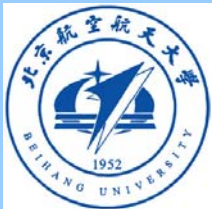


# Charmonium and light hadron spectroscopy

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**Beihang University**

**PIC 2013 : 4-7 September, 2013, IHEP**



# Outline



- ❖ Charmonium states:

$\Psi(4040)$  ,  $\Psi(4160)$  ,  $\eta_c$ ,  $\eta_c(2S)$ ,  $\Psi_2$ ,  
 $X(3872)$

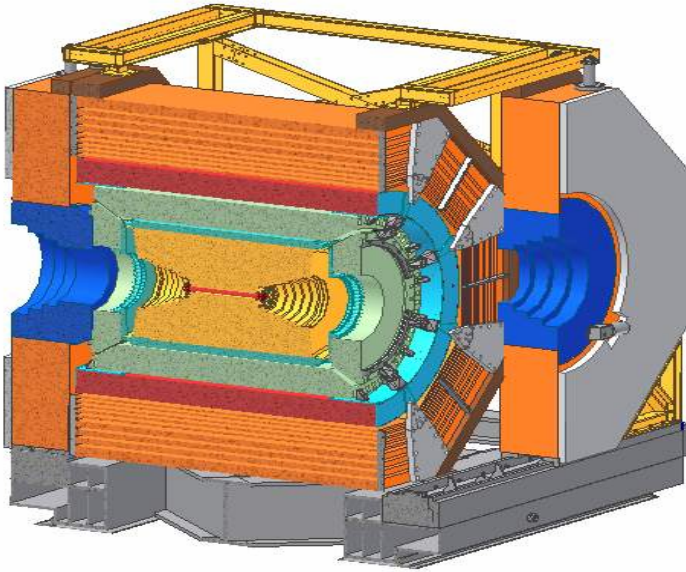
- ❖ light hadron spectroscopy

$X(1835)$ ,  $\eta\eta$ ,  $\omega\omega$ ,  $\phi\phi$ ,  $\omega\phi$

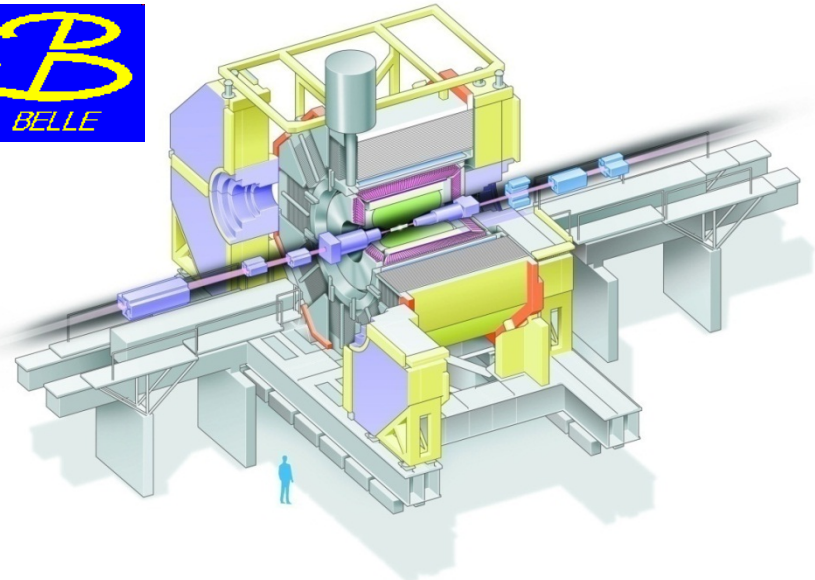
- ❖ Summary & Outlook

# Results are from these experiments

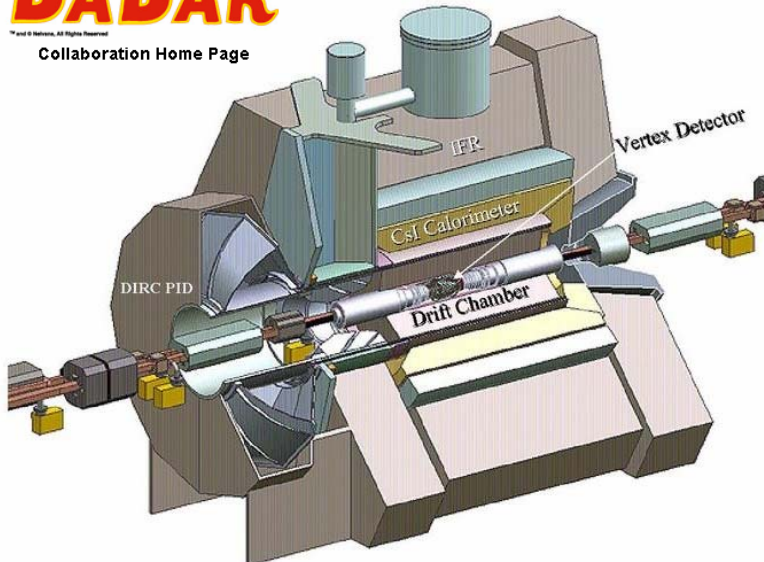
BES  $\tau$



BELLE



 **BABAR**  
Collaboration Home Page



Most of the results are from BESIII and Belle. Due to limited time, I can only cover a few topics. For more results, please refer to Belle and BESIII publication pages:

<http://bes3.ihep.ac.cn/pub/physics.htm>

[http://belle.kek.jp/bdocs/b\\_journal.html](http://belle.kek.jp/bdocs/b_journal.html)

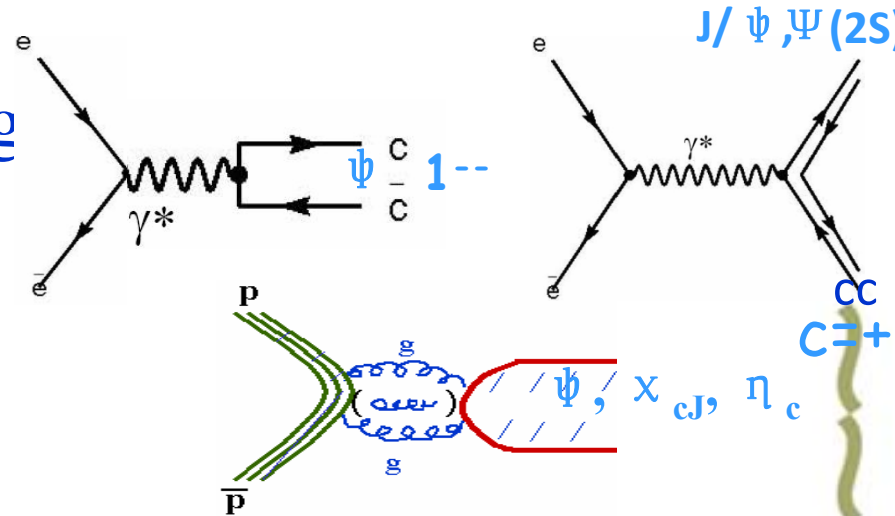
# Charmonium

- ❖ Charmed-quark( $c$ ) anticharmed-quark( $\bar{c}$ ) bound states.
- ❖ Has been a power tool for the understanding of the strong interaction
  - ⌘ QCD is well tested at high energies
  - ⌘ In low-energy regime, many aspects are not understood
  - ⌘ Test QCD and improve out limited understanding of QCD

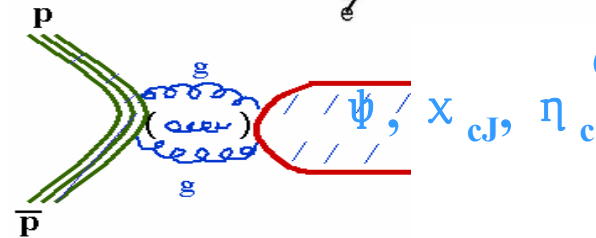
**For Exotic hadrons and Quarkonium, please wait for Choi's report – next one !**

# Production

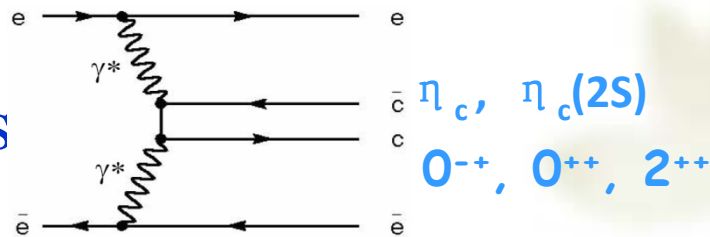
1.  $e^+e^-$  annihilation (including ISR/double charmonium)



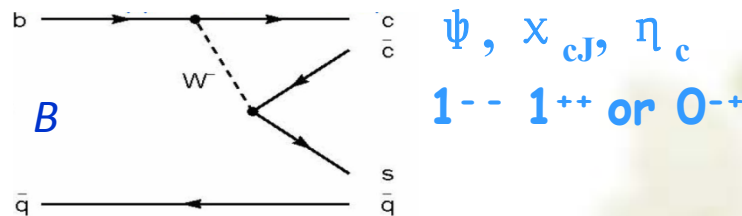
2.  $p\bar{p}$  annihilation



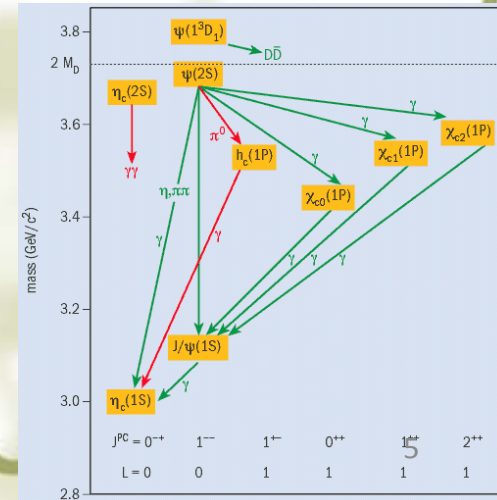
3. Two-photon process



4. B decays



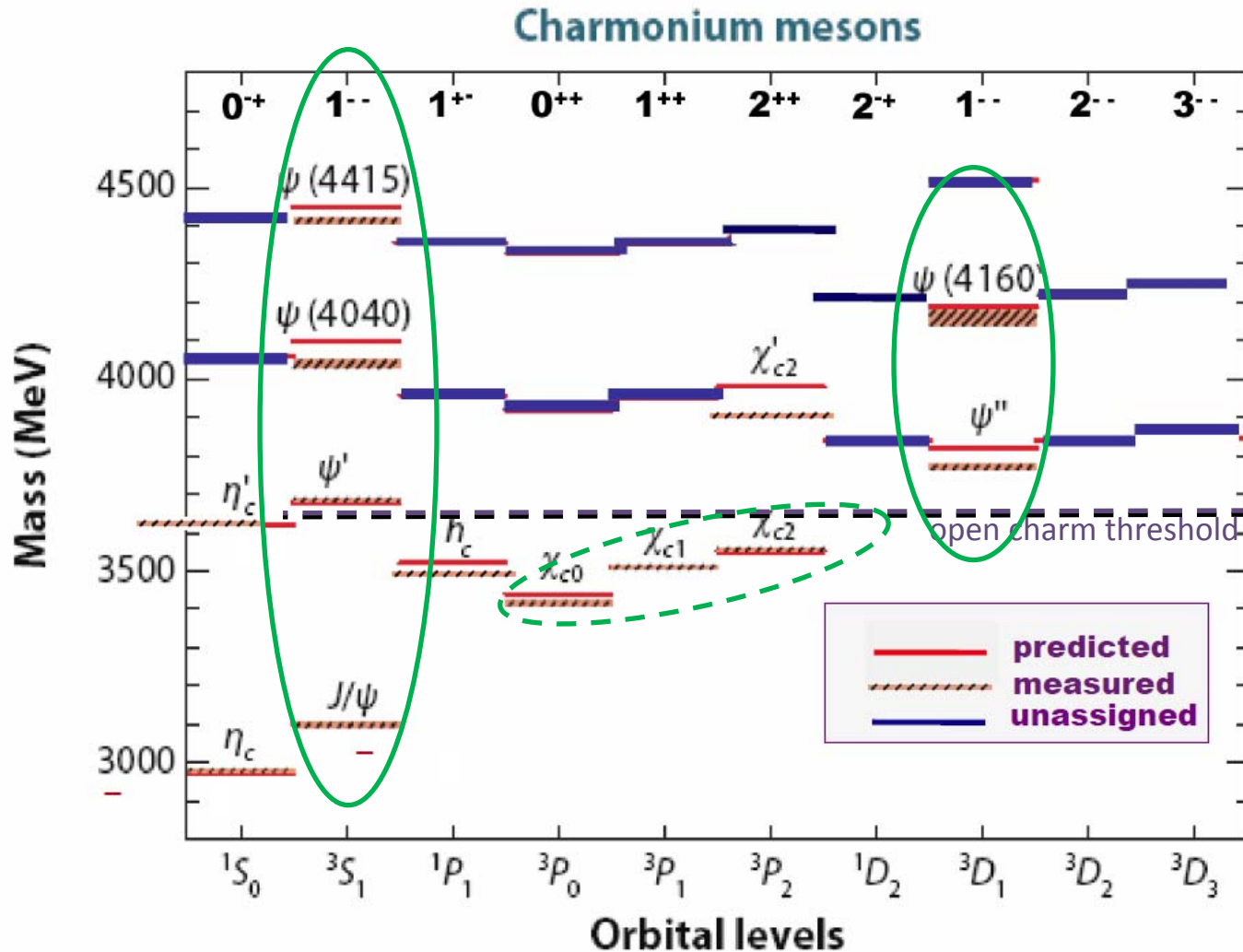
5. Through charmonium transition





# 1<sup>-</sup> states: $J/\psi$ , $\psi'$ , $\psi''$ , $\psi(4040)$ , $\psi(4160)$ , $\psi(4415)$

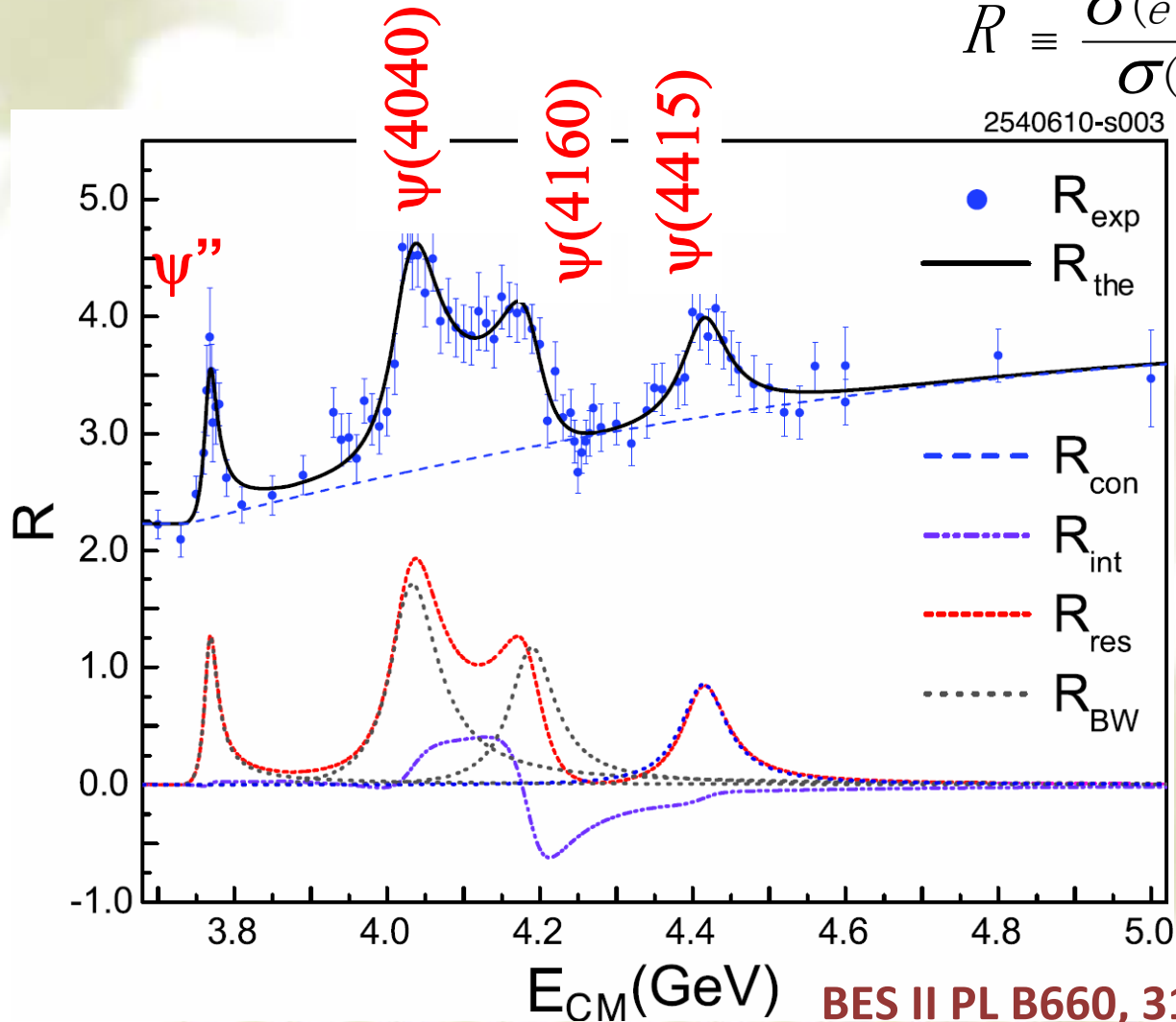
- Abundantly produced from  $e^+e^-$ , pp collisions
- Observed in 70's



