi\pi)c\bar{c}} A_{KK}^{ch} + \xi_{K\pi}^{(\pi\pi)c\bar{c}} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(\pi\pi)c\bar{c}} A_{\pi\pi}^{ch})$$

$$A_{KK}^{D^*} = f_{uds}^{KK} \cdot (\xi_{KK}^{(KK)D^*} A_{KK} + \xi_{K\pi}^{(KK)D^*} A_{K\pi} + \xi_{\pi\pi}^{(KK)D^*} A_{\pi\pi}) + f_{c\bar{c}}^{KK} \cdot (\xi_{KK}^{(KK)c\bar{c}-D^*} A_{KK}^{ch} + \xi_{K\pi}^{(KK)c\bar{c}-D^*} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(KK)c\bar{c}-D^*} A_{\pi\pi}^{ch})$$

$$A_{K\pi}^{D^*} = f_{uds}^{K\pi} \cdot (\xi_{KK}^{(K\pi)D^*} A_{KK} + \xi_{K\pi}^{(K\pi)D^*} A_{K\pi} + \xi_{\pi\pi}^{(K\pi)D^*} A_{\pi\pi}) + f_{c\bar{c}}^{K\pi} \cdot (\xi_{KK}^{(K\pi)c\bar{c}-D^*} A_{KK}^{ch} + \xi_{K\pi}^{(K\pi)c\bar{c}-D^*} A_{K\pi}^{ch} + \chi_{\pi\pi}^{(K\pi)c\bar{c}-D^*} A_{\pi\pi}^{ch})$$

$$A_{\pi\pi}^{D^*} = f_{uds}^{\pi\pi} \cdot (\xi_{KK}^{(\pi\pi)D^*} A_{KK} + \xi_{K\pi}^{(\pi\pi)D^*} A_{K\pi} + \xi_{\pi\pi}^{(\pi\pi)D^*} A_{\pi\pi}) + f_{c\bar{c}}^{\pi\pi} \cdot (\xi_{KK}^{(\pi\pi)c\bar{c}-D^*} A_{KK}^{ch} + \xi_{K\pi}^{(\pi\pi)c\bar{c}-D^*} A_{K\pi}^{ch} + \xi_{\pi\pi}^{(\pi\pi)c\bar{c}-D^*} A_{\pi\pi}^{ch})$$

