

# Review of $h_c$ , $\eta_c$ and $\eta_c(2S)$

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*BESIII*  
*05-14-2012*

CHARM2012, Hawaii

# Introduction: Importance and Challenges of Charmonium

- **Great Lab for precision tests of quark mode**
- **Mysteries, e.g., “ $\rho\pi$  puzzle”**
- **$h_c, \eta_c, \eta_c(2S)$** 
  - **Predicted after  $J/\psi$  discovery**
  - **Technically challenging: statistic, low energy photon detection, interference, EM hinder effects...**
  - **Observed through various processes, but properties need to be understood**

## **In this talk:**

**$h_c$  – mostly recently discovered charmonium state**

– **new measurements of production and properties**

**$\eta_c$  – mass, width, distorted lineshape**

**$\eta_c(2S)$  – observed in charmonium transitions at last!**

# Experimental Approaches

**BESIII, CLEO-c:**

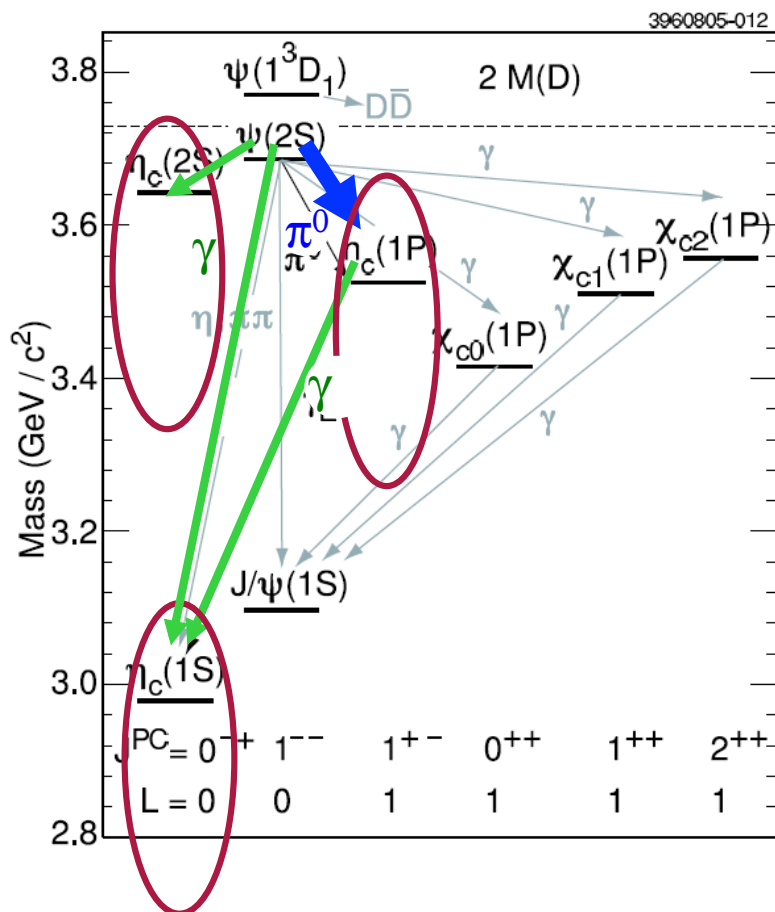
From  $\psi'$  decays and  $e^+e^-$  annihilation near  $D\bar{D}$  threshold

→ very clean and simple environment

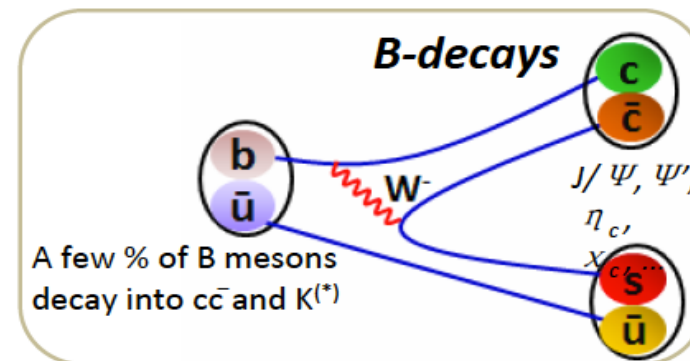
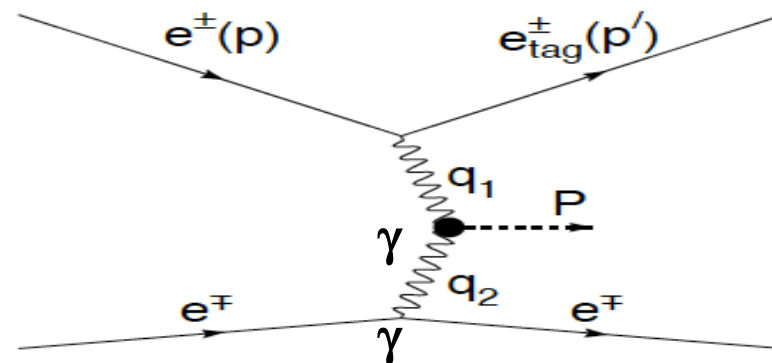
**BaBar, Belle:**

From  $\gamma\gamma$  and  $B$  decay

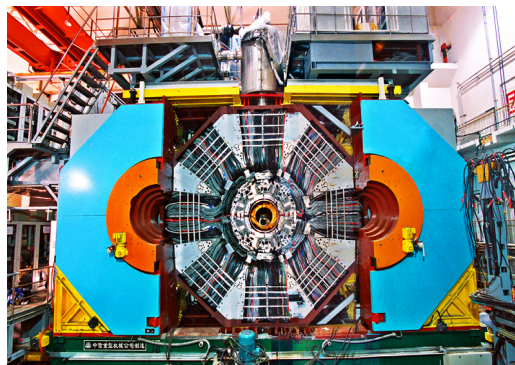
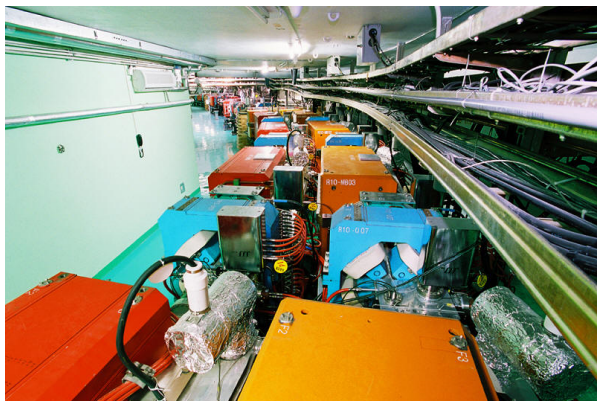
→ large production rate.