# $J^{PC} = 1^{--}$ states produce peaks in $R_{had}$

Extraction of resonance parameters from  $R$  measurement

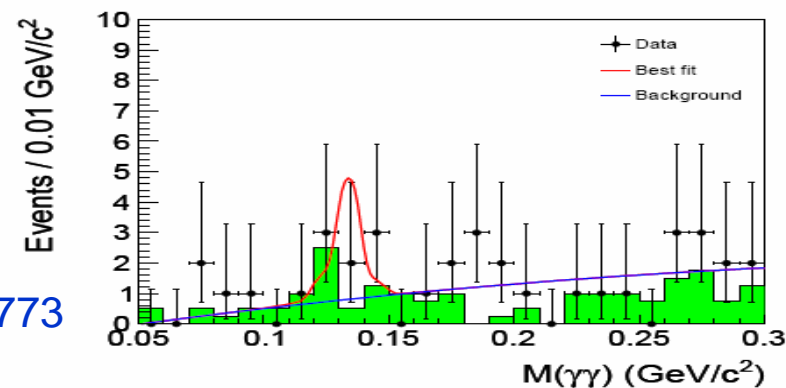
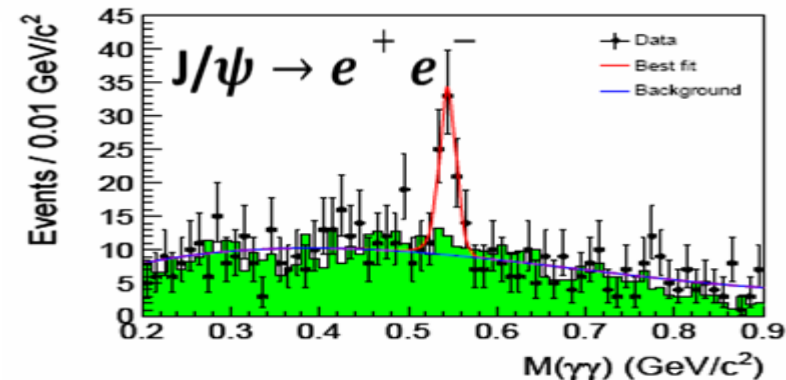
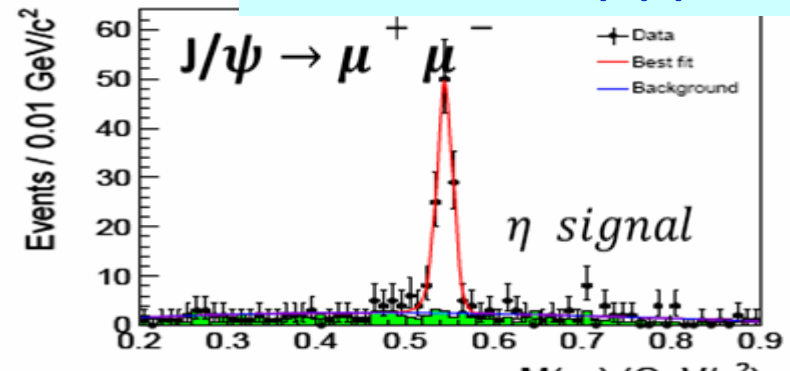
$$R \equiv \frac{\sigma(e^+e^- \rightarrow hadrons)}{\sigma(e^+e^- \rightarrow \mu^+\mu^-)}$$



# $e^+e^- \rightarrow \eta J/\psi @ 4.01 \text{ GeV}$

PRD86, 071101(R) (2012)

- ❖ Hadronic transition between charmonium states above open-charm threshold is not well understood
- ❖ Data sample:  $478 \text{ pb}^{-1} @ 4.01 \text{ GeV}$
- ❖ **First observation:**  $e^+e^- \rightarrow \eta J/\psi$  (significance  $> 10\sigma$ )
- ❖ Measured Born cross section:  $(32.1 \pm 2.8 \pm 1.3) \text{ pb}$
- ❖ Assume  $\eta J/\psi$  from  $\psi(4040)$   
 $\text{Br}(\psi(4040) \rightarrow \eta J/\psi) = (5.2 \pm 0.5 \pm 0.2 \pm 0.5) \times 10^{-3}$   
 $\text{Br}(\psi(4040) \rightarrow \pi^0 J/\psi) < 2.8 \times 10^{-4} @ 90\% \text{ CL}$
- ❖ Consistent with the theoretical calculation (Q.Wang et al., arXiv:1206.4511)
- ❖ Partial width of  $\psi(4040) \rightarrow \eta J/\psi$ :  $\sim 400 \text{ keV}$  ( $>$  two times  $\psi(4040) \rightarrow \pi\pi J/\psi$ )
  - ↪ Similar to the hadronic transition of  $Y(4S)$  (admixture of a four-quark state in the wave function, M. B. Voloshin, Mod. Phys. Lett. A 26, 773 (2011))





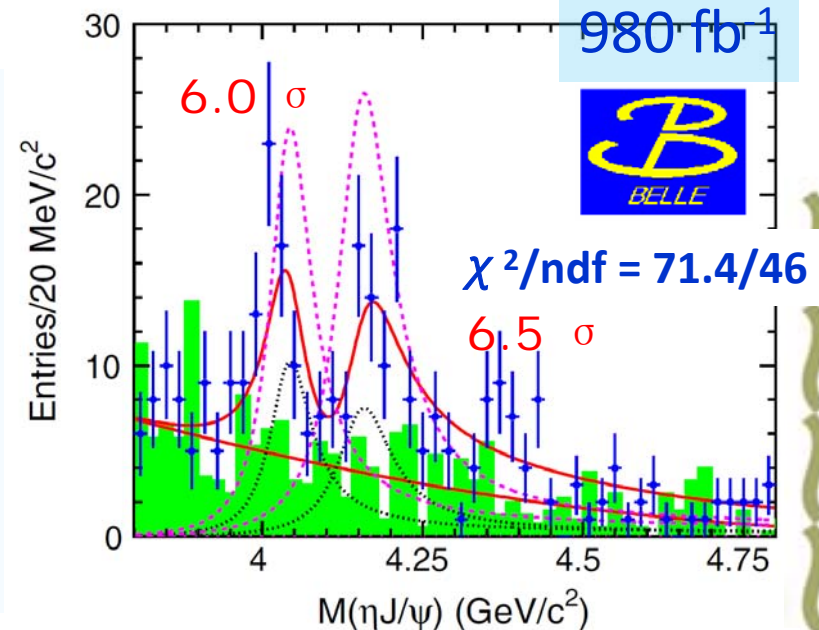
# $\psi(4040)$ and $\psi(4160)$ decay into $\eta$ $J/\psi$

PRD 87, 051101(R) (2013)

❖ **BESIII can not measure the line shape of  $\eta$   $J/\psi$ . Belle did it via ISR.**

- $\eta \rightarrow \gamma\gamma$  and  $\pi^+ \pi^- \pi^0$
- $J/\psi \rightarrow e^+e^-$  mode is not used in  $\eta \rightarrow \gamma\gamma$  (high Bhabha bkg.)
- $\Psi(2S)$  signal is a tagged signal
- $\sigma(e^+e^- \rightarrow \Psi(2S)) = 13.9 \pm 1.4$  (stat) pb and  $14.0 \pm 0.8$  (stat) for  $\eta \rightarrow \pi^+ \pi^- \pi^0$  and  $\gamma\gamma$ , in good agreement with the theoretical value of 14.7 pb.

- **An unbinned maximum likelihood fit to the signal events and  $\eta$  and  $J/\psi$  sidebands simultaneously**
- **Two coherent P-wave BWs for  $\Psi(4040)$  and  $\Psi(4160)$**

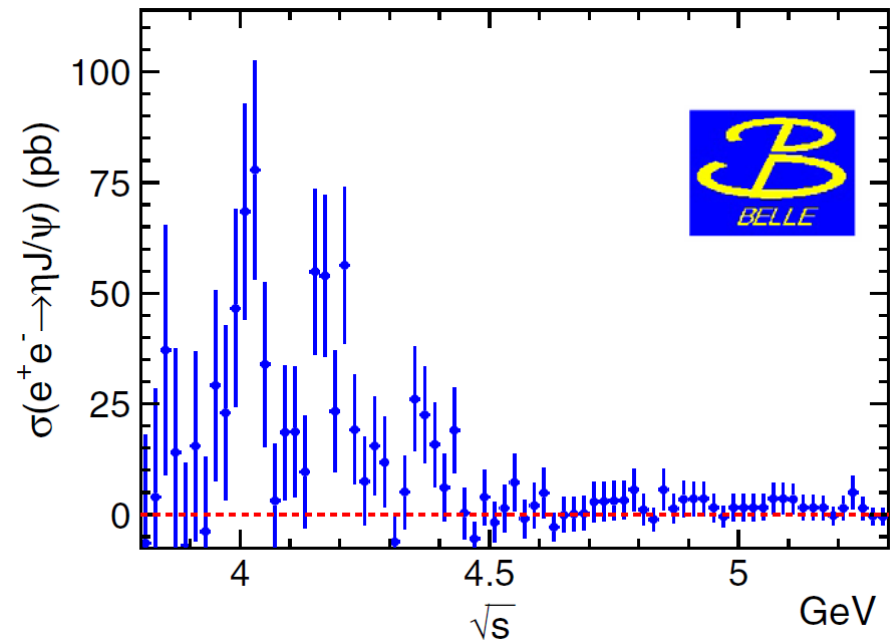


|  |                       |                           |
|--|-----------------------|---------------------------|
| $M_{\psi(4040)}$                                 | 4039 (fixed)          |                           |
| $\Gamma_{\psi(4040)}$                            | 80 (fixed)            | MeV                       |
| $\mathcal{B} \cdot \Gamma_{e^+e^-}^{\psi(4040)}$ | $4.8 \pm 0.9 \pm 1.5$ | $11.2 \pm 1.3 \pm 2.1$ eV |
| $M_{\psi(4160)}$                                 | 4153 (fixed)          |                           |
| $\Gamma_{\psi(4160)}$                            | 103 (fixed)           |                           |
| $\mathcal{B} \cdot \Gamma_{e^+e^-}^{\psi(4160)}$ | $4.0 \pm 0.8 \pm 1.4$ | $13.8 \pm 1.3 \pm 2.1$ eV |
| $\phi$   | $336 \pm 12 \pm 14$   | $251 \pm 4 \pm 7$ eV      |

transition rates to  $\eta$   $J/\psi$  are large, being of order 1 MeV/c<sup>2</sup>

# Cross section of $e^+e^- \rightarrow \eta J/\Psi$

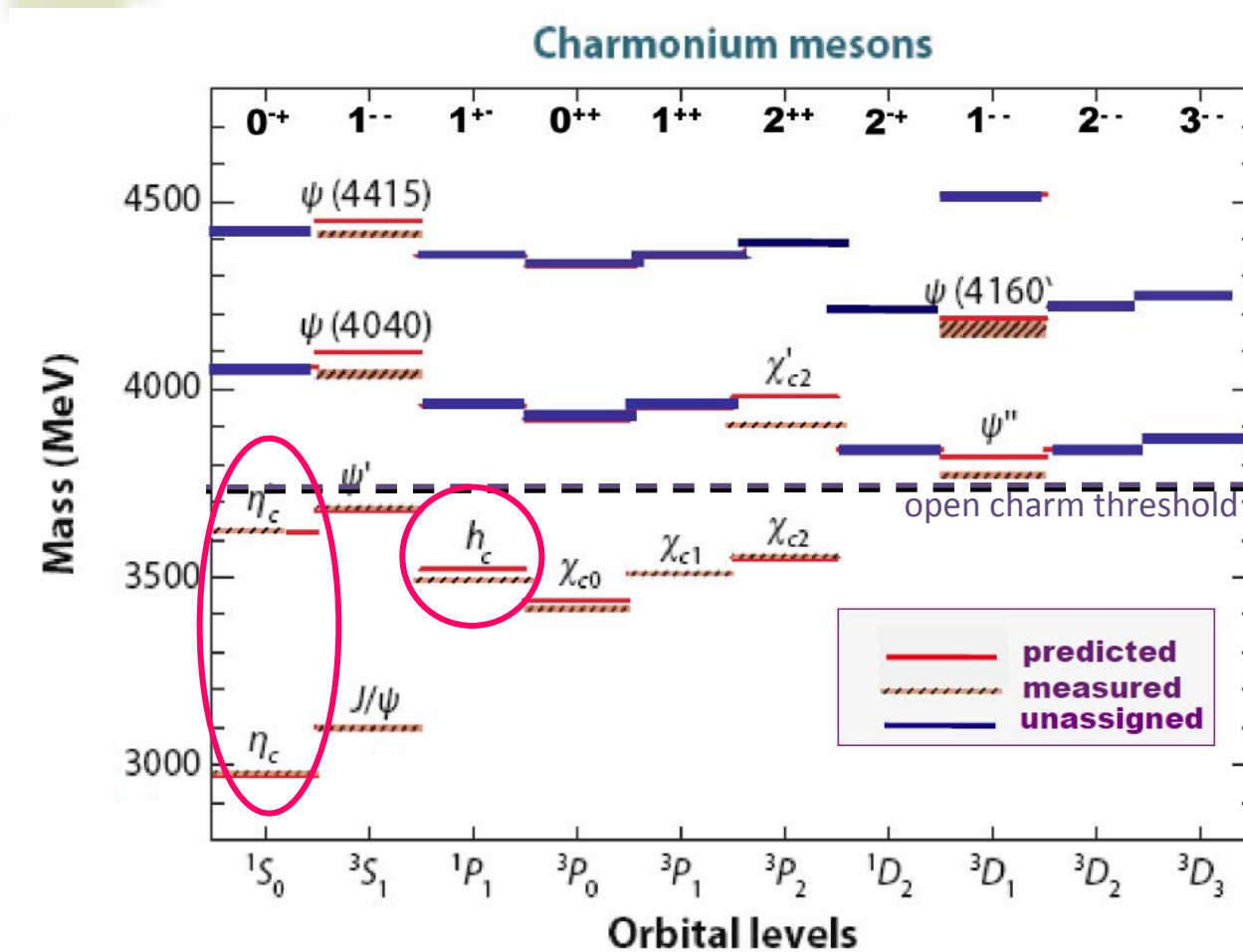
- ❖ We find no evidence for the  $Y(4260)$ ,  $Y(4360)$ ,  $\Psi(4415)$  or  $Y(4660)$  in the  $\eta J/\psi$  final states
- ❖ The cross sections of  $e^+e^- \rightarrow \eta J/\psi$  are around 70 pb and 50 pb at the  $\Psi(4040)$  and  $\Psi(4160)$  peaks, to be compared with around 20pb and 10pb measured in  $e^+e^- \rightarrow \pi^+ \pi^- J/\psi$



**This is the first time that the  $\psi(4040)$  and  $\psi(4160)$  have been observed to decay to final states not involving charm meson pairs.**

# Spin singlet states: $\eta_c$ $\eta_c(2S)$ $h_c$

- Be produced in  $\gamma\gamma$  process, B decay, pp collision, ..
- Least-understood states below the DD threshold



# $\eta_c(1S)$

❖ S-wave spin-singlet ground state, first found by MarkII in 1980  
PRL 45, 1146 (1980)

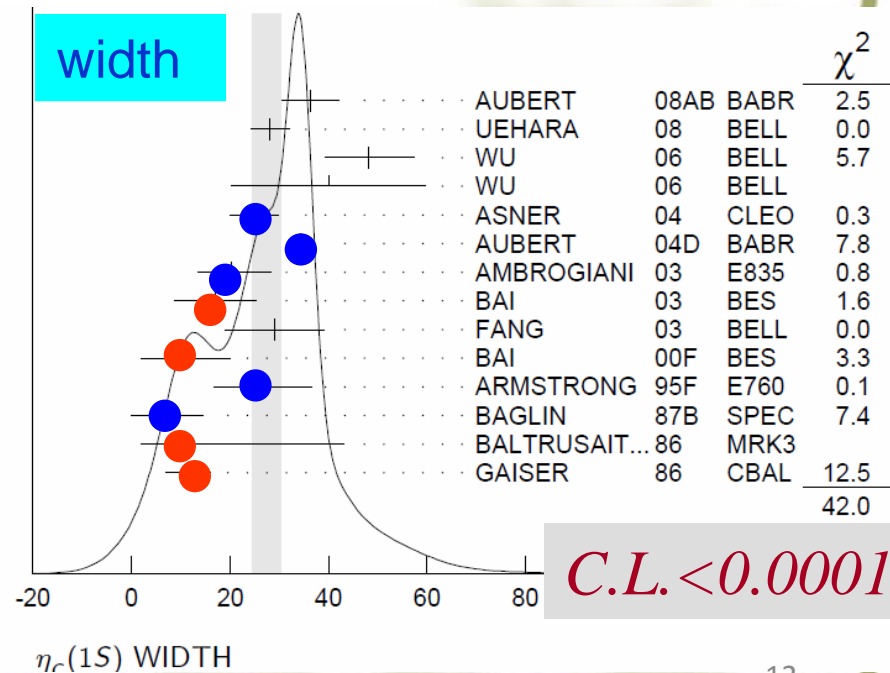
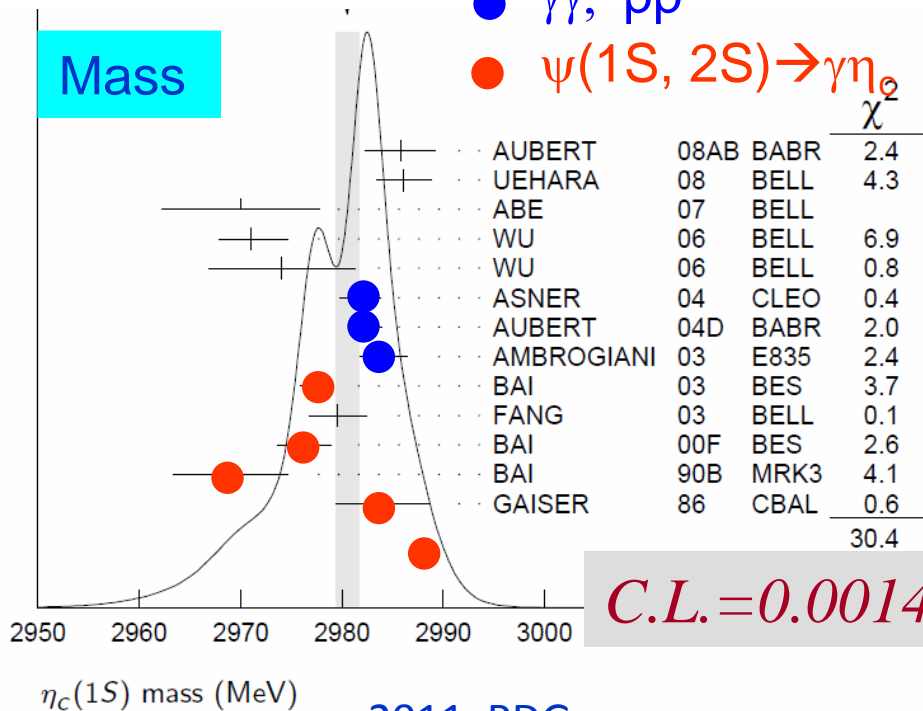
❖ The mass & width