 = Collins asymmetries for light hadrons

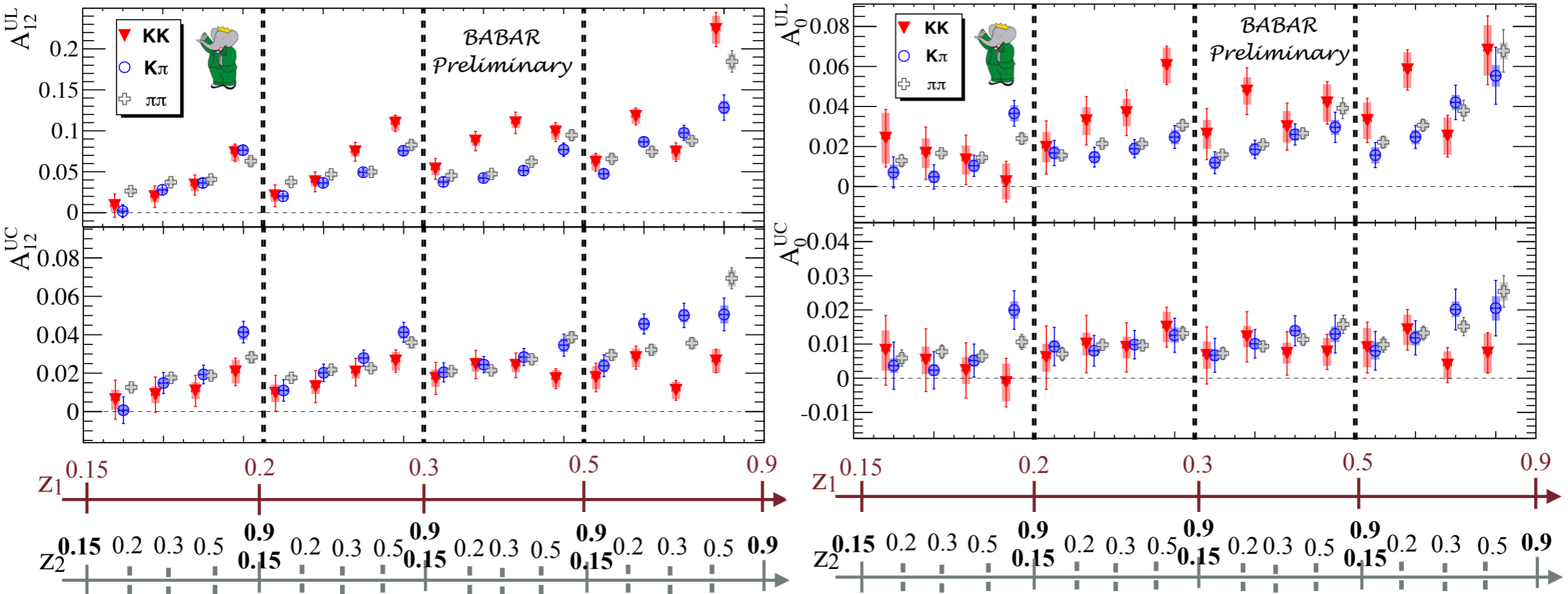
Results: RF12

Simultaneous measurement of KK , $K\pi$ and $\pi\pi$ Collins asymmetries

- all corrections are applied

arXiv:1506.05864

Submitted on PRL

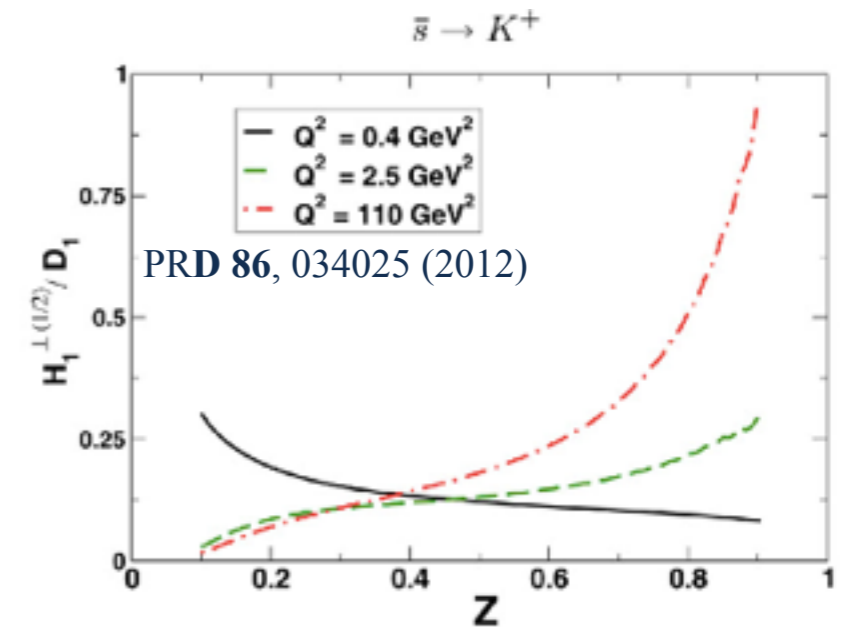
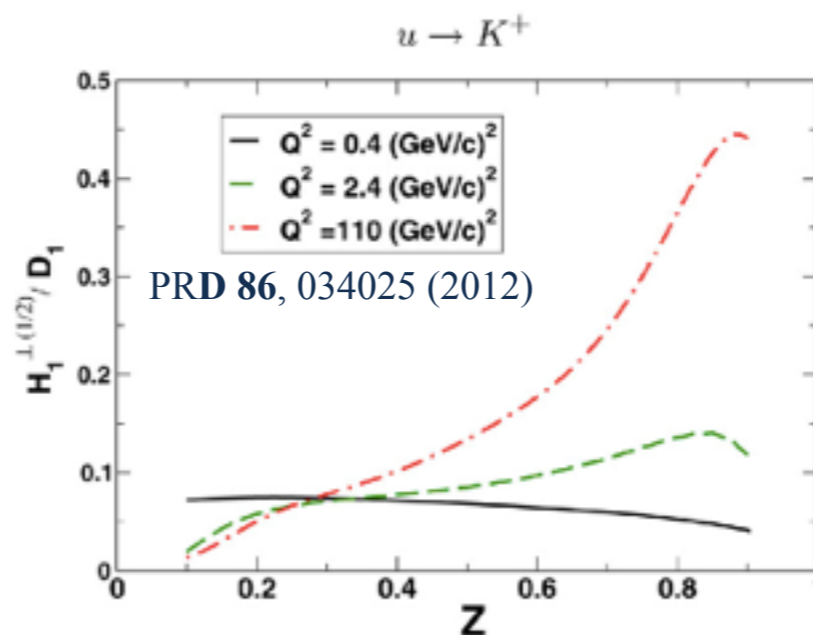
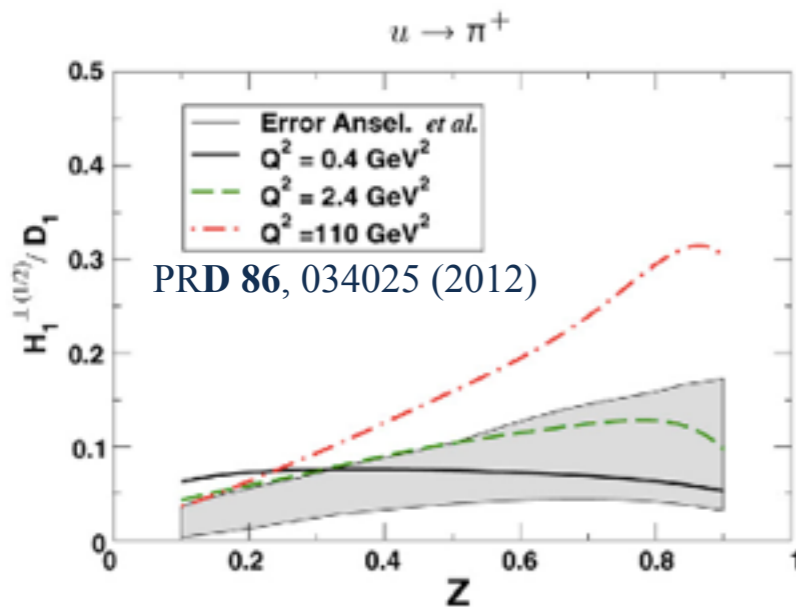


- ⊠ Rising of the asymmetry as a function of z (more pronounced for U/L)
- ⊠ A^{UL} KK asymmetry slightly higher than pion asymmetry for high z
- ⊠ KK asymmetry consistent with zero at lower z

Note that A^{UL} and A^{UC} asymmetries are obtained using the same data sample, and are strongly correlated

Conclusions

- Collins asymmetries for $\pi\pi$ pairs was deeply investigated:
 - BaBar and Belle @ $Q^2 \sim 110 \text{ GeV}^2$ (PRD90,052003, PRD86,039905)
 - **BESIII preliminary results @ $Q^2 \sim 13 \text{ GeV}^2$ allow to study the evolution of TMD objects**
 - Collins effect studied as a function of several kinematic variables
- BaBar preliminary results: simultaneous extraction of A_{KK} , $A_{K\pi}$, and $A_{\pi\pi}$ Collins asymmetries
 - 16 (z_1, z_2) -bins
 - Good agreement with previous BaBar results (PRD 90,052003 (2014))



- Agreement with theoretical prediction !? [*PL B659*, 234 (2008); *PRD 86*, 034025 (2012)]
 - A^{UL} asymmetry for KK are slightly **larger** than $\pi\pi$
 - A^{UC} asymmetry for KK are slightly **lower** than $\pi\pi$

Backup slides