**Two-Photon process**



# BEPCII/BESIII



**BESIII Detector**

## BEPCII

- Beam energy:  
 $\sqrt{s}=2.0 - 4.6 \text{ GeV}$
- Optimum energy:  
 $\sqrt{s}= 3.7 \text{ GeV}$
- Beam crossing  
angle: 22 mrad
- Designed luminosity:  $1.0 \times 10^{33}$
- Record  
luminosity  $0.57 \times 10^{33}$
- Energy spread:  $5.16 \times 10^{-4}$

He-based drift chamber:

$\delta p/p=0.58\%$ ,  
 $dE/dx \sim 6\% @ 1 \text{ GeV}$

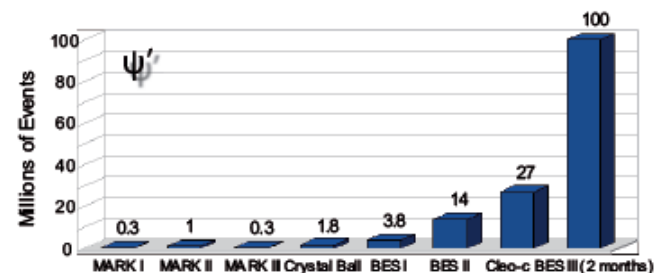
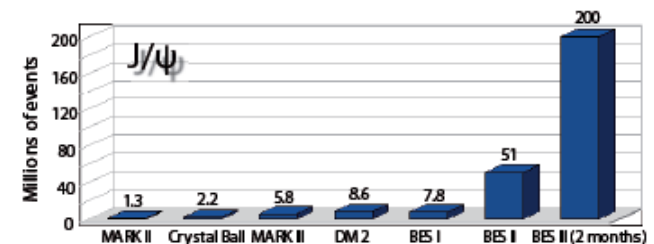
CsI EM calorimeter:  
 $\delta E \sim 2.5\%$ ,

TOF: 80 ps (barrel), 100 ps (endcap)

1T Superconducting magnet

Muon system :

9 layers of RPC



**Large luminosity**

**BESIII has a comparable detector to CLEO-c with a much larger luminosity.**

# $h_c(^1P_1)$

- Spin singlet  $P$  wave ( $S=0, L=1$ )
- Potential model: if non-zero  $P$ -wave spin-spin interaction,

$$\Delta M_{\text{hf}}(1P) = M(h_c) - \langle m(1^3P_J) \rangle \neq 0$$

$$\text{where } \langle m(1^3P_J) \rangle = [(M(\chi_{c0}) + 3M(\chi_{c1}) + 5M(\chi_{c2}))]/9,$$

- CLEO-c 1<sup>st</sup> observed  $h_c$  in  $e^+e^- \rightarrow \psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c$

$$\Delta M_{\text{hf}}(1P) = 0.08 \pm 0.18 \pm 0.12 \text{ MeV}/c^2$$

*Consistent with 1P hyperfine splitting = 0.*

## Theoretical predictions:

$$BF(\psi(2S) \rightarrow \pi^0 h_c) = (0.4-1.3) \times 10^{-4}$$

$$BF(h_c \rightarrow \gamma \eta_c) = 48\% \text{ (NRQCD)}$$

$$BF(h_c \rightarrow \gamma \eta_c) = 88\% \text{ (PQCD)}$$

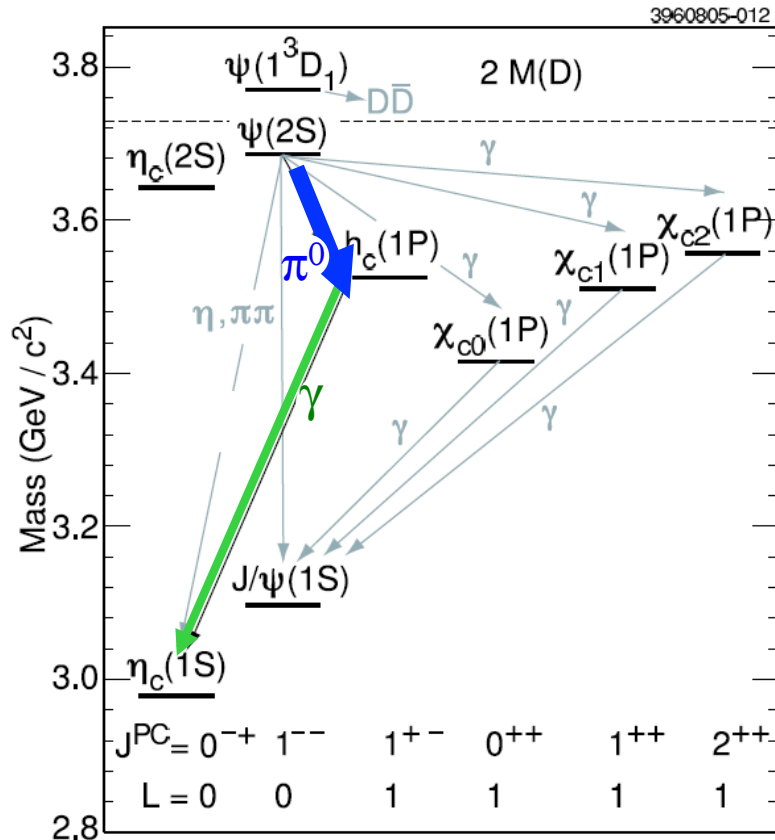
*Kuang, PR D65 094024 (2002)*

$$BF(h_c \rightarrow \gamma \eta_c) = 38\%$$

*Godfrey and Rosner, PR D66 014012(2002)*

*Different theoretical approaches give a wide range of predictions and that we've been waiting for experiment to resolve it.*