J/ $\psi$  radiative transition:  $M \sim 2978.0 \text{ MeV}/c^2$ ,  $\Gamma \sim 10 \text{ MeV}$

$\gamma\gamma$  process:  $M = 2983.1 \pm 1.0 \text{ MeV}/c^2$ ,  $\Gamma = 31.3 \pm 1.9 \text{ MeV}$

●  $\gamma\gamma, p\bar{p}$

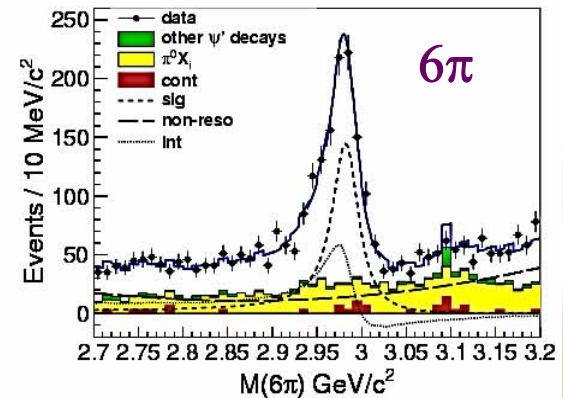
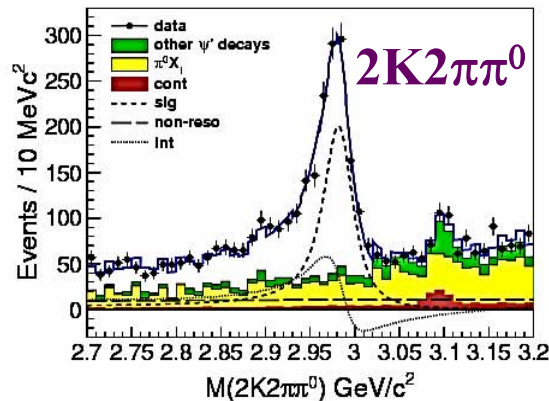
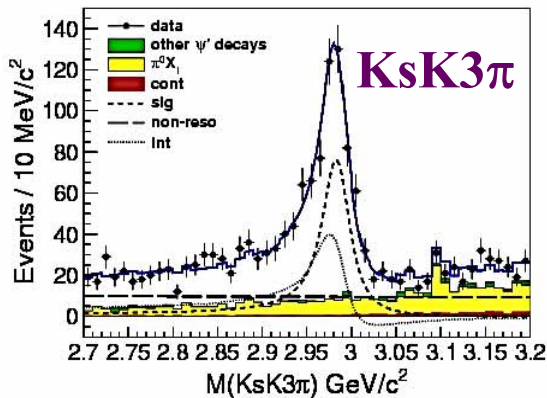
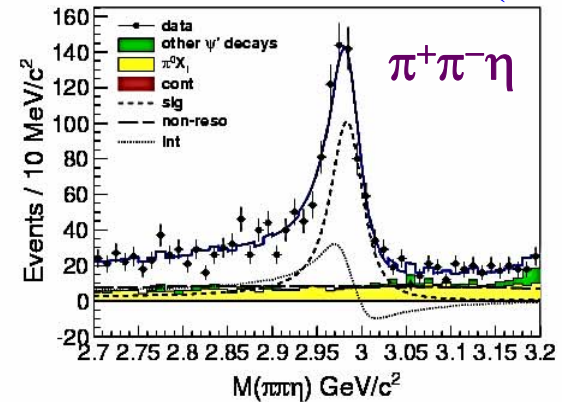
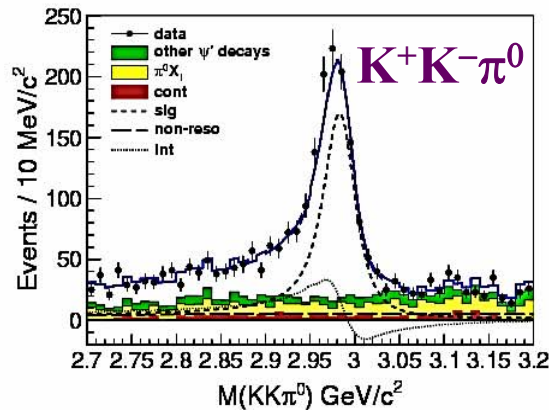
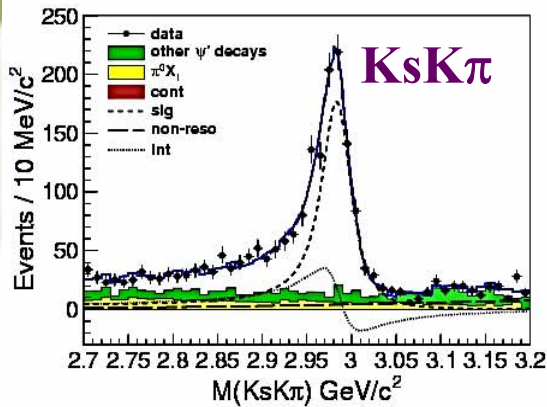
●  $\psi(1S, 2S) \rightarrow \gamma\eta_c$





# Measure $\eta_c$ in $\psi' \rightarrow \gamma \eta_c$

PRL 108,222002(2012)



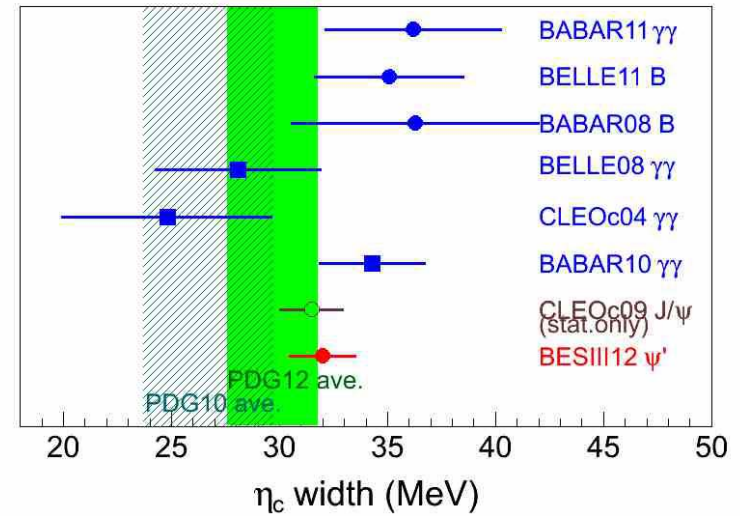
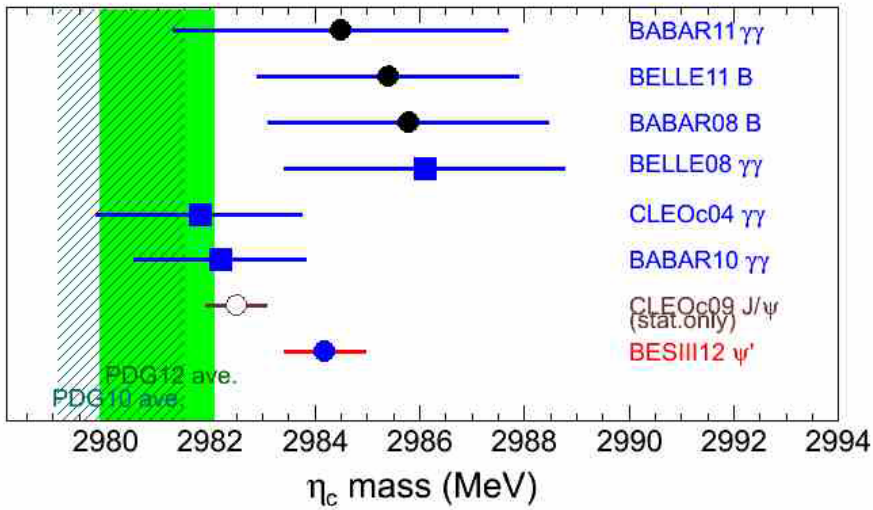
**The interference between  $\eta_c$  and non-resonant is significant.**  
 Simultaneous fit to 6 modes,

$$\text{Mass} = 2984.3 \pm 0.6 \pm 0.6 \text{ MeV}/c^2$$

$$\text{Width} = 32.0 \pm 1.2 \pm 1.0 \text{ MeV}$$



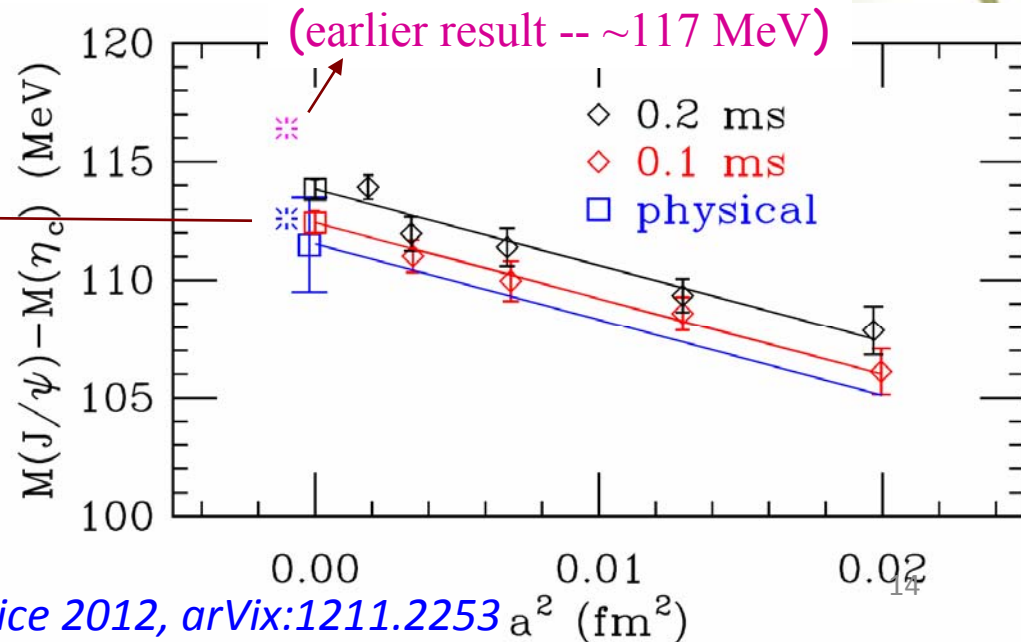
# Comparison with the $\eta_c$ results



Hyperfine splitting (BESIII alone)

$$\Delta M(1S) = 112.5 \pm 0.8 \text{ MeV}$$

Closer to prediction than earlier result



# $\eta_c(2S)$

Crystal Ball's "first observation" of  $\psi' \rightarrow \gamma X$  never been confirmed  
PRL 48 70 (1982); until Belle found it in  $B \rightarrow K\eta_c(2S)$  in 2002.

## Observed in different production mechanisms,

1.  $B \rightarrow K\eta_c(2S)$  *Belle: PRL 89 102001 (2002)*  
*CLEOc: PRL 92 142001 (2004)*
2.  $\gamma\gamma \rightarrow \eta_c(2S) \rightarrow KK\pi$  *Belle: NPPS.184 220 (2008); PRL 98 082001(2007)*
3. double charmonium production  
*BaBar: PRL 92 142002 (2004); PR D72 031101(2005)*  
*BaBar: PR D84 012004 (2011)*
4. M1 transition  $\psi' \rightarrow \gamma\eta_c(2S)$   
CLEO found no signals in 25M  $\psi'$ .

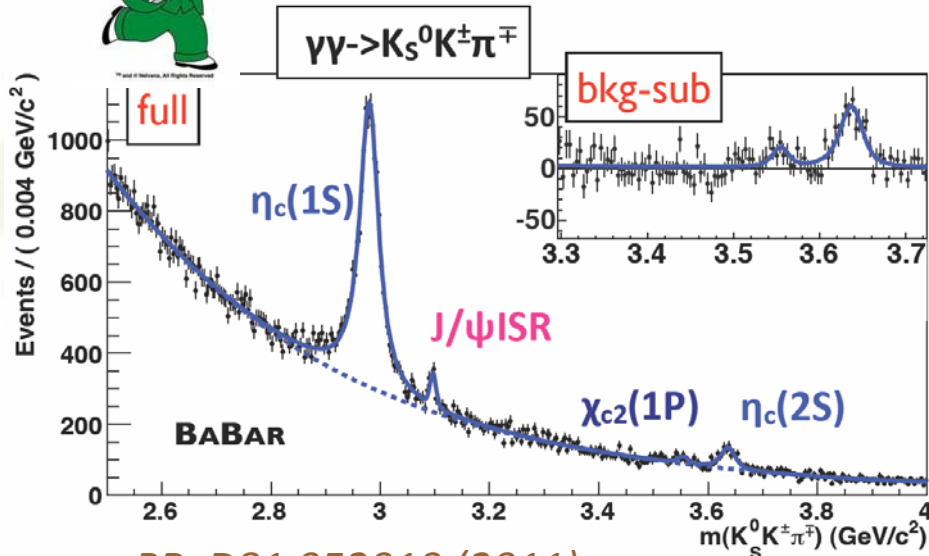
$$BF(\psi' \rightarrow \gamma\eta_c(2S)) < 7.6 \times 10^{-4}$$

*PRD 81 052002 (2010)*

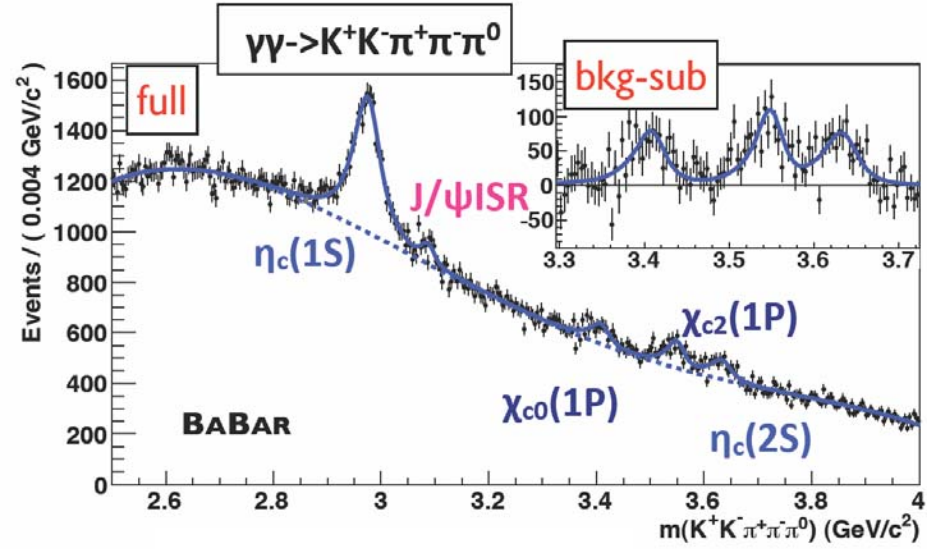
**Experimental challenge : search for photons of 50 MeV**



# $\gamma\gamma \rightarrow \eta_c(1S/2S) \rightarrow K_S K \pi; KK3\pi$



PR D81 052010 (2011)



PR D84 012004 (2011)

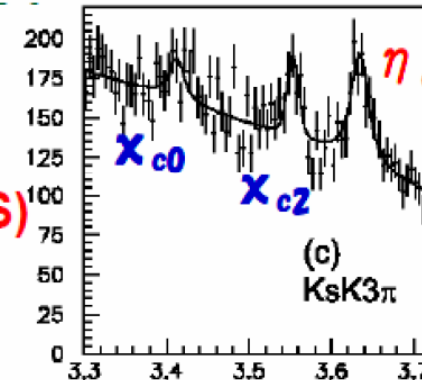
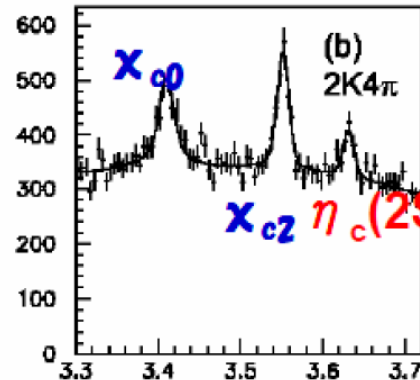
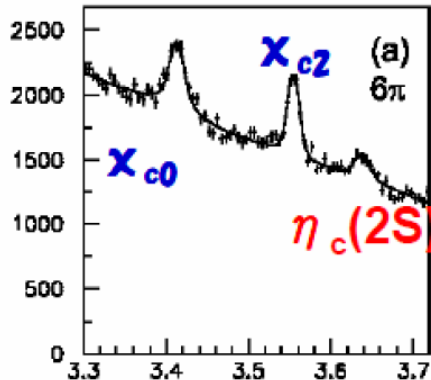


$6\pi(\pi^+\pi^-\pi^+\pi^-\pi^+\pi^-)$

$2K4\pi(K^+K^-\pi^+\pi^-\pi^+\pi^-)$

$K_S K 3\pi(K_S K^\pm \pi^\mp \pi^+ \pi^-)$

Nevents/5 MeV



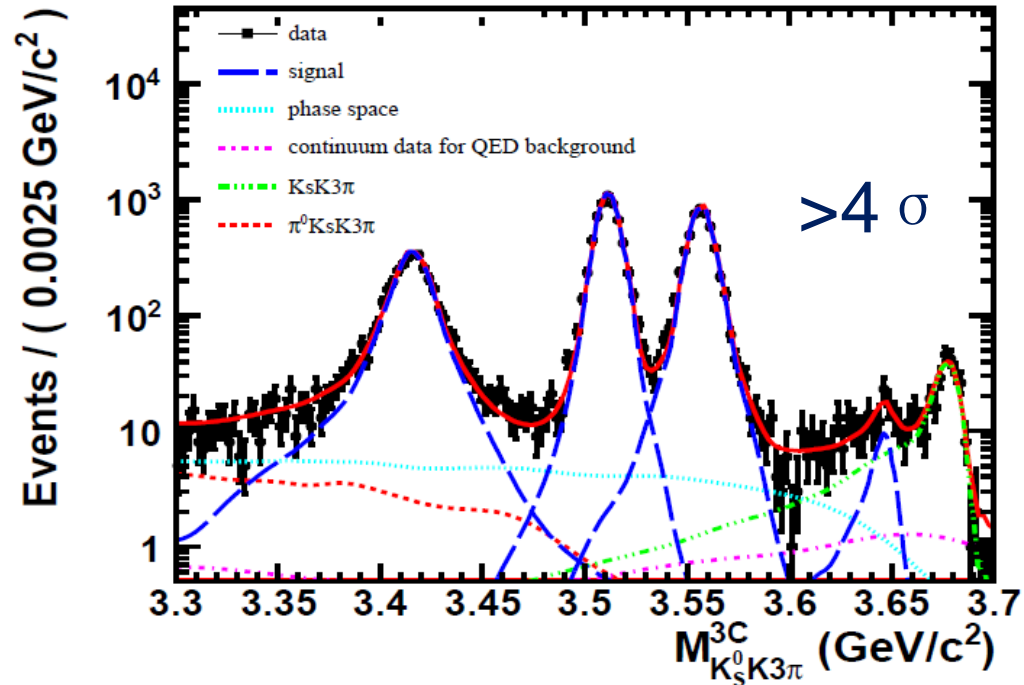
ICHEP2010

M(hadrons) (GeV)

# Evidence $\eta_c(2S) \rightarrow K_s K^+ \pi^- \pi^+ \pi^-$

PRD 87,052005(2013)

- ❖ For  $\eta_c(2S)$ , only two measured decay Brs are available:  $KK\pi$  and  $K^+K^- \pi^+ \pi^- \pi^0$
- ❖  $\psi' \rightarrow \gamma \eta_c(2S)$ : M1 transition
- ❖ Search for more  $\eta_c(2S)$  decay modes
- ❖ To measure the mass, width of  $\eta_c(2S)$



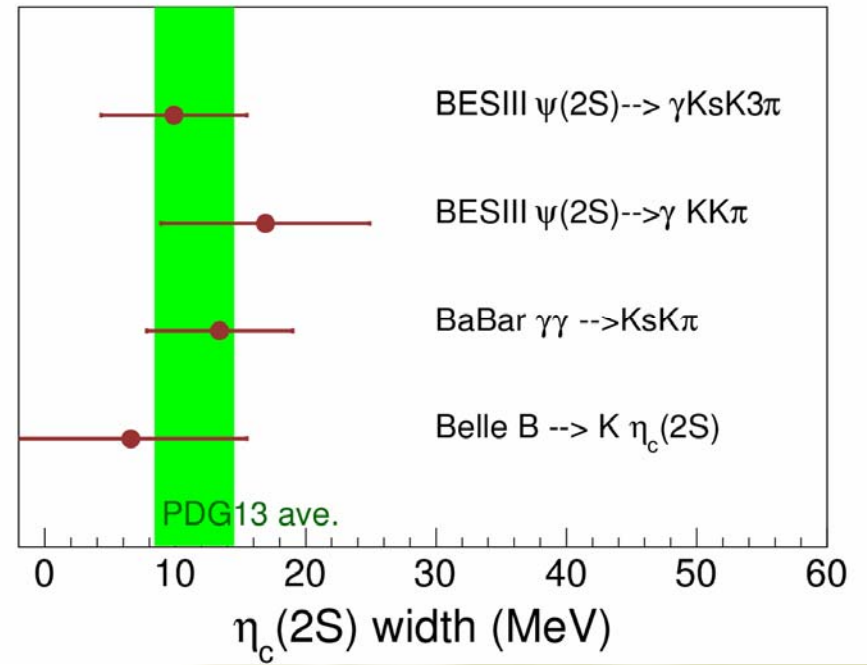
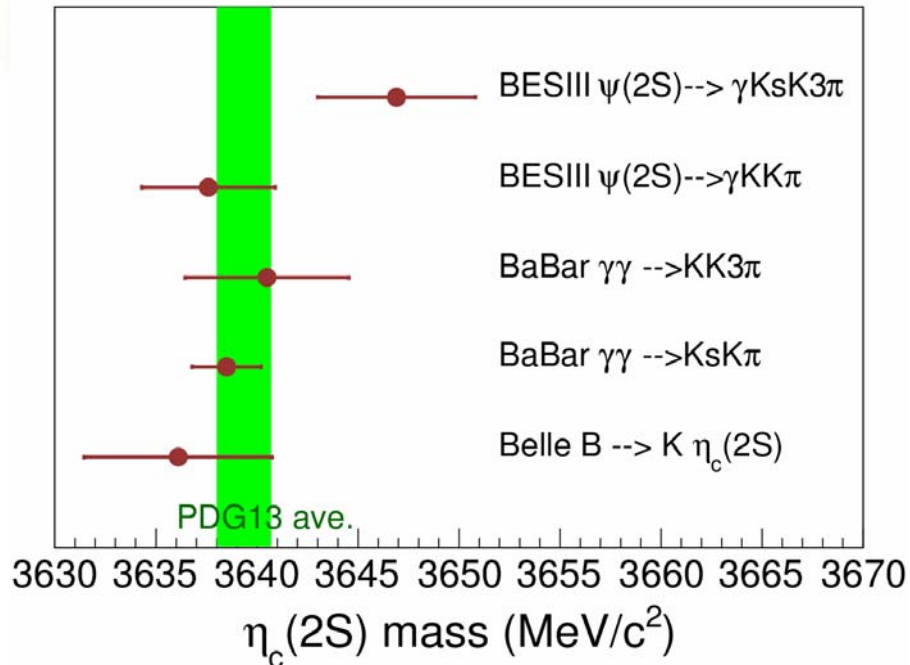
$$M = 3646.9 \pm 1.6 \pm 3.6 \text{ MeV}/c^2$$

$$\Gamma = 9.2 \pm 4.8 \pm 2.9 \text{ MeV}$$

$$B(\psi' \rightarrow \gamma \eta_c(2S)) \times B(K_s K^+ \pi^- \pi^+ \pi^-) = (7.03 \pm 2.10 \pm 0.70) \times 10^{-6}$$

The measured  $M$  and  $\Gamma$  are consistent with values in PRL109, 042003 (2012)

# Summary for $\eta_c(2S)$



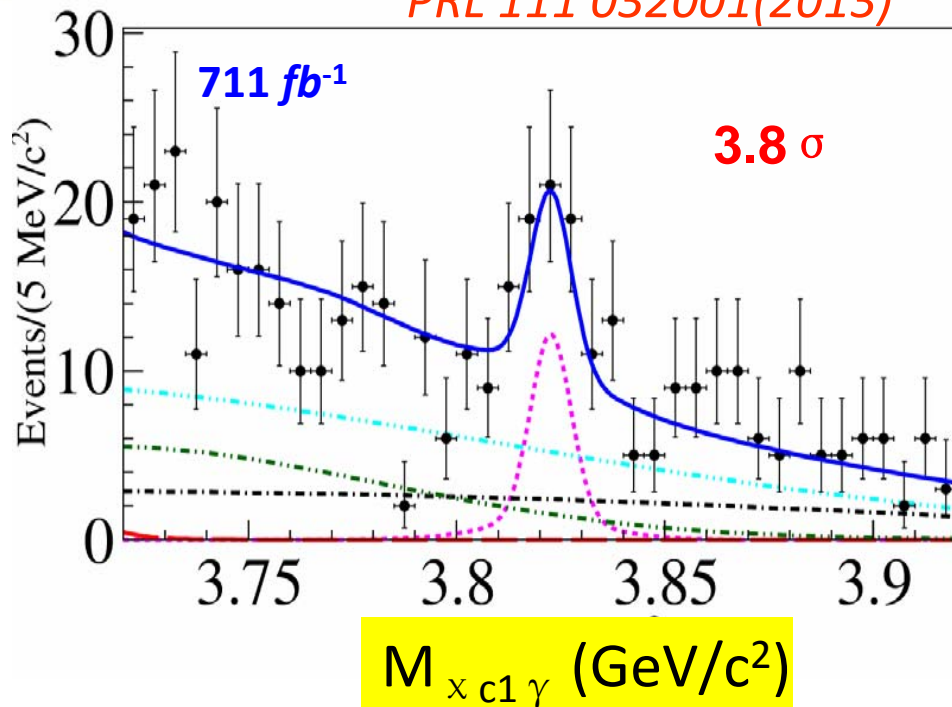


# $X(3823) \rightarrow \chi_{c1} \gamma$ in $B \rightarrow \chi_{c1} \gamma K$

Simultaneous fit to  $B^\pm \rightarrow \chi_{c1} \gamma K^\pm$  &  $B^0 \rightarrow \chi_{c1} \gamma K_S$

$\chi_{c1}$  reconstructed in  $\gamma J/\psi$

*PRL 111 032001(2013)*



$$M_{X(3823)} = M_{X(3823)}^{meas} - M_{\psi'}^{meas} + M_{\psi'}^{PDG}$$

$$= 3823.1 \pm 1.8 \pm 0.7 \text{ MeV}$$

The measured mass and other properties are consistent with the missing  $\psi_2(1^3D_2)$  state

# What is the X(3872)?

❖ Mass: Very close to  $\bar{D}^0 D^{*0}$  threshold

❖ Width: Very narrow,  $< 1.2$  MeV

❖  $J^{PC}=1^{++}$  [LHCb]

❖ Production

↪ in  $\bar{p}p/pp$  collision – rate similar to charmonia

↪ In B decays –  $KX$  similar to  $\bar{c}c$ ,  $K^*X$  smaller than  $\bar{c}c$

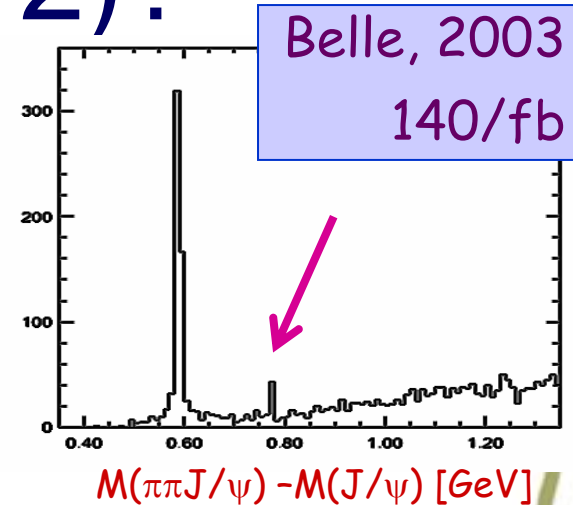
↪  $Y(4260) \rightarrow \gamma + X(3872)$  [BESIII, see next slides]

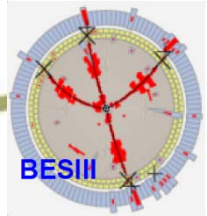
❖ Nature (very likely exotic)

↪ Loosely  $\bar{D}^0 D^{*0}$  bound state (like deuteron?)

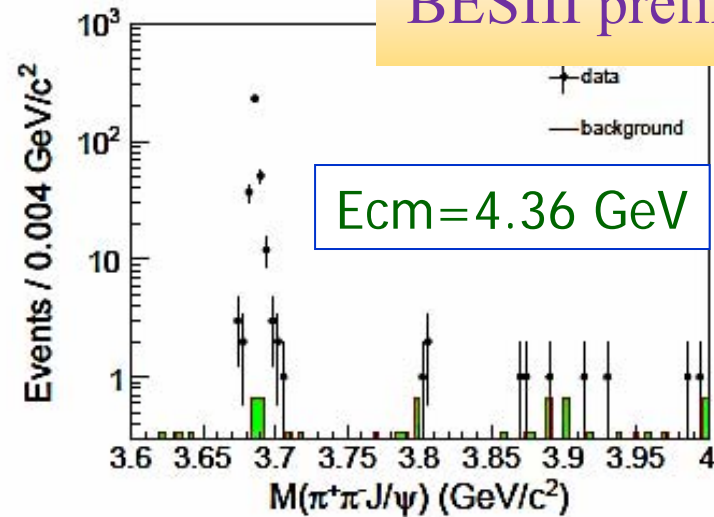
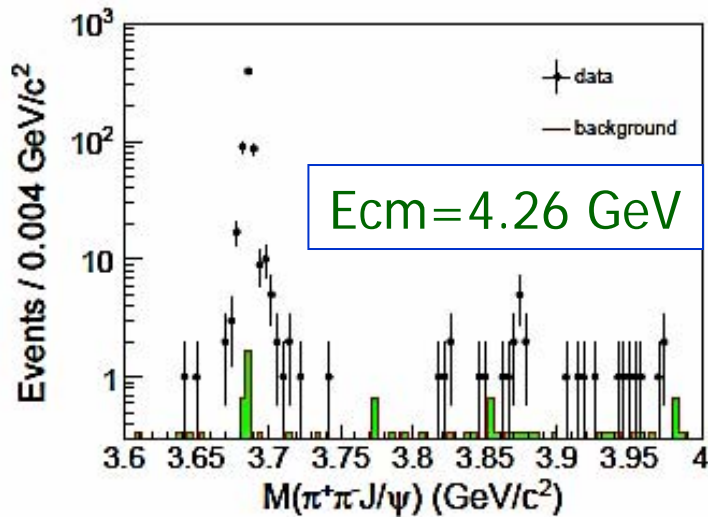
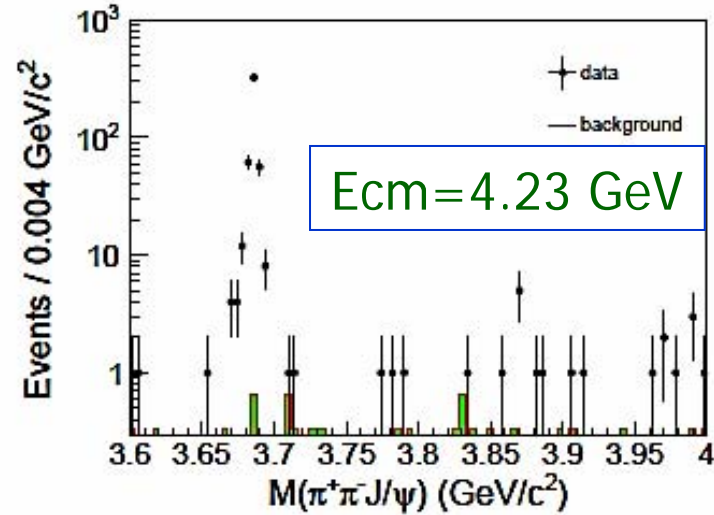
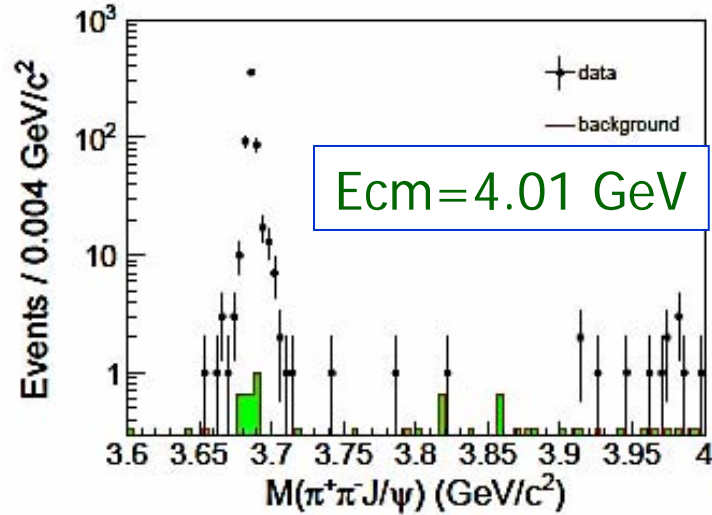
↪ Mixture of excited  $\chi_{c1}$  and  $\bar{D}^0 D^{*0}$  bound state?

↪ Many other possibilities (if it is not  $\chi'_{c1}$ , where is  $\chi'_{c1}$ ?)