# Methods for studying the $h_c$ in $\psi'$ decays



Only detect the  $\pi^0 \rightarrow$  “inclusive”  
(compute  $M_{h_c}$  from kinematics)

$$Rate \propto Bf(\psi' \rightarrow \pi^0 h_c)$$

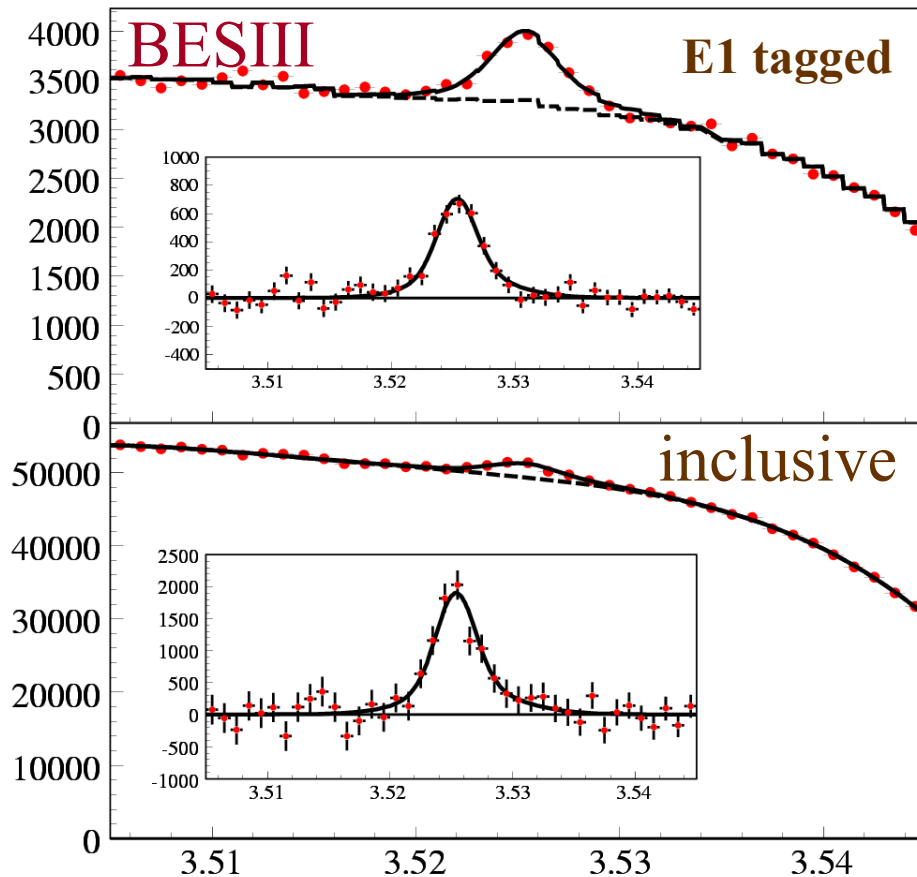
Detect the  $\pi^0$  &  $\gamma \rightarrow$  “ $E_1$ -tagged”  
(compute  $M_{h_c}$  from kinematics)

$$Rate \propto Bf(\psi' \rightarrow \pi^0 h_c) \times Bf(h_c \rightarrow \gamma \eta_c)$$

Detect the  $\pi^0$ ,  $\gamma$  & all  $\eta_c \rightarrow X_i$  decay  
products  $\rightarrow$  “exclusive”  
(compute  $M_{h_c}$  from 4-C kinematic fit)

$$Rate \propto Bf(\psi' \rightarrow \pi^0 h_c) \times Bf(h_c \rightarrow \gamma \eta_c) \times Bf(\eta_c \rightarrow X_i)$$

# $\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c$ at BESIII



**BESIII: 106M  $\psi'$  :**

**PRL 104 132002 (2010)**

Mass =  **$3525.40 \pm 0.13 \pm 0.18$  MeV/c<sup>2</sup>**

Width =  **$0.73 \pm 0.45 \pm 0.28$  MeV**

**$<1.44$  MeV @90%**

CLEO-c: PRL 101 182003 (2008)

Mass =  **$3525.28 \pm 0.19 \pm 0.12$  MeV**

Width: fixed at 0.9 MeV

Hyperfine mass splitting

$$\Delta M_{\text{hf}}(1^1\text{P}) = M(h_c) - \langle m(1^3\text{P}_J) \rangle$$

BESIII:  **$0.10 \pm 0.13 \pm 0.18$  MeV/c<sup>2</sup>**

CLEO-c:  **$0.02 \pm 0.19 \pm 0.13$  MeV/c<sup>2</sup>**

By combining inclusive results with E1-photon tagged results

$$BF(\psi' \rightarrow \pi^0 h_c) = (8.4 \pm 1.3 \pm 1.0) \times 10^{-4}$$

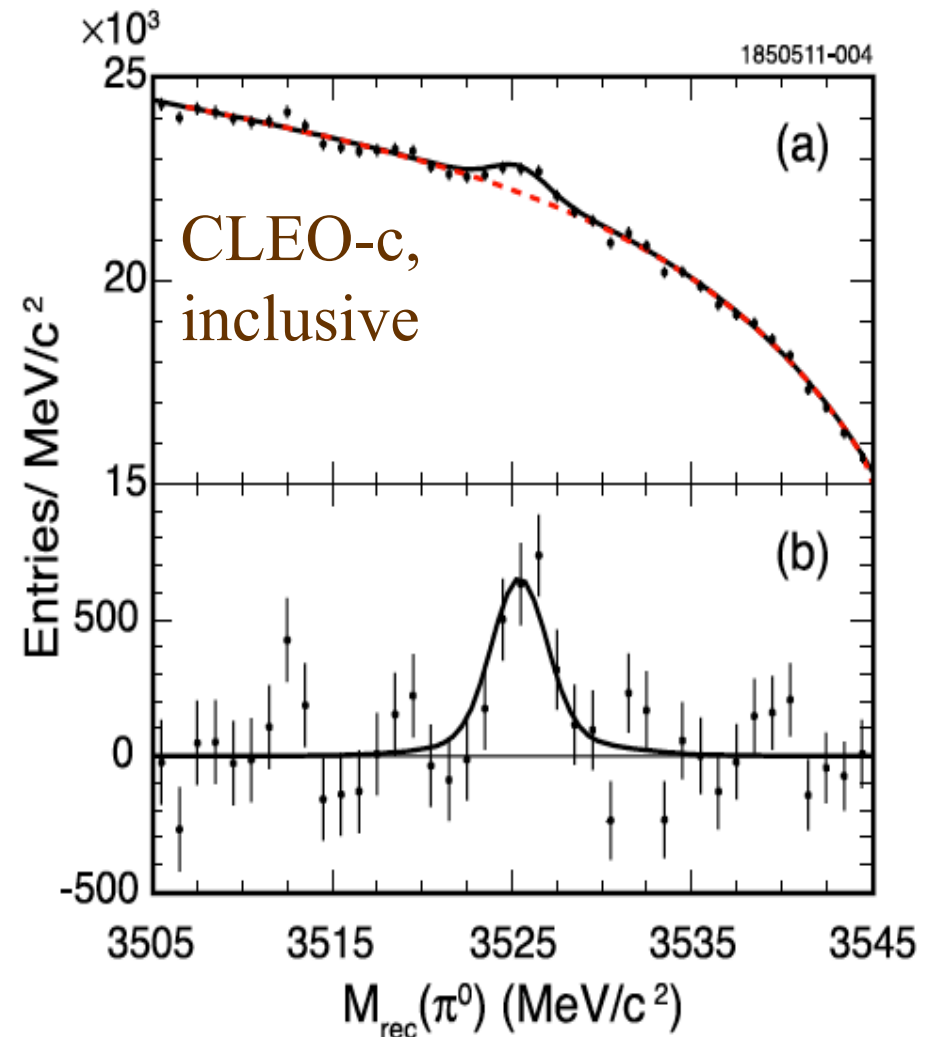
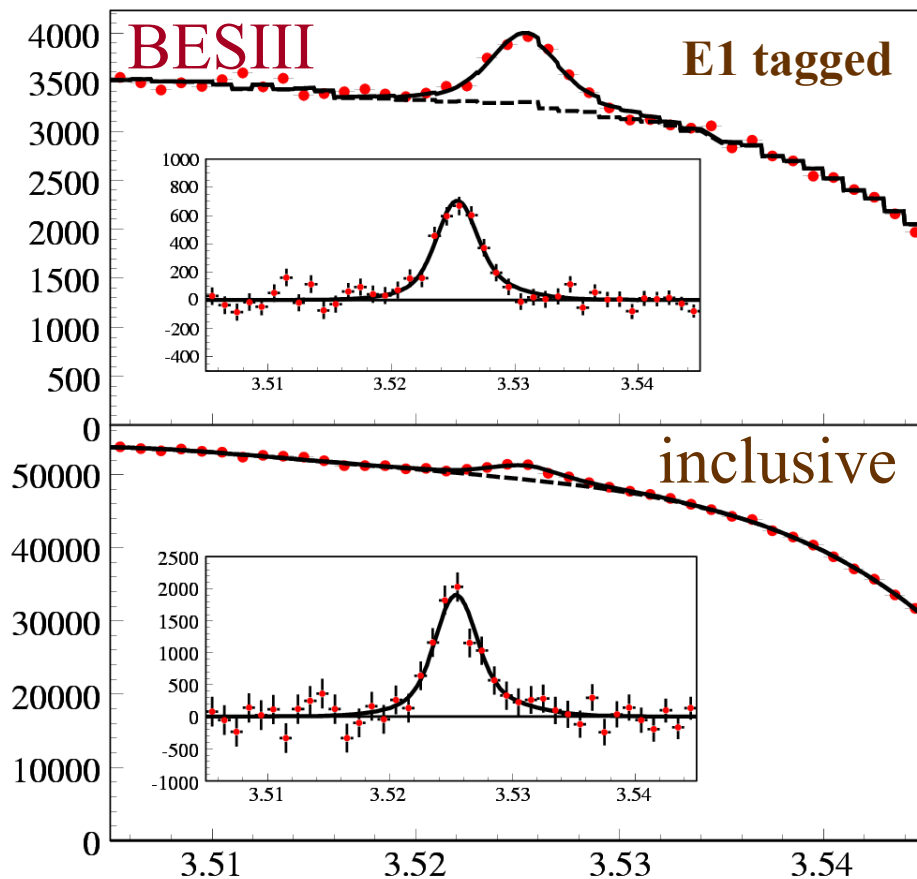
$$BF(h_c \rightarrow \gamma \eta_c) = (54.3 \pm 6.7 \pm 5.2)\%$$

**Make it possible to extract absolute  $h_c$  cross sections.**

Agrees with prediction from Kuang,

Godfrey, Dude et al.