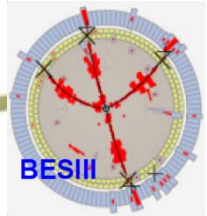


# Observation of $e^+e^- \rightarrow \gamma X(3872) \rightarrow \gamma \pi^+ \pi^- J/\psi$

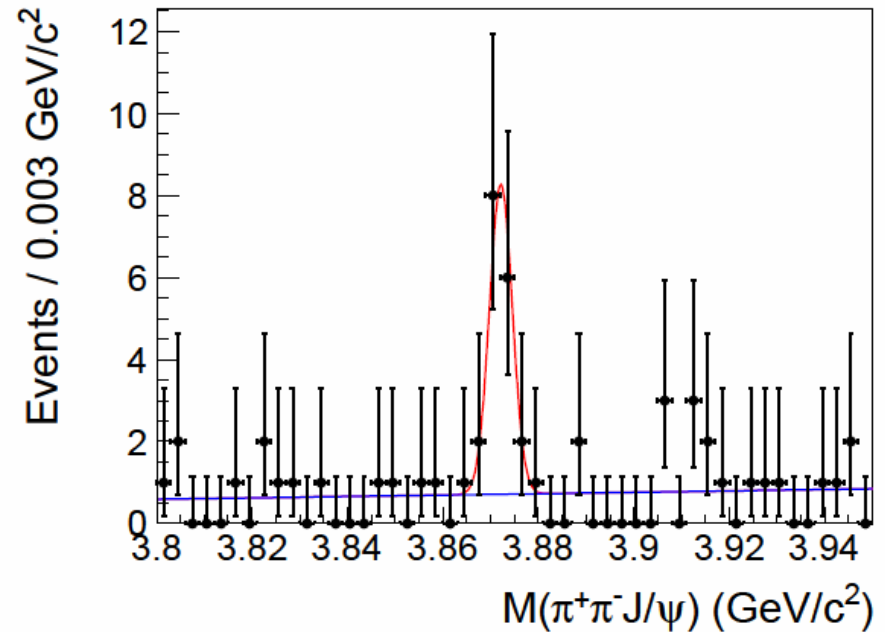
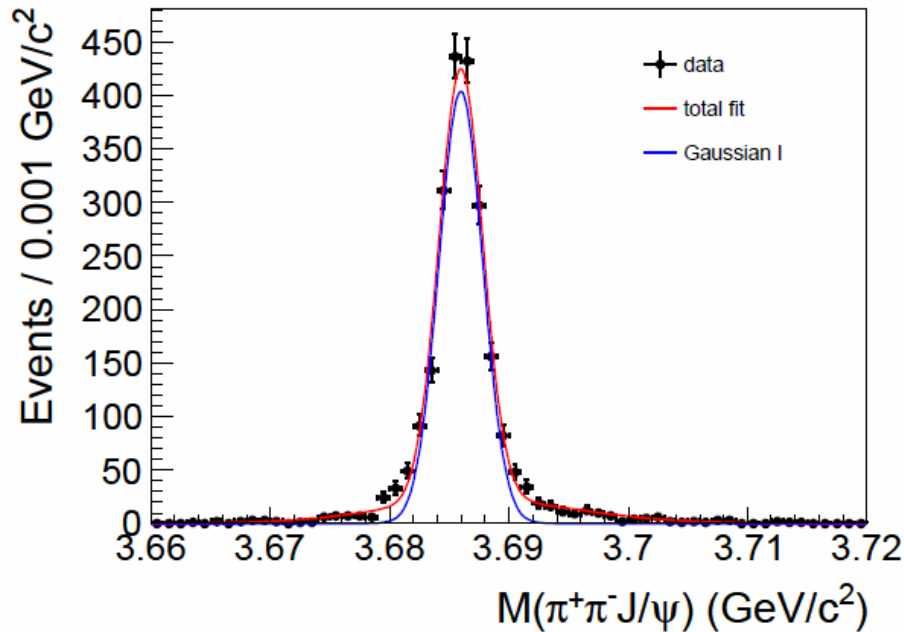


BESIII preliminary

Clear ISR  $\psi'$  signal for data validation  
X(3872) signal at around 4.23-4.26 GeV



# Observation of $e^+e^- \rightarrow \gamma X(3872)$



ISR  $\psi'$  signal is used for rate, mass, and mass resolution calibration.

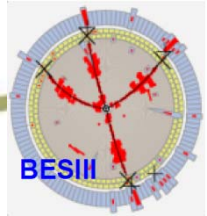
$N(\psi')=1242$  ;  $Mass=3685.96 \pm 0.05$  MeV;  $\sigma_M=1.84 \pm 0.06$  MeV

BESIII preliminary

$N(X(3872))=15.0 \pm 3.9$

**5.3 $\sigma$**

$M(X(3872)) = 3872.1 \pm 0.8 \pm 0.3$  MeV [PDG:  $3871.68 \pm 0.17$  MeV]



# Observation of $e^+e^- \rightarrow \gamma X(3872)$

---

| $\sqrt{s}$ (GeV) | $\sigma^B[e^+e^- \rightarrow \gamma X(3872)] \cdot \mathcal{B}(X(3872) \rightarrow \pi^+\pi^- J/\psi)$ (pb) |
|------------------|---|
| 4.009            | $< 0.13$ at 90% C.L.  |
| 4.230            | $0.32 \pm 0.15 \pm 0.02$  |
| 4.260            | $0.35 \pm 0.12 \pm 0.02$  |
| 4.360            | $< 0.39$ at 90% C.L.  |

---

It seems  $X(3872)$  is from  $Y(4260)$  decays. At 4.26 GeV,

$$\sigma^B(e^+e^- \rightarrow \pi^+\pi^- J/\psi) = (62.9 \pm 1.9 \pm 3.7) \text{ pb},$$

$$\frac{\sigma[e^+e^- \rightarrow \gamma X(3872)] \cdot \mathcal{B}(X(3872) \rightarrow \pi^+\pi^- J/\psi)}{\sigma(e^+e^- \rightarrow \pi^+\pi^- J/\psi)} = (5.6 \pm 2.0) \times 10^{-3}$$

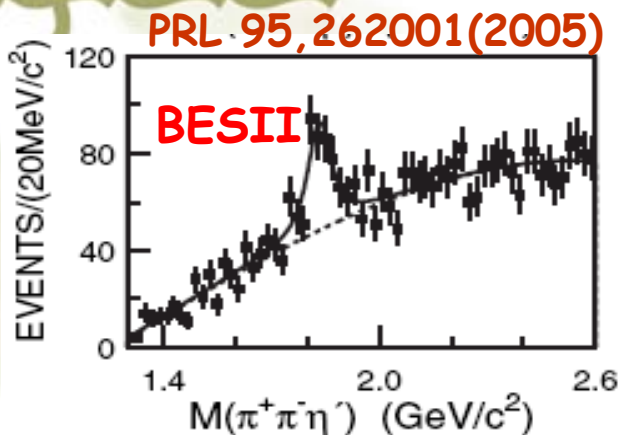
If we take  $\mathcal{B}(X(3872) \rightarrow \pi^+\pi^- J/\psi) \sim 5\%$ , ( $>2.6\%$  in PDG)

$$\frac{\sigma(e^+e^- \rightarrow \gamma X(3872))}{\sigma(e^+e^- \rightarrow \pi^+\pi^- J/\psi)} \sim 11.2\% \quad \text{Large transition ratio !}$$



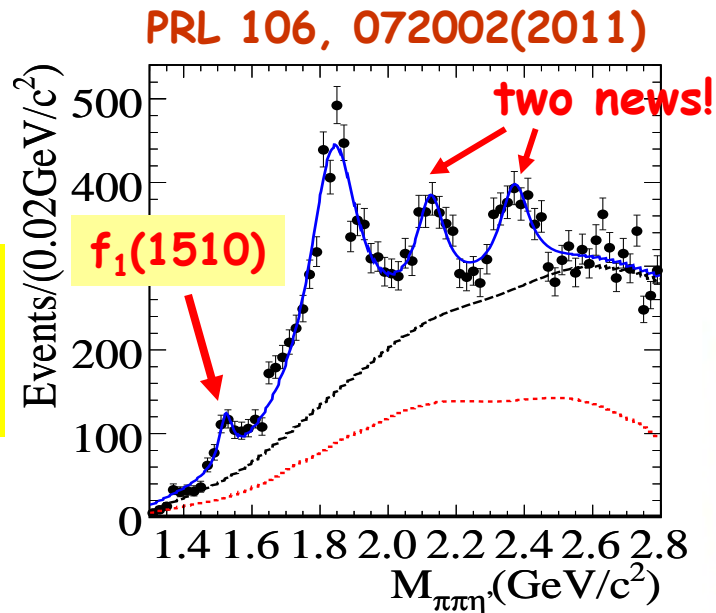
# light hadron spectroscopy

# Confirmation of X(1835) and two new structures



**BESIII**  
 $J/\psi \rightarrow \gamma(\eta' \pi^+ \pi^-)$

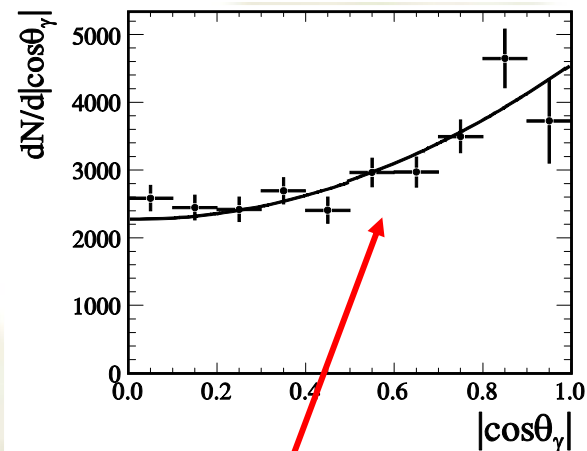
**BESIII: 225M  
 $J/\psi$  events,  
 new structures!**



**BESII result (Stat. sig.  $\sim 7.7\sigma$ ):**  
 $M = 1833.7 \pm 6.1(stat) \pm 2.7(syst) MeV$   
 $\Gamma = 67.7 \pm 20.3(stat) \pm 7.7(syst) MeV$

## BESIII fit results:

| Resonance | $M( MeV/c^2)$                  | $\Gamma( MeV/c^2)$          | Stat.Sig.    |
|-----------|--------------------------------|-----------------------------|--------------|
| X(1835)   | $1836.5 \pm 3.0^{+5.6}_{-2.1}$ | $190.1 \pm 9.0^{+38}_{-36}$ | $>20 \sigma$ |
| X(2120)   | $2122.4 \pm 6.7^{+4.7}_{-2.7}$ | $83 \pm 16^{+31}_{-11}$     | $7.2 \sigma$ |
| X(2370)   | $2376.3 \pm 8.7^{+3.2}_{-4.3}$ | $83 \pm 17^{+44}_{-6}$      | $6.4 \sigma$ |

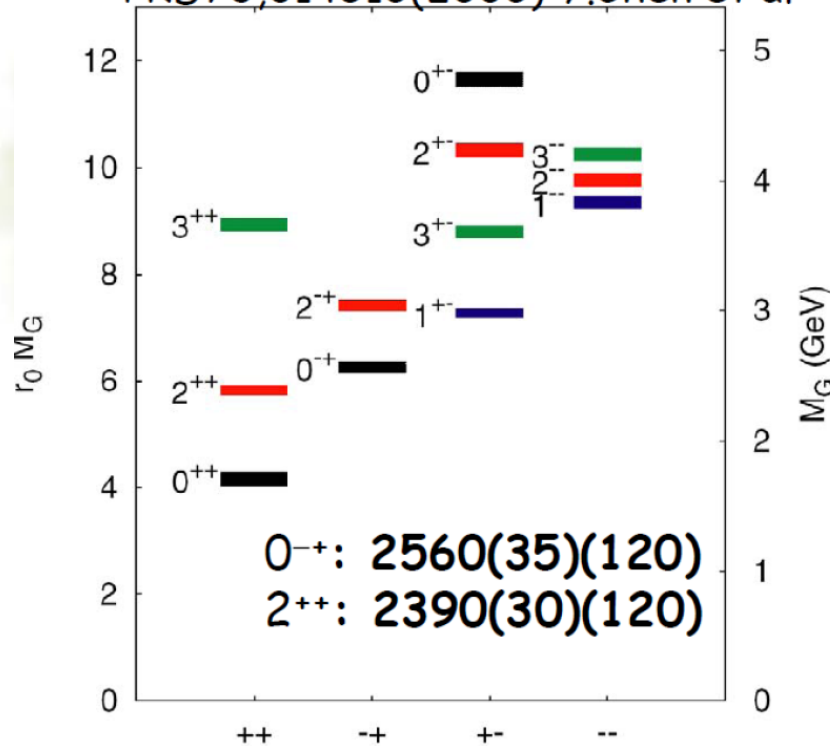


**X(1835) favors  $0^{-+}$**

**An amplitude analysis could help with interpretation for the additional new structures!**

# Possible theoretical explanation

PRD73,014516(2006) Y.Chen et al



✓ It is the first time resonant structures are observed in the 2.3 GeV/c<sup>2</sup> region, it is interesting since:

LQCD predicts that the lowest lying pseudoscalar glueball: around 2.3 GeV/c<sup>2</sup>.

$J/\psi \rightarrow \gamma \pi \pi \eta'$  decay is a good channel for finding  $0^{-+}$  glueballs.

✓ Nature of X(2120)/X(2370) pseudoscalar glueball?  $\eta/\eta'$  excited states?

Finally we need a full amplitude analysis to determine the property for the new structures, but there were many predictions which make the observation more interesting!

PRD82,074026,2010

J.F. Liu, G.J. Ding and M.L. Yan

PRD83:114007,2011

([J.S. Yu](#), [Z.-F. Sun](#), [X. Liu](#), [Q. zhao](#)),

and more...

# $\eta_c, \eta(1760)$ and $X(1835)$ in $\gamma\gamma \rightarrow \eta' \pi^+ \pi^-$

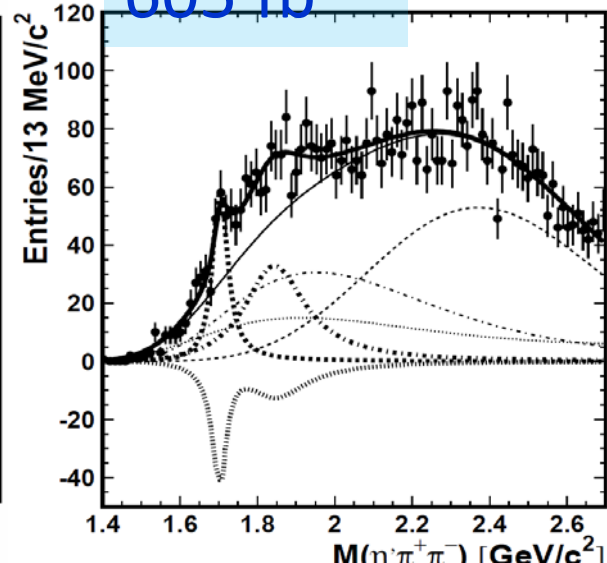
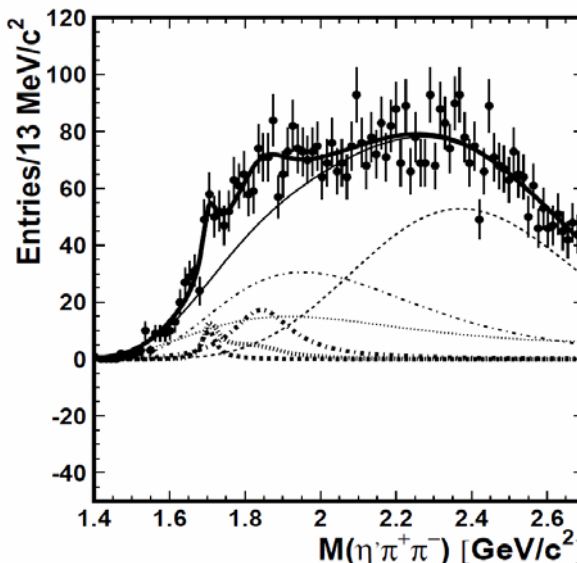


PRD 86, 052002 (2012)

605 fb<sup>-1</sup>

**Search for X(1835) in Belle experiment in two-photon process !**

- ▼ X(1835) and  $\eta(1760)$  with interference (assuming  $J^{PC}=0^{++}$ )
- ▼ No interference between resonant and non-resonant
- ▼ Two solutions (see Table)



**No significant X(1835) signal --- 2.8  $\sigma$  !**

- ★ thin solid line: total bkg
- ★ thick dashed (dot-dashed, dotted) lines: the  $\eta(1760)$  (X(1835), the interference term)
- ★ thin dashed, dot-dashed and dotted lines: non-resonant,  $\eta'$ -sidebands and  $\eta' \pi^+ \pi^- X$  bkg components

◆ The fit with only  $\eta(1760)$  signal is also tried

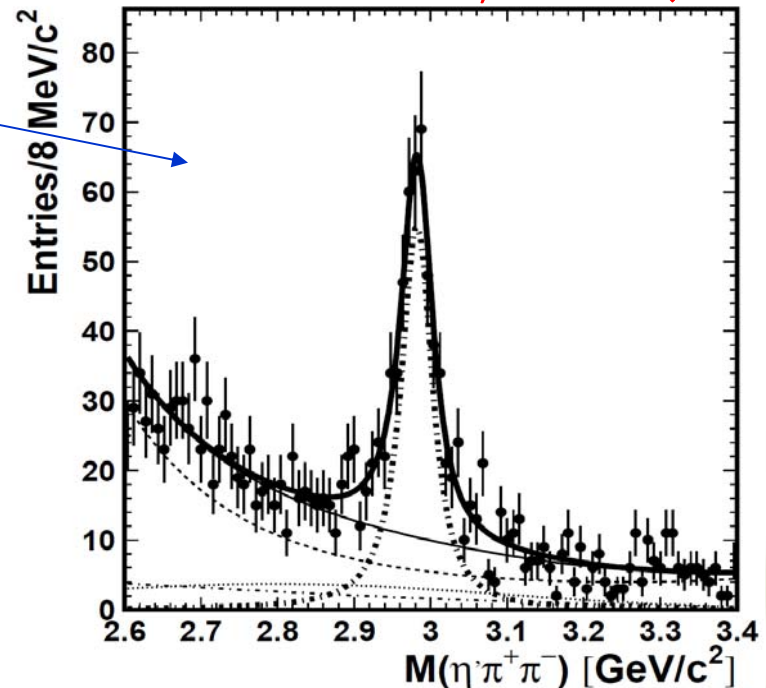
| Parameter                                       | One resonance                | Two interfering resonances   |                             |
|---|------------------------------|------------------------------|-----------------------------|
|   |                              | Solution I                   | Solution II                 |
| <u>X(1835)</u>                                  |                              |                              |                             |
| $M, \text{MeV}/c^2$                             |                              | 1836.5 (fixed)               |                             |
| $\Gamma, \text{MeV}/c^2$                        |                              | 190 (fixed)                  |                             |
| $Y$   |                              | $332^{+140}_{-122} \pm 73$   | $632^{+224}_{-231} \pm 139$ |
| $Y_{90}$  |                              | $< 650$                      | $< 1490$                    |
| $\Gamma_{\gamma\gamma} B, \text{eV}/c^2$        |                              | $18.2^{+7.7}_{-6.7} \pm 4.0$ | $35^{+12}_{-13} \pm 8$      |
| $(\Gamma_{\gamma\gamma} B)_{90}, \text{eV}/c^2$ |                              | $< 35.6$                     | $< 83$                      |
| $S, \sigma$                                     |                              | 2.8                          |                             |
| <u><math>\eta(1760)</math></u>                  |                              |                              |                             |
| $M, \text{MeV}/c^2$                             | $1768^{+24}_{-25} \pm 10$    | $1703^{+12}_{-11} \pm 1.8$   |                             |
| $\Gamma, \text{MeV}/c^2$                        | $224^{+62}_{-56} \pm 25$     | $42^{+36}_{-22} \pm 15$      |                             |
| $Y$   | $465^{+131}_{-124} \pm 60$   | $52^{+35}_{-20} \pm 15$      | $315^{+223}_{-165} \pm 88$  |
| $\Gamma_{\gamma\gamma} B, \text{eV}/c^2$        | $28.2^{+7.9}_{-7.5} \pm 3.7$ | $3.0^{+2.0}_{-1.2} \pm 0.8$  | $18^{+13}_{-10} \pm 5$      |
| $S, \sigma$                                     | 4.7                          | 4.1                          |                             |
| $\phi$  |                              | $(287^{+42}_{-51})^\circ$    | $(139^{+19}_{-9})^\circ$    |

# $M(\eta' \pi^+ \pi^-)$ in $\eta_c$ mass region

❖ Assuming no interference between  $\eta_c$  and background

★ The fit with interference was also tried. The results of mass and width of  $\eta_c$  are almost the same. The differences are taken as sys error.