# Inclusive $\psi' \rightarrow \pi^0 h_c$ at CLEO-c



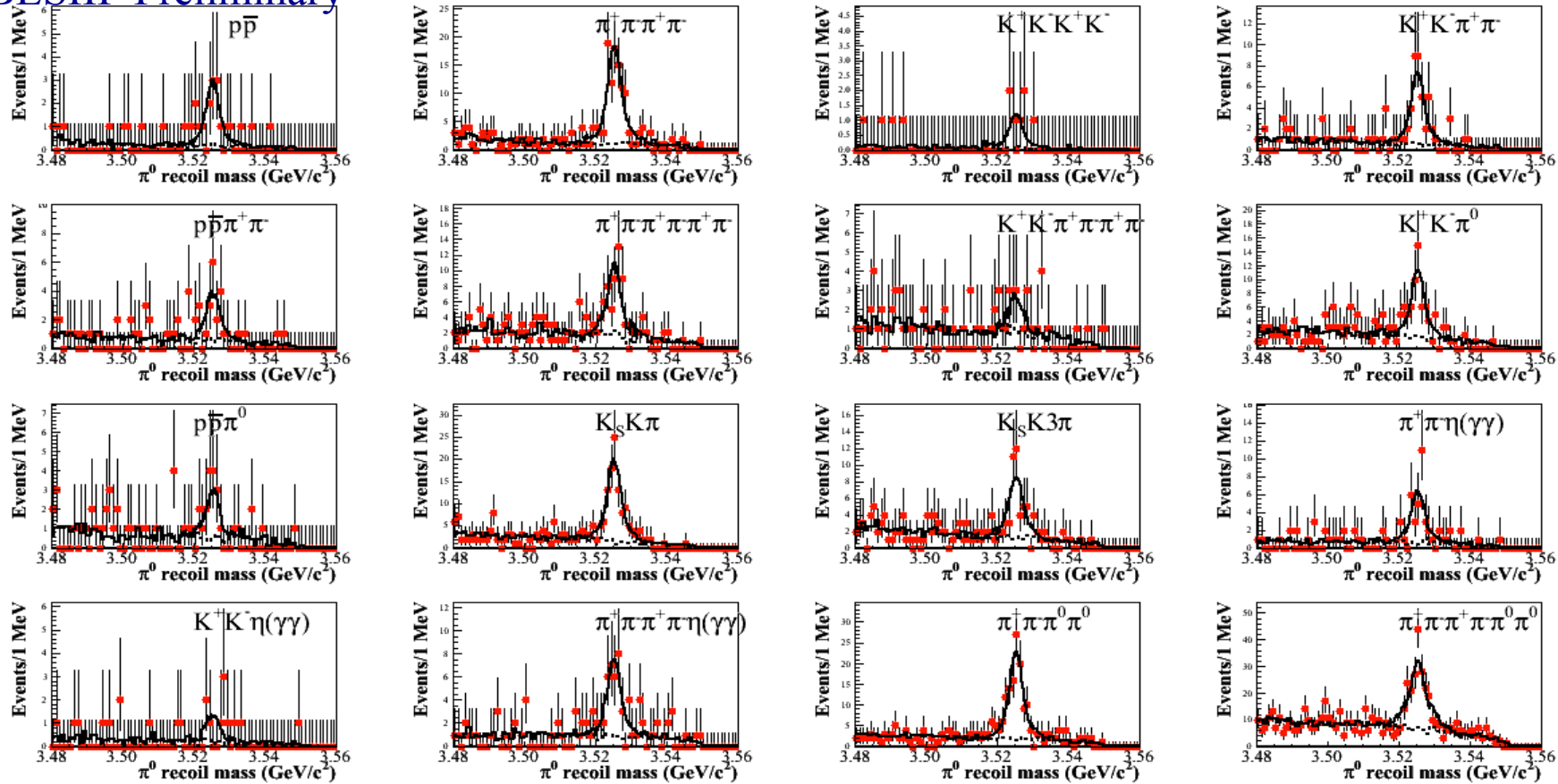
*BESIII's result has been confirmed by CLEO-c*

$$BF(\psi' \rightarrow \pi^0 h_c) = (9.0 \pm 1.5 \pm 1.3) \times 10^{-4} \text{ Phys.Rev. D84 (2011) 032008}$$



# $\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c$ exclusive decays at BESIII

BESIII Preliminary



16 different  $\eta_c$  decay channels

Simultaneous fit to  $\pi^0$  recoiling mass  
 $\chi^2/\text{d.o.f.} = 32/46$

Mass =  $3525.31 \pm 0.11 \pm 0.15 \text{ MeV}/c^2$

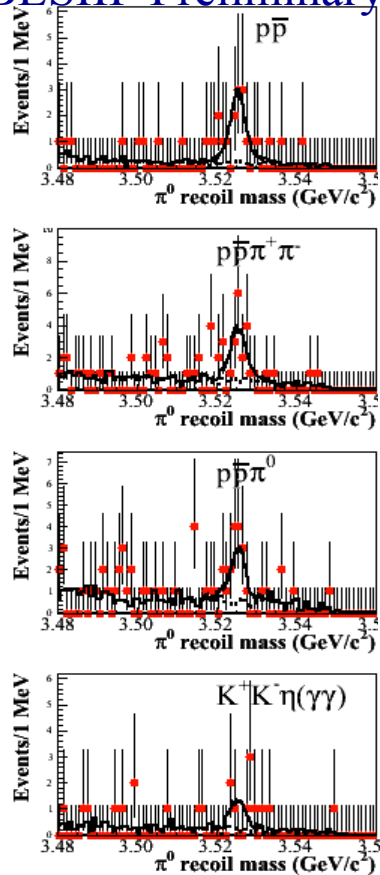
Width =  $0.70 \pm 0.28 \pm 0.25 \text{ MeV}$

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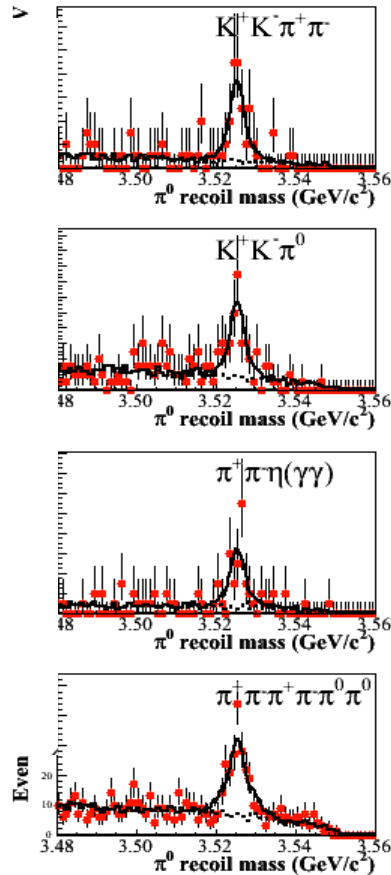
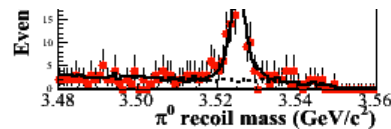
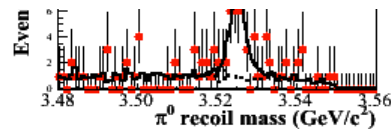
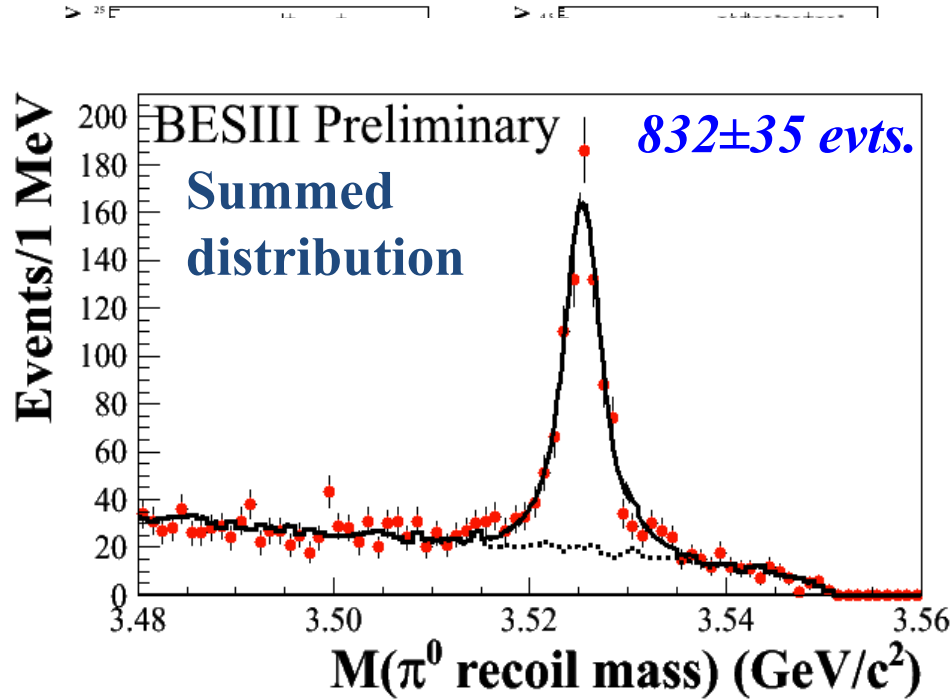
} consistent with BESIII  $E_1$ -tagged results