PRD 86, 052002 (2012)



| Parameters   | This work                    | PDG              |
|--|------------------------------|------------------|
| $Y$  | $486^{+40}_{-39} \pm 53$     |                  |
| $M, \text{MeV}/c^2$                                | $2982.7 \pm 1.8 \pm 2.2$     | $2980.3 \pm 1.2$ |
| $\Gamma, \text{MeV}/c^2$                           | $37.8^{+5.8}_{-5.3} \pm 2.8$ | $26.7 \pm 3$     |
| $\Gamma_{\gamma\gamma} \mathcal{B}, \text{eV}/c^2$ | $50.5^{+4.2}_{-4.1} \pm 5.6$ | $194 \pm 97$     |
| $\mathcal{B}, \%$                                  | $0.87 \pm 0.20$              | $2.7 \pm 1.1$    |

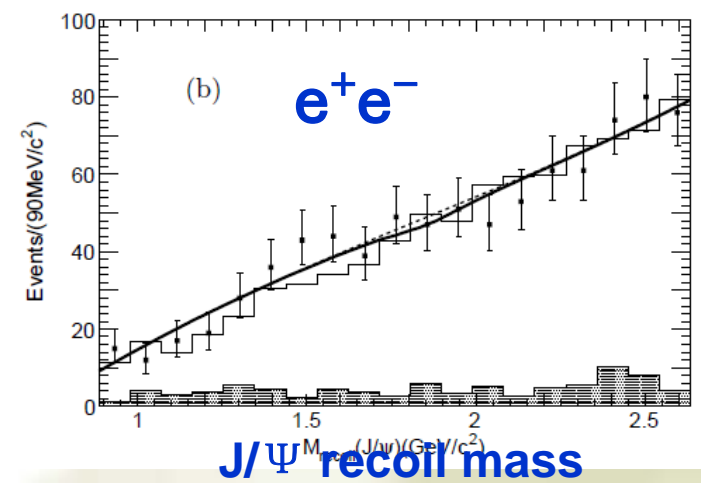
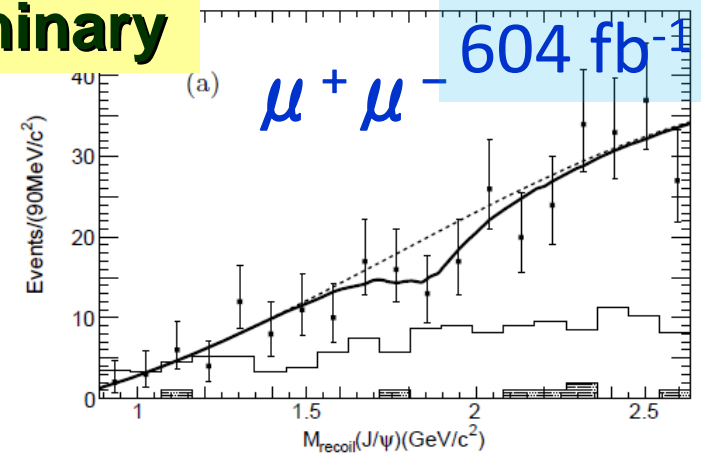


# Search for $e^+e^- \rightarrow J/\Psi + X(1835)$ at 10.6 GeV

**Preliminary**

- ❖ Search for X(1835) in Belle experiment in  $e^+e^-$  continuum process !
- ❖ C-even glueballs can be studied in  $e^+e^- \rightarrow \gamma^* \rightarrow H+G_J$ , H denotes a  $c\bar{c}$  quark pair or charmonium state

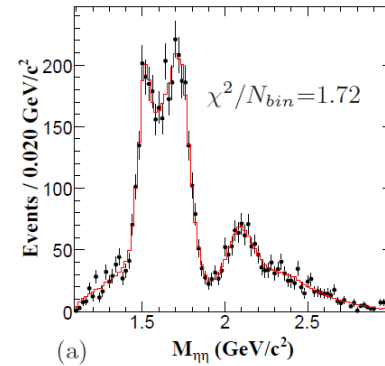
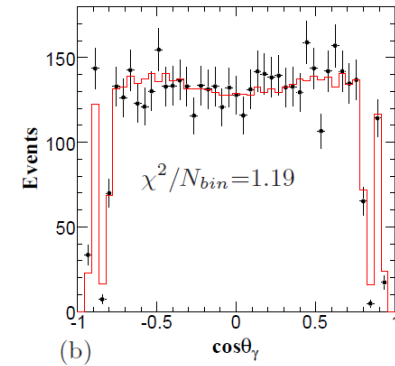
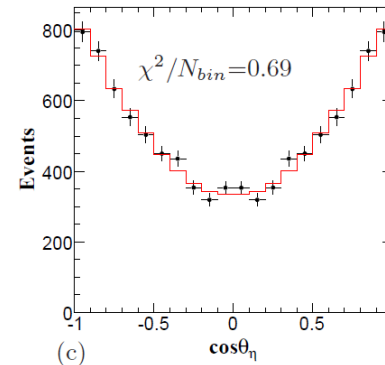
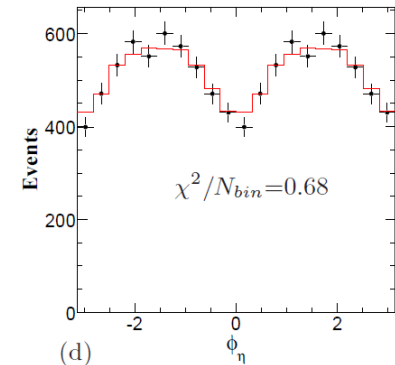
- ❖ Signal pdf is from MC with mass and width fixed to the values from BESIII [PRL 106, 072002, 2012]
- ❖ 90% C.L. upper limit on the  $\sigma(e^+e^- \rightarrow J/\Psi X(1835)) \text{Br}(X(1835) \rightarrow \text{charged tracks}) < 1.3 \text{ fb}$



open histogram:  $J/\Psi$  sidebands  
 shaded histogram: charmed + uds background

| Mode  | $N_{\text{signal}}$ | $N_{\text{background}}$ |
|---|---------------------|-------------------------|
| $M_{\text{recoil}}(J/\psi \rightarrow \mu^+ \mu^-)$ | $-20.0 \pm 20.0$    | $340.0 \pm 18.0$        |
| $M_{\text{recoil}}(J/\psi \rightarrow e^+ e^-)$     | $-7.5 \pm 7.6$      | $859.5 \pm 29.2$        |

- ❖ Search for glueballs, hybrids and multi-quarks
- ❖ LQCD: the lowest mass glueball with  $0^{++}$  is in the mass region from 1.5-1.7 GeV
- ❖ The mixing with  $q\bar{q}$  nonet mesons makes the identification of the glueballs difficult
- ❖ Radiative  $J/\psi$  decay is a gluon-rich process
- ❖  $J/\psi$  radiative decay to two pseudoscalar mesons offers a very clean laboratory to search for scalar and tensor glueballs

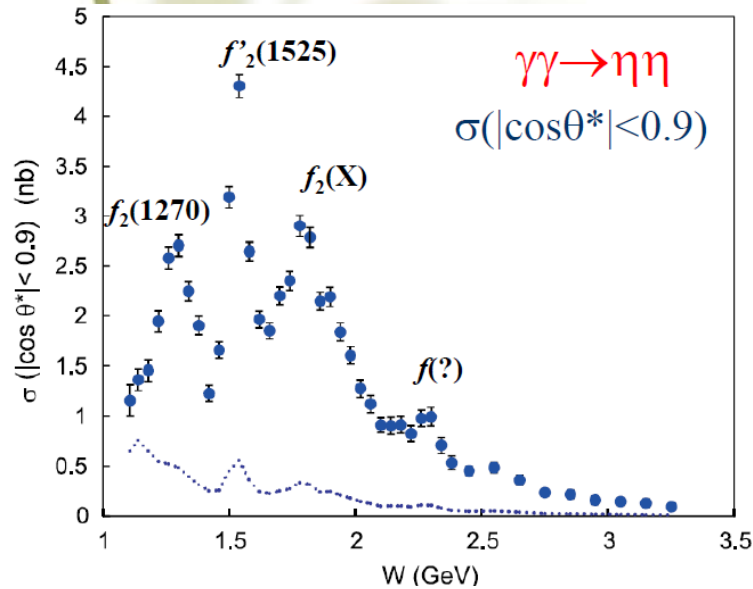

 (a)  $M_{\eta\eta}$  ( $\text{GeV}/c^2$ )

 (b)  $\cos\theta_\gamma$ 

 (c)  $\cos\theta_\eta$ 

 (d)  $\phi_\eta$ 

| Resonance    | Mass( $\text{MeV}/c^2$ )  | Width( $\text{MeV}/c^2$ ) | $\mathcal{B}(J/\psi \rightarrow \gamma X \rightarrow \gamma\eta\eta)$ | Significance  |
|--------------|---------------------------|---------------------------|---|---------------|
| $f_0(1500)$  | $1468^{+14+23}_{-15-74}$  | $136^{+41+28}_{-26-100}$  | $(1.65^{+0.26+0.51}_{-0.31-1.40}) \times 10^{-5}$                     | $8.2 \sigma$  |
| $f_0(1710)$  | $1759 \pm 6^{+14}_{-25}$  | $172 \pm 10^{+32}_{-16}$  | $(2.35^{+0.13+1.24}_{-0.11-0.74}) \times 10^{-4}$                     | $25.0 \sigma$ |
| $f_0(2100)$  | $2081 \pm 13^{+24}_{-36}$ | $273^{+27+70}_{-24-23}$   | $(1.13^{+0.09+0.64}_{-0.10-0.28}) \times 10^{-4}$                     | $13.9 \sigma$ |
| $f_2'(1525)$ | $1513 \pm 5^{+4}_{-10}$   | $75^{+12+16}_{-10-8}$     | $(3.42^{+0.43+1.37}_{-0.51-1.30}) \times 10^{-5}$                     | $11.0 \sigma$ |
| $f_2(1810)$  | $1822^{+29+66}_{-24-57}$  | $229^{+52+88}_{-42-155}$  | $(5.40^{+0.60+3.42}_{-0.67-2.35}) \times 10^{-5}$                     | $6.4 \sigma$  |
| $f_2(2340)$  | $2362^{+31+140}_{-30-63}$ | $334^{+62+165}_{-54-100}$ | $(5.60^{+0.62+2.37}_{-0.65-2.07}) \times 10^{-5}$                     | $7.6 \sigma$  |

# $\gamma\gamma \rightarrow \eta\eta$

PRD 82, 114031 (2010)

## Fits for low-mass resonances with partial-wave decomposition



| Parameter                                       | Fit (1.1-1.64GeV)                         | Unit               |
|---|---|--------------------|
| Mass $f_0(\Upsilon)$                            | $1262^{+51}_{-78} \quad ^{+82}_{-103}$    | MeV/c <sup>2</sup> |
| Width   | $484^{+246}_{-170} \quad ^{+246}_{-263}$  | MeV                |
| $\Gamma_{\gamma\gamma} B(\eta\eta)$             | $121^{+133}_{-53} \quad ^{+169}_{-106}$   | eV                 |
| $\Gamma_{\gamma\gamma} B(\eta\eta)$ $f_2(1270)$ | $11.5^{+1.8}_{-2.0} \quad ^{+4.5}_{-3.7}$ | eV                 |
| $\chi^2$ (ndf)                                  | 137.1 (119)                               |                    |

### Confirmation of $f'_2(1525)$ amplitude

| Parameter                           | Fit (1.1-1.64GeV)    | Unit | $\chi^2$ (ndf) |
|-------------------------------------|----------------------|------|----------------|
| $\Gamma_{\gamma\gamma} B(\eta\eta)$ | $f'_2(1525)$         |      |                |
| Sol. A                              | $23.1^{+2.6}_{-2.8}$ | eV   | 136.4 (119)    |
| Sol. B                              | $8.0^{+2.0}_{-1.5}$  | eV   | 137.2 (119)    |
| Sol. C                              | $5.0^{+5.8}_{-5.0}$  | eV   | 138.6 (119)    |

| Parameter                           | Fit (1.1-2.0GeV)                          | Unit               |
|-------------------------------------|---|--------------------|
| Mass                                | $1737 \pm 9 \quad ^{+198}_{-65}$          | MeV/c <sup>2</sup> |
| Width $f_2(X)$                      | $228^{+21}_{-20} \quad ^{+234}_{-153}$    | MeV                |
| $\Gamma_{\gamma\gamma} B(\eta\eta)$ | $5.2^{+0.9}_{-0.8} \quad ^{+37.3}_{-4.5}$ | eV                 |
| $\chi^2$ (ndf)                      | 311.4(204)                                |                    |

**PDG:** Product of  $\Gamma_{\gamma\gamma}$  and  $B(\eta\eta)$

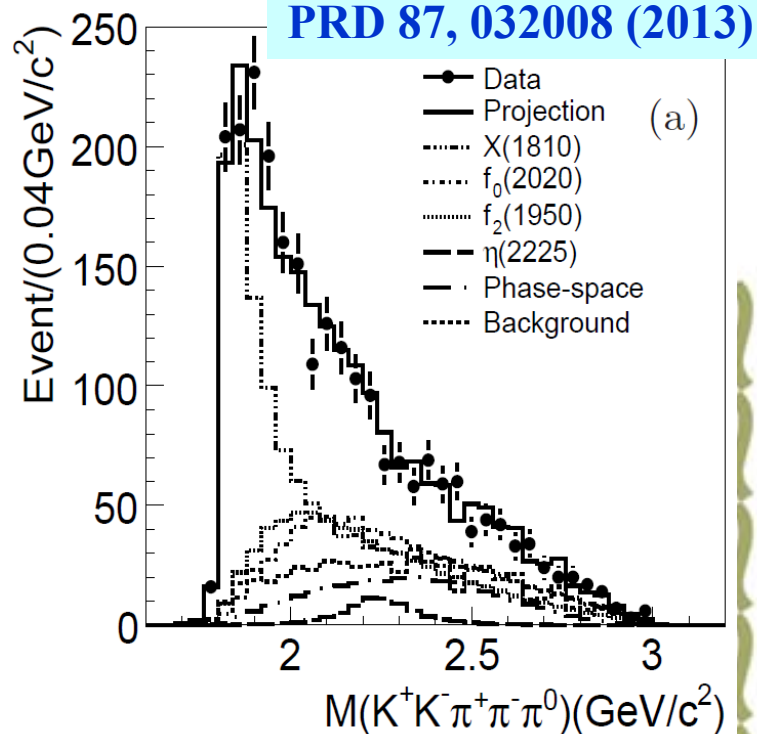
$f_2(1270)$  :  $12.1 \pm 2.8$  eV : consistent

$f'_2(1525)$  :  $8.3 \pm 2.1$  eV :

Structures are very complicated !

# PWA of $J/\psi \rightarrow \gamma \omega \phi$

- ❖  $X(1810)$  was observed in  $J/\psi \rightarrow \gamma \omega \phi$  by BESII [PRL96,162002]
- ❖ PWA:  $0^{++}$  favors  $0^{-+}$  or  $2^{++}$  ( $>10 \sigma$ )
- ❖  $J/\psi \rightarrow \gamma \omega \phi$  is a doubly OZI suppressed process
- ❖ Possible interpretations: a tetraquark state, a hybrid, or a glueball state, a dynamical effect arising from intermediate meson rescattering, or a threshold cusp of an attracting resonance.