# $\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c, \eta_c$ exclusive decays at BESIII

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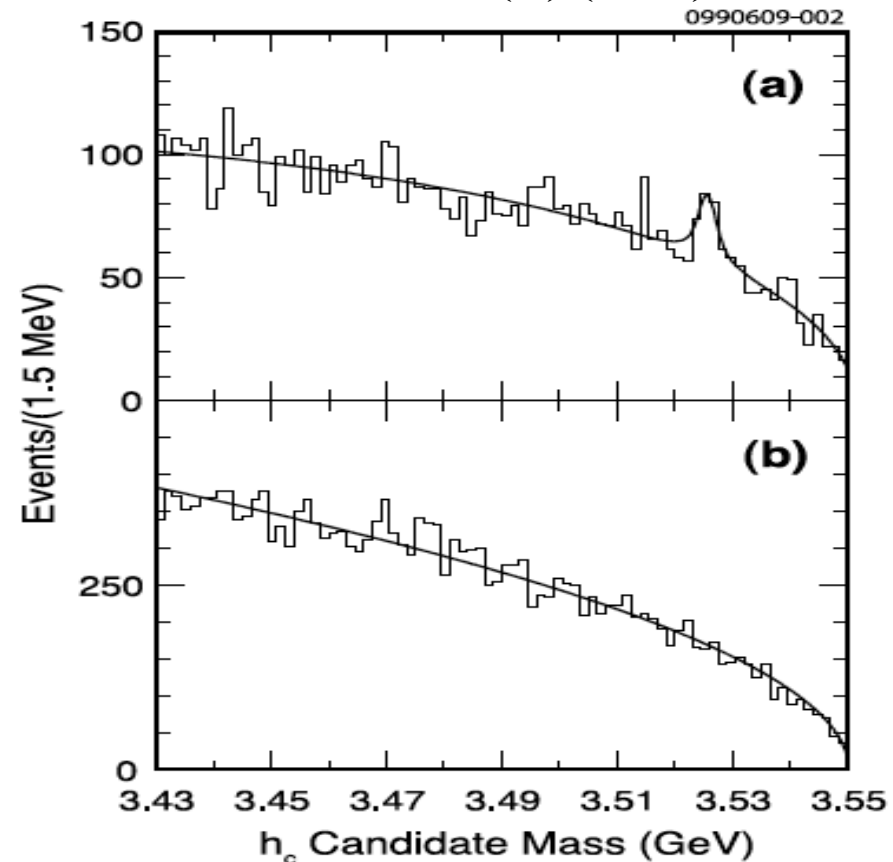
# $h_c$ hadronic decays at CLEO-c

Because the  $\text{Br}(h_c \rightarrow \gamma \eta_c) = (54.3 \pm 8.5)\%$  (BESIII), the remaining hadronic decays should be large enough to be observed. CLEO-c has searched for odd pion decays and found the evidence of  $h_c \rightarrow 2(\pi^+ \pi) \pi^0$ .

$$\begin{aligned} & \text{B}(\psi' \rightarrow \pi^0 h_c) \times \text{Br}(h_c \rightarrow 2(\pi^+ \pi) \pi^0) \\ & = 1.88_{-0.45}^{+0.48} \text{ (stat.) }_{-0.30}^{+0.47} \text{ (syst.)} \times 10^{-5} \\ & \text{Yield: } 92_{-0.22}^{+23} \\ & \text{Significance: } 4.4\sigma \end{aligned}$$

The main part of the remaining 45% hadronic decays is still unclear...

PRD80, 051106(R) (2009)



Invariant mass plots for  $h_c \rightarrow 2(\pi^+ \pi) \pi^0$ . for (a) data, and (b) non- $h_c$  MC events.

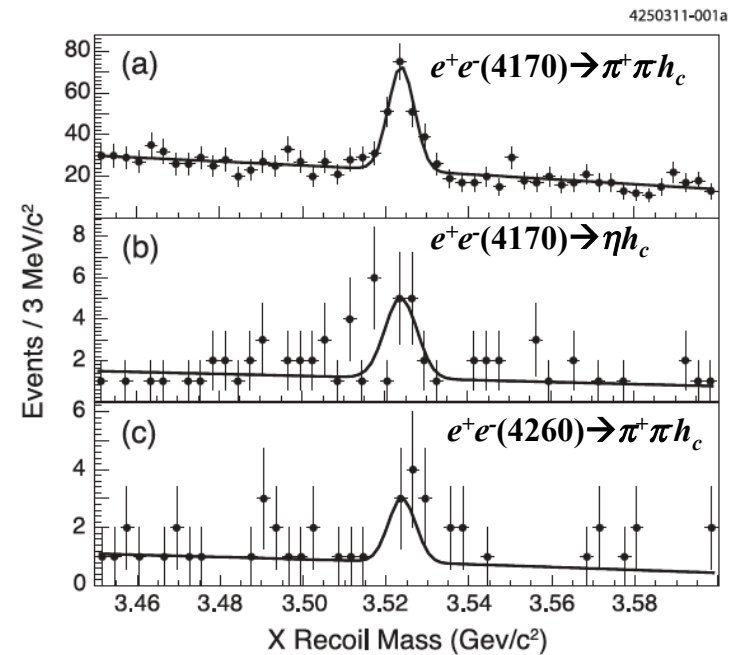
# New $h_c$ production mode found at CLEO-c

CLEO-c has discovered a prolific new source ( $\sim 10\sigma$ ) of  $h_c$  from  $e^+e^-$  annihilation at  $\sqrt{s}=4170\text{MeV}$ :

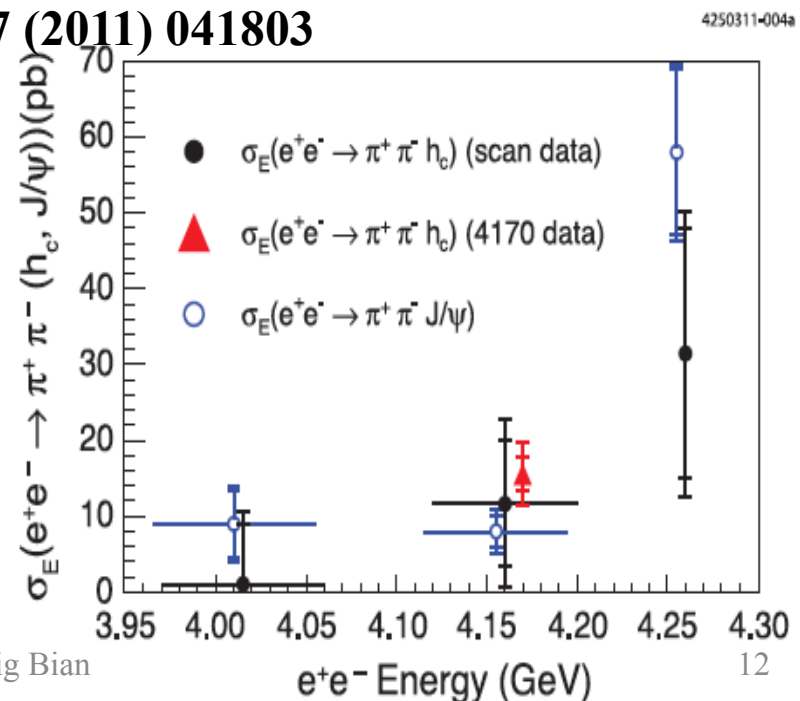
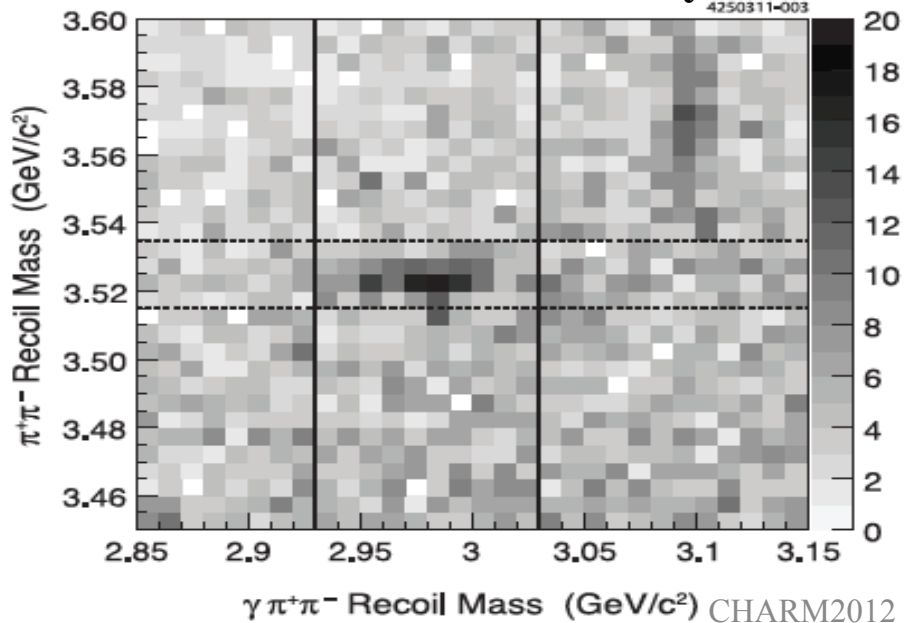
$$e^+e^-(4170) \rightarrow \pi^+\pi^-h_c(1P)$$

with  $h_c \rightarrow \gamma\eta_c$ ,  $\eta_c \rightarrow 12$  decay modes.

This discovery of the population of  $h_c$  in  $e^+e^-$  annihilations above the DD threshold of charmonium has led the Belle collaboration to search for  $h_b(1P, 2P)$  in  $e^+e^-$  annihilations at  $\sqrt{s} = 10.685$  GeV using the same technique.