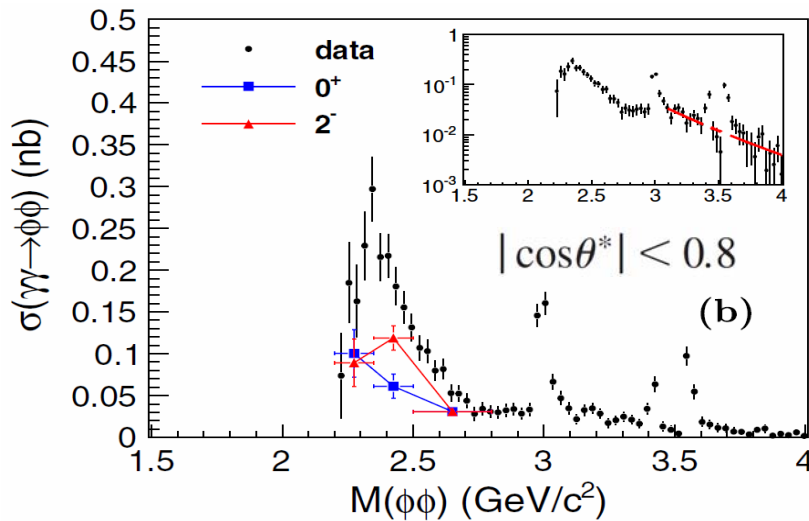
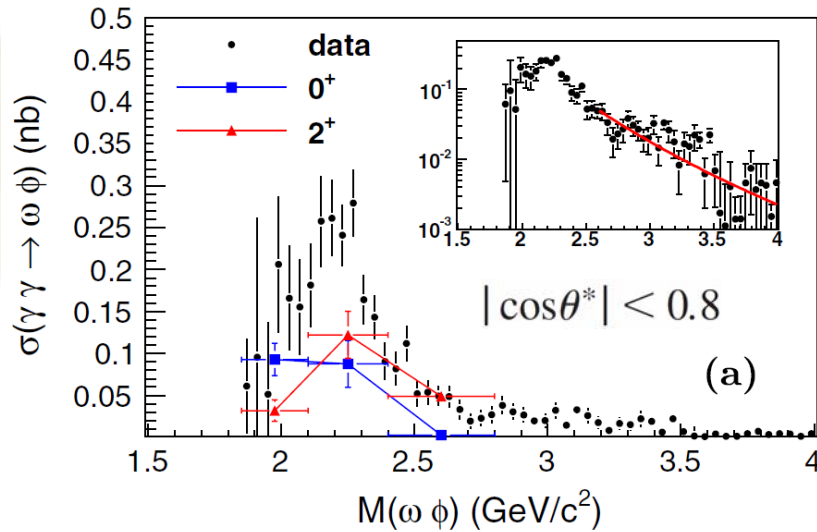


| Resonance    | $J^{PC}$ | $M(\text{MeV}/c^2)$ | $\Gamma(\text{MeV}/c^2)$ | Events        | $\Delta S$ | $\Delta ndf$ | Significance |
|--------------|----------|---------------------|--------------------------|---------------|------------|--------------|--------------|
| $X(1810)$    | $0^{++}$ | $1795 \pm 7$        | $95 \pm 10$              | $1319 \pm 52$ | 783        | 4            | $> 30\sigma$ |
| $f_2(1950)$  | $2^{++}$ | 1944                | 472                      | $665 \pm 40$  | 211        | 2            | $20.4\sigma$ |
| $f_0(2020)$  | $0^{++}$ | 1992                | 442                      | $715 \pm 45$  | 100        | 2            | $13.9\sigma$ |
| $\eta(2225)$ | $0^{-+}$ | 2226                | 185                      | $70 \pm 30$   | 23         | 2            | $6.4\sigma$  |
| phase space  | $0^{-+}$ | —                   | —                        | $319 \pm 24$  | 45         | 2            | $9.1\sigma$  |

# $\gamma\gamma \rightarrow \omega \omega, \phi\phi, \omega \phi$

PRL 108, 232001 (2012)

In order to search for possible structures in low mass region, we did  $\gamma\gamma \rightarrow VV$

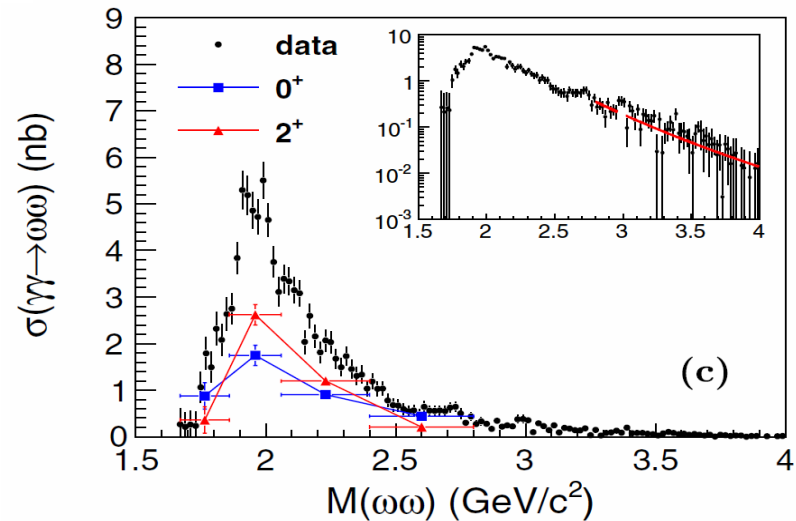


$$\sigma_{\gamma\gamma \rightarrow VV}(W_{\gamma\gamma}) = \frac{\Delta n}{\frac{dL_{\gamma\gamma}}{dW_{\gamma\gamma}} \epsilon(W_{\gamma\gamma}) \Delta W_{\gamma\gamma}}$$

$\frac{dL_{\gamma\gamma}}{dW_{\gamma\gamma}}$ : the differential luminosity  
 $\epsilon$ : efficiency

$\Delta W_{\gamma\gamma}$ : bin width

$\Delta n$ : the number of events in the  $\Delta W_{\gamma\gamma}$  bin.



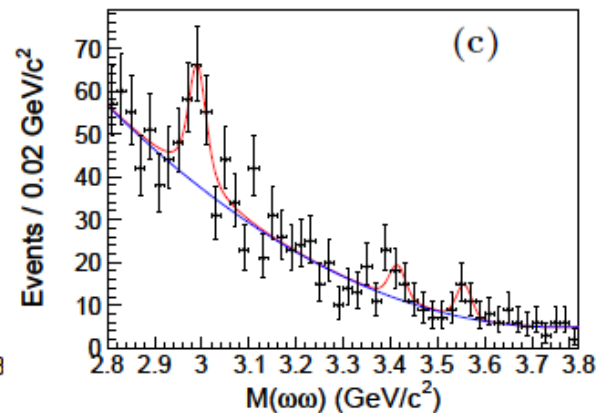
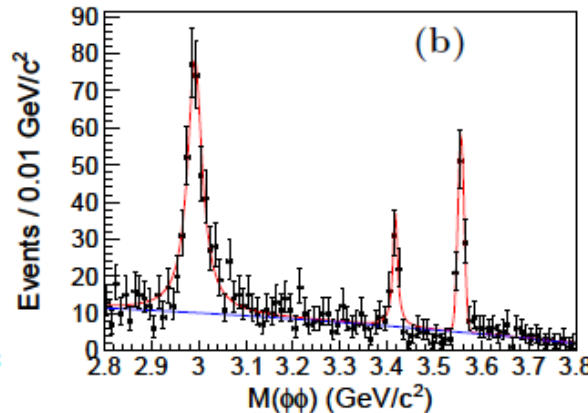
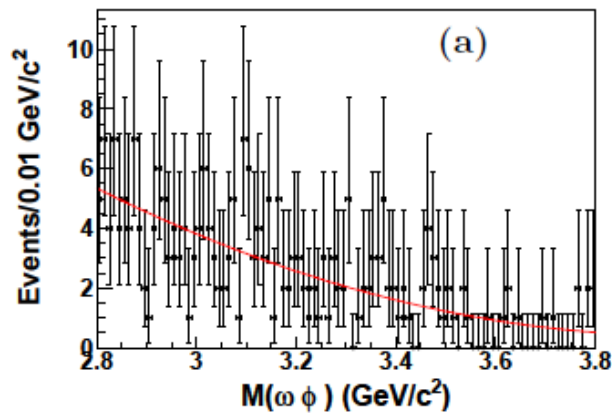
there are at least two different  $J^P$  components (J=0 and J=2)



$\Gamma_{\gamma\gamma} \mathcal{B}(X \rightarrow VV)$  (eV) for  $\eta_c$ ,  $\chi_{c0}$  and  $\chi_{c2}$ :

Fits: three incoherent BW  $\otimes$  double Gaussian + 2nd order Chebychev polynomial

PRL 108, 232001 (2012)



Results for  $\Gamma_{\gamma\gamma} \mathcal{B}(X \rightarrow VV)$  (eV) for  $\eta_c$ ,  $\chi_{c0}$  and  $\chi_{c2}$ .

The upper limits are obtained at the 90% confidence level.

| Mode        | $\omega\phi$ | $\phi\phi$               | $\omega\omega$           |
|-------------|--------------|--------------------------|--------------------------|
| $\eta_c$    | $< 0.49$     | $7.75 \pm 0.66 \pm 0.62$ | $8.67 \pm 2.86 \pm 0.96$ |
| $\chi_{c0}$ | $< 0.34$     | $1.72 \pm 0.33 \pm 0.14$ | $< 3.9$                  |
| $\chi_{c2}$ | $< 0.04$     | $0.62 \pm 0.07 \pm 0.05$ | $< 0.64$                 |

The measurements of  $\Gamma_{\gamma\gamma} \mathcal{B}(X \rightarrow \phi\phi)$  are consistent with results [Eur. Phys. J. C 53, 1 (2008)] with improved precision.

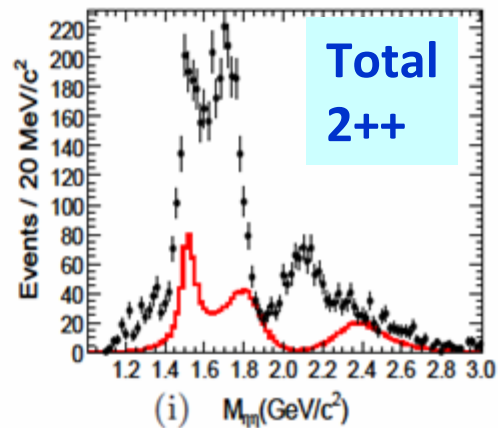
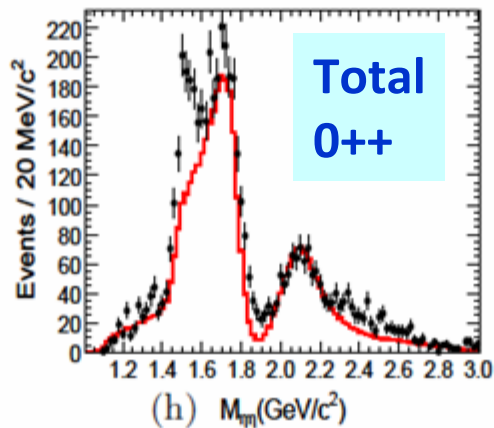
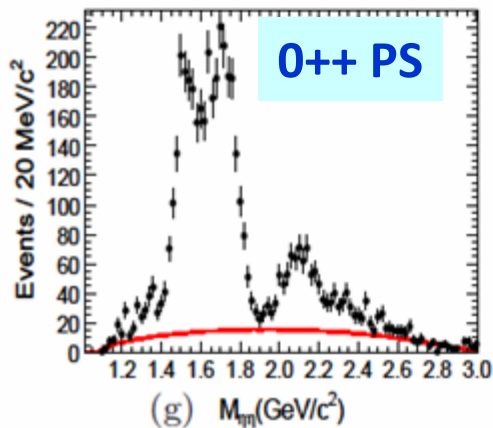
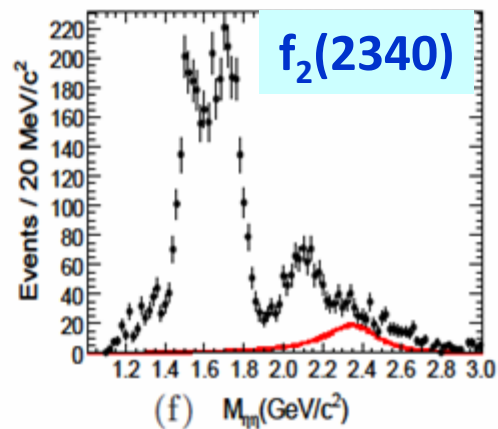
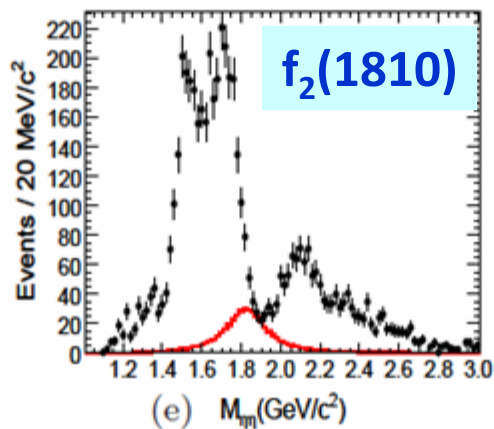
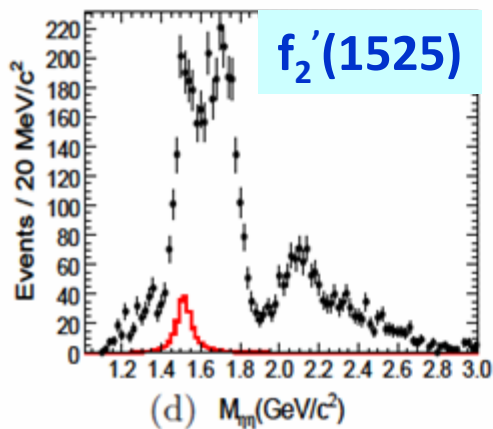
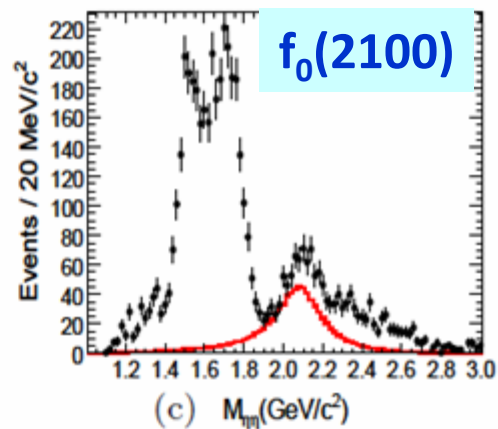
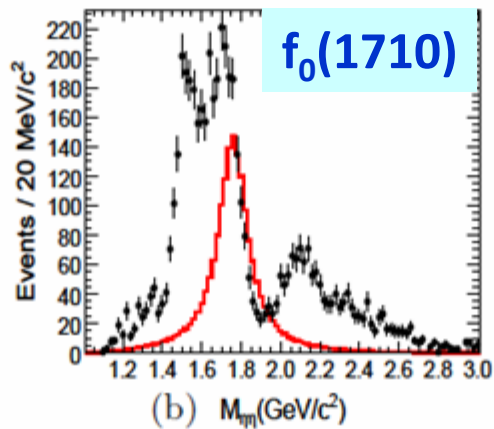
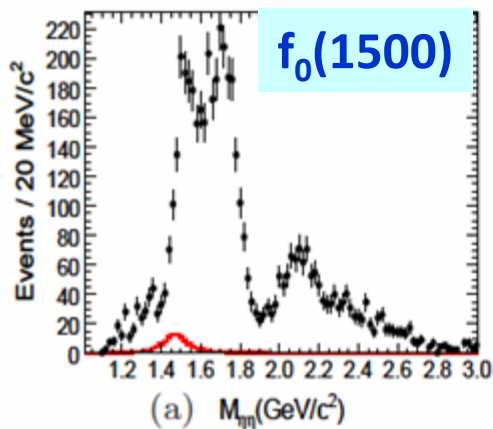
# Summary & Outlook

- Charmonium states provide a platform to study non-perturbative mechanism.
- Below the open-charm threshold: Spin-singlet states  $\eta_c$ ,  $h_c$ ,  $\eta_c(2S)$  have been measured
- Lots of discoveries, expected and unexpected
  - ↪  $X_{c_2}$  is assigned;  $X(3823)$  is consistent with  $y_2(1^3D_2)$
  - ↪ Are the X/Y states really new? Or the missing charmonium states  $X_{c_1}$ ? What's their nature?
- Future potential model, Lattice QCD, sum rules, novel method
- BESIII and future experiments, Panda, Belle II, have chance to establish not-yet-observed states.

- ❖ Many interesting states are observed:  
 $X(1835)(0^{-+})$ ,  $X(\omega \phi)(0^{++})$ , ...
- ❖ Some of them may be exotic states candidates.
- ❖ Where is lowest scalar/ pseudo-scalar glueball( $f_0(1500)$ ,  $f_0(1710)$ ,  $x(\omega \phi)$ ?...)
- ❖ Troubled by the possible mixing between glueball and  $q\bar{q}$ , it's hard to distinguish an exotic state from normal states.
- ❖ Amplitude analysis is needed to determine the property of these states.

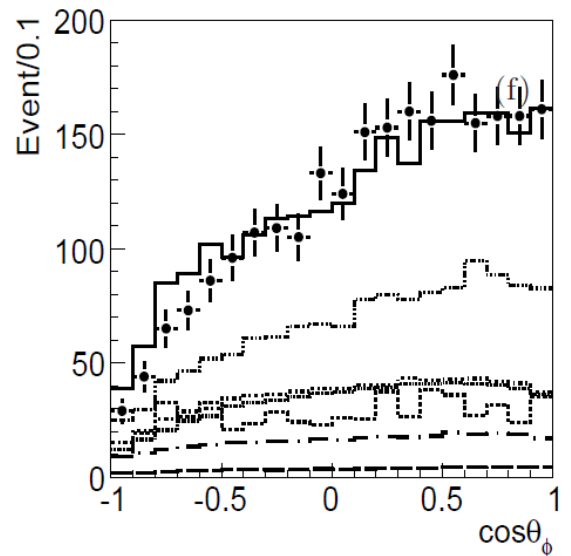
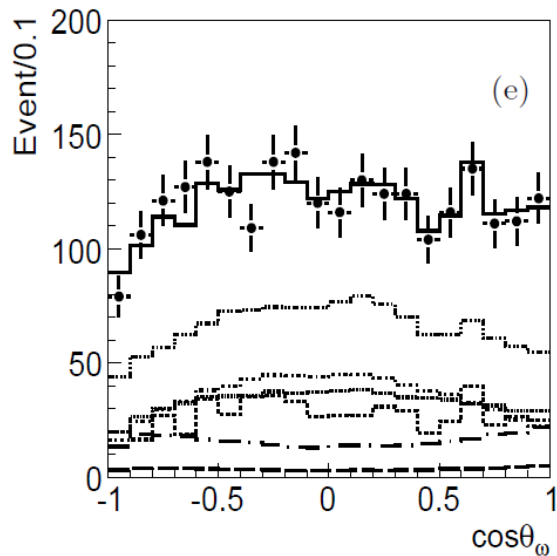
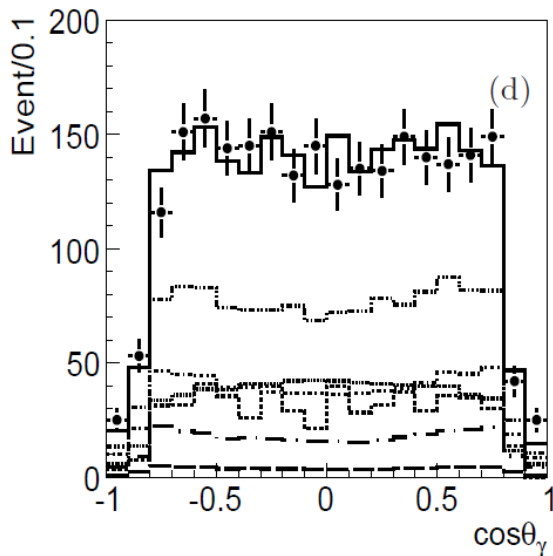
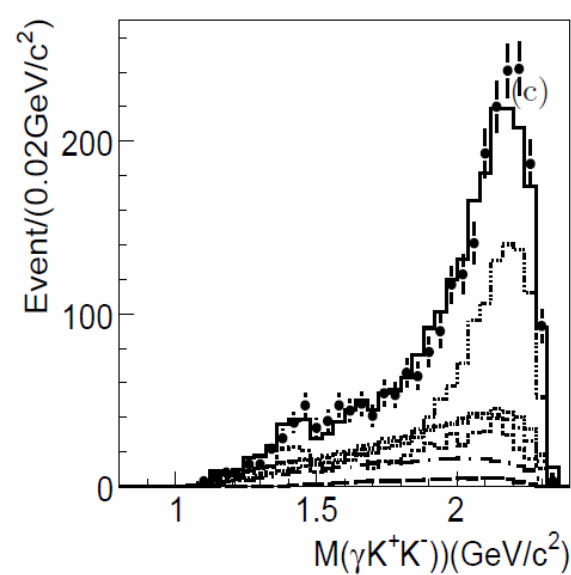
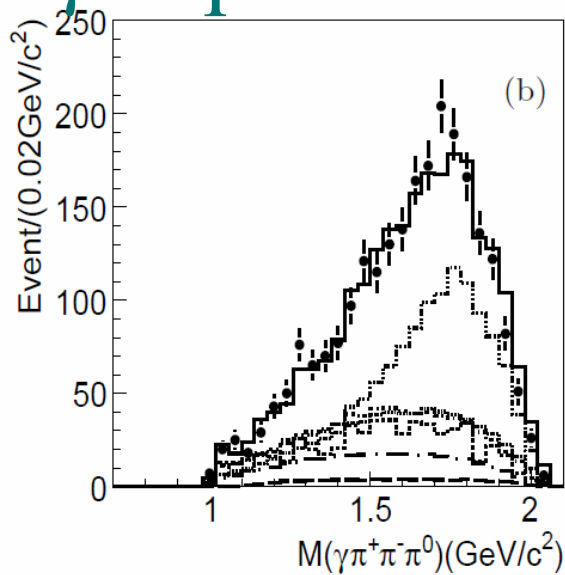
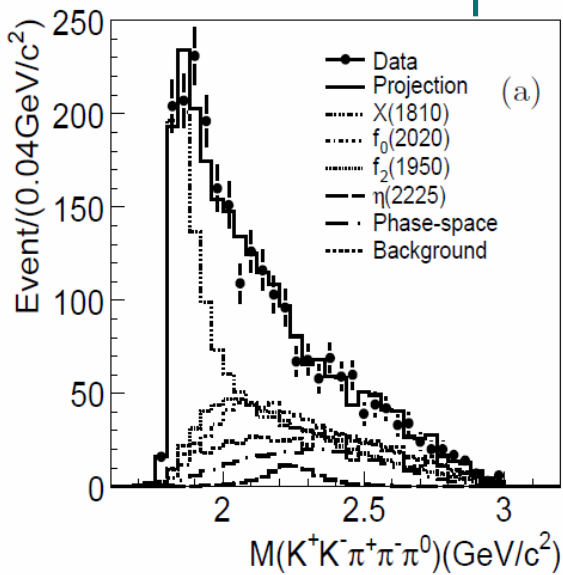
**Thanks!**







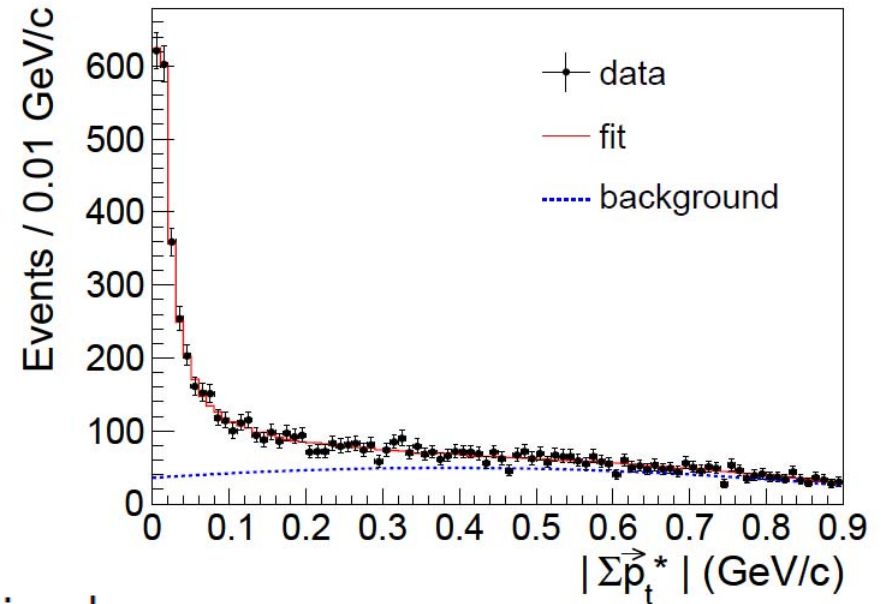
# PWA of $J/\psi \rightarrow \gamma \omega \phi$

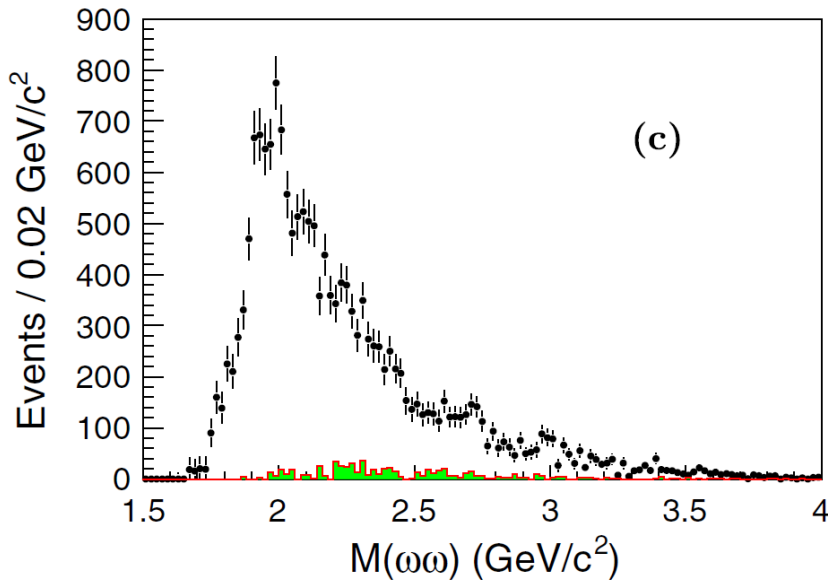
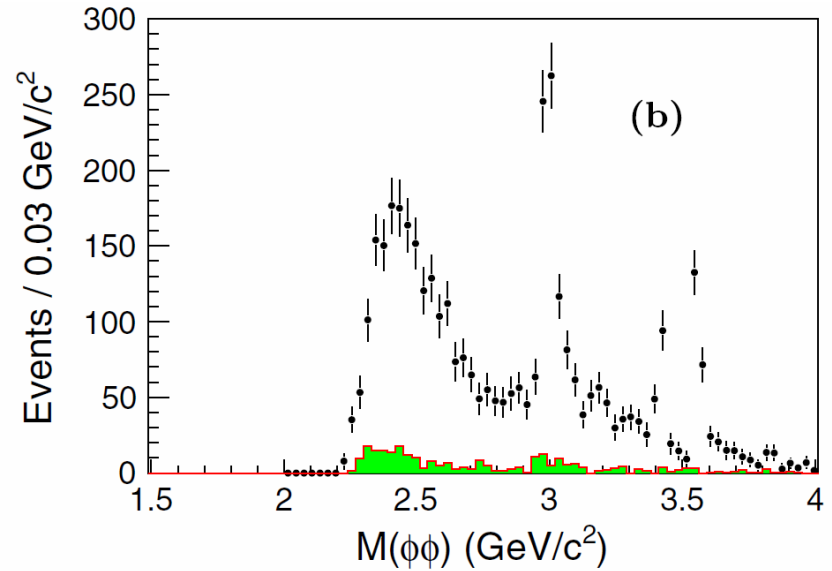
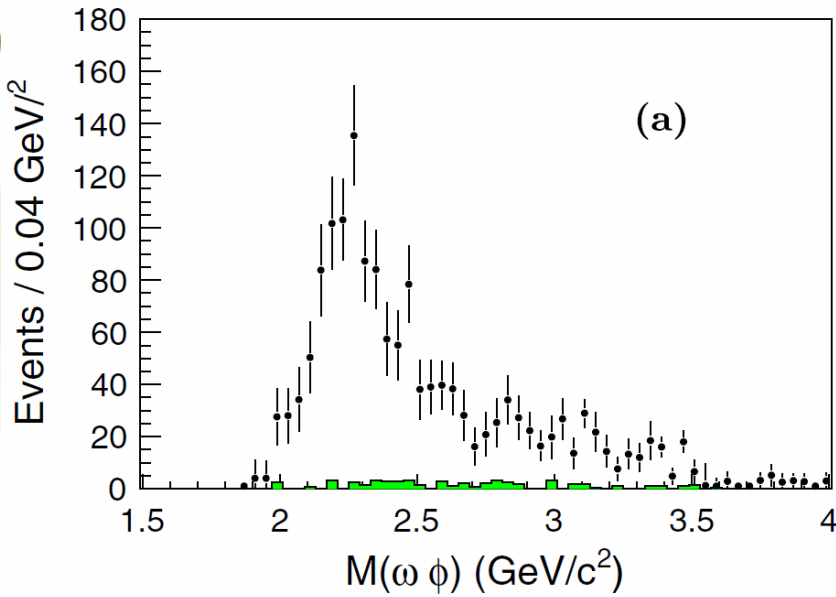


## $VV$ ( $V = \omega$ or $\phi$ ) invariant mass distributions:

$|\sum \vec{P}_t^*|$ : the magnitude of the vector sum of the final particles' transverse momenta in the  $e^+e^-$  C.M. frame.

$N(VV)$  in each  $VV$  mass bin is obtained by fitting the  $|\sum \vec{P}_t^*|$  distribution.  
Signal pdf: MC simulation  
Background pdf: 2nd Cheby. poly.





*The shaded histograms are from the corresponding normalized sidebands*

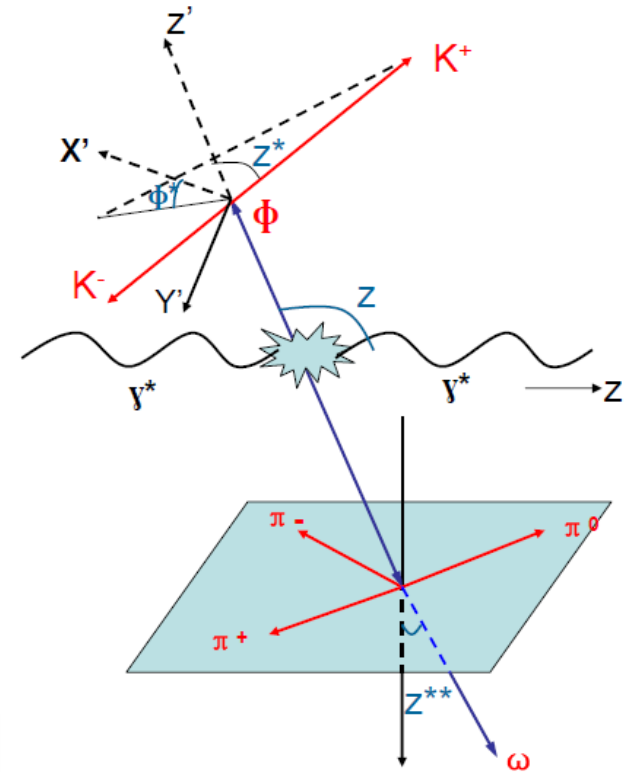
There are some obvious structures in the low VV invariant mass region. We did spin-parity analysis. 

# Spin-parity analysis:

For  $\gamma\gamma \rightarrow VV$ , five angles are kinematically independent:  $z$ ,  $z^*$ ,  $z^{**}$ ,  $\phi^*$ , and  $\phi^{**}$ .

Using  $\omega\phi$  as an example:

- $z$ : cosine of the scattering polar angle of  $\phi$  in the  $\gamma\gamma$  C.M. system;
- $z^*$  and  $\phi^*$ : the cosine of the helicity angle of  $K^+$  in the  $\phi$  rest frame and the azimuthal angle defined in the  $\phi$  rest frame with respect to the  $\gamma\gamma \rightarrow \omega\phi$  scattering plane;
- $z^{**}$  and  $\phi^{**}$ : the cosine of the helicity angle of normal direction to the decay plane of the  $\omega \rightarrow \pi^+\pi^-\pi^0$  and the azimuthal angle defined in the  $\omega$  rest frame.



**transversity angle ( $\phi_T$ ):**  $\phi_T = |\phi^* + \phi^{**}|/2\pi$

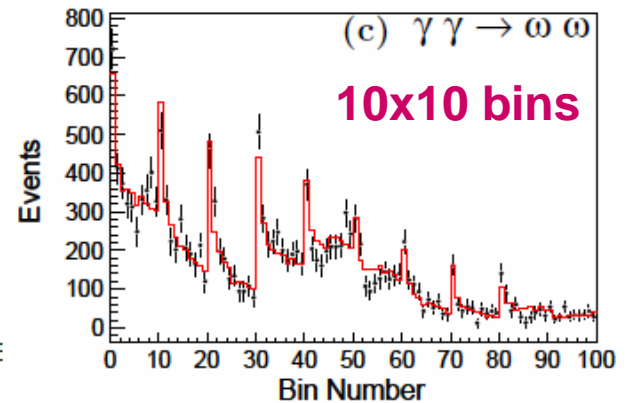
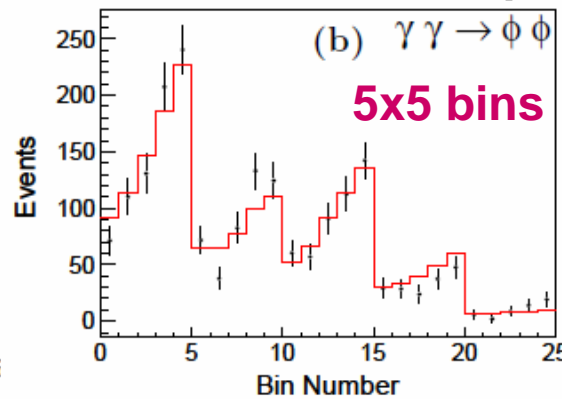
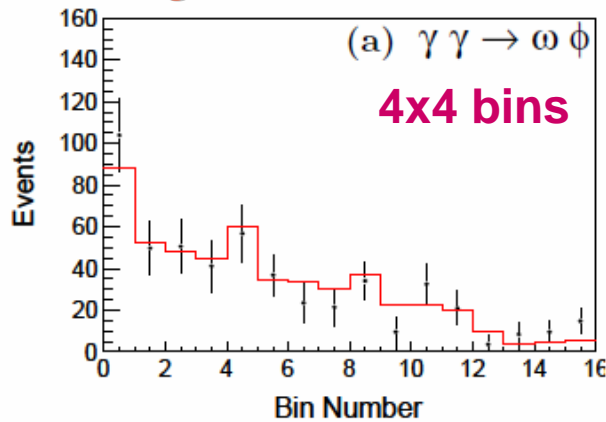
**polar-angle product ( $\Pi_\theta$ ):**  $\Pi_\theta = [1 - (z^*)^2][1 - (z^{**})^2]$

$N_{event}$  is obtained by fitting the  $|\sum \vec{P}_t^*|$  distribution in each  $\phi_T$  and  $\Pi_\theta$  bin in the 2D space.

# The number of event projections in the 2D space of the transversity angle and polar-angle product

$M(VV) < 2.8 \text{ GeV}/c^2$

**Histograms:** the best fits with different  $J^P$  components



- for  $\omega\phi$ : a mixture of  $0^+$  ( $S$ -wave) and  $2^+$  ( $S$ -wave) describes data with  $\chi^2/ndf = 0.9$  ( $ndf$  is the number of degrees of freedom)
- for  $\phi\phi$ : a mixture of  $0^+$  ( $S$ -wave) and  $2^-$  ( $P$ -wave) describes data with  $\chi^2/ndf = 1.3$
- for  $\omega\omega$ : a mixture of  $0^+$  ( $S$ -wave) and  $2^+$  ( $S$ -wave) describes data with  $\chi^2/ndf = 1.3$