Phys.Rev.Lett. 107 (2011) 041803



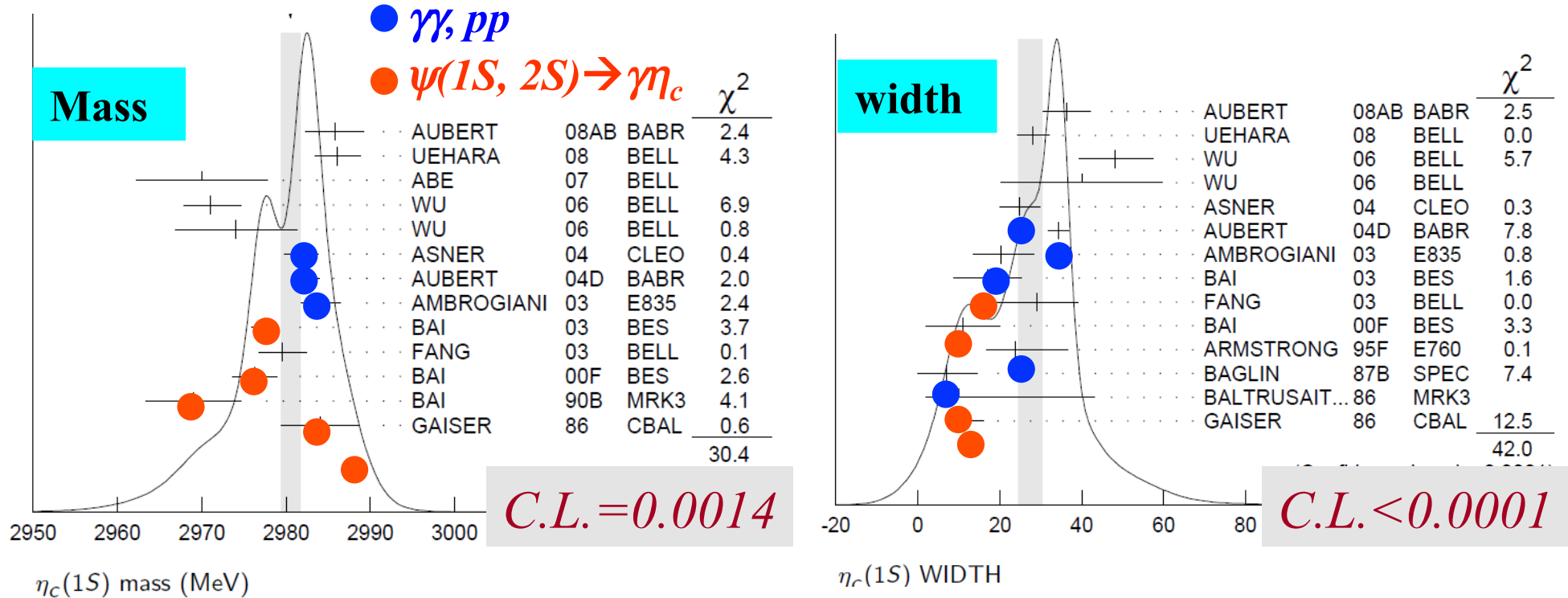
# $\eta_c(1S)$

- The lowest lying S-wave spin singlet charmonium, discovered in 1980 by MarkII

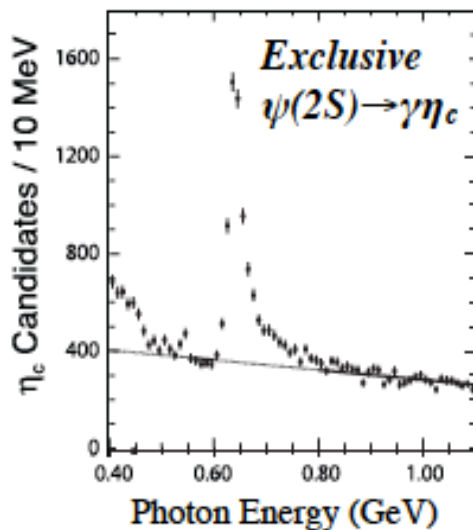
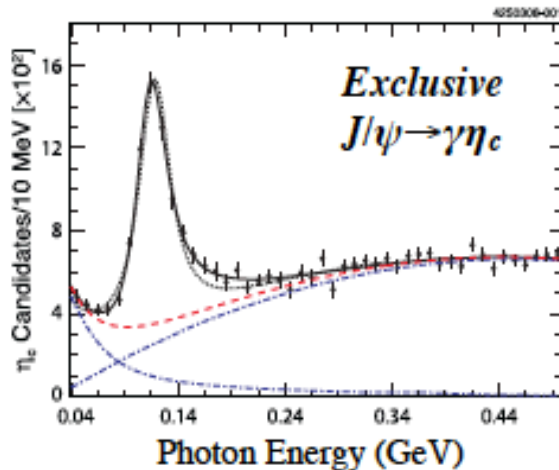
- Parameters:

$J/\psi, \psi'$  radiative transition:  $M \sim 2978.0 \text{ MeV}/c^2$ ,  $\Gamma \sim 10 \text{ MeV}$

$\gamma\gamma$  process:  $M = 2983.1 \pm 1.0 \text{ MeV}/c^2$ ,  $\Gamma = 31.3 \pm 1.9 \text{ MeV}$

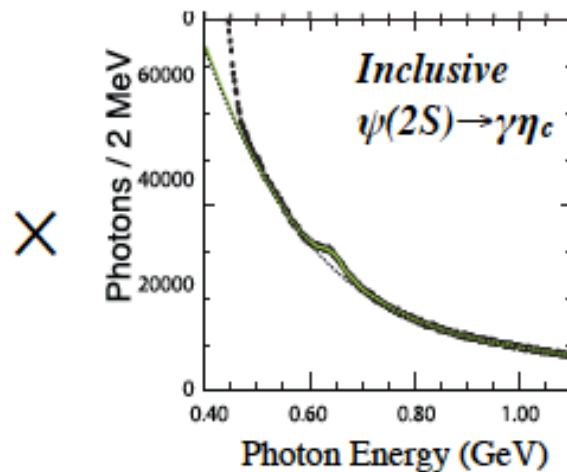


# $\psi' \rightarrow \gamma \eta_c, \eta_c \rightarrow$ exclusive decays at CLEO-c



## Three Measurements of M1 Transitions:

- A.  $B(\psi(2S) \rightarrow \gamma \eta_c) = (4.32 \pm 0.16 \pm 0.60) \times 10^{-3}$  from inclusive  $\eta_c$  decays.
- B.  $B(J/\psi \rightarrow \gamma \eta_c) / B(\psi(2S) \rightarrow \gamma \eta_c)$  using exclusive  $\eta_c$  decays.
- C.  $B(J/\psi \rightarrow \gamma \eta_c) = (1.98 \pm 0.09 \pm 0.30) \%$  taking  $A \times B$ .



*Slide from Ryan Mitchell*

$$\times = B(J/\psi \rightarrow \gamma \eta_c)$$

PRL 106, 159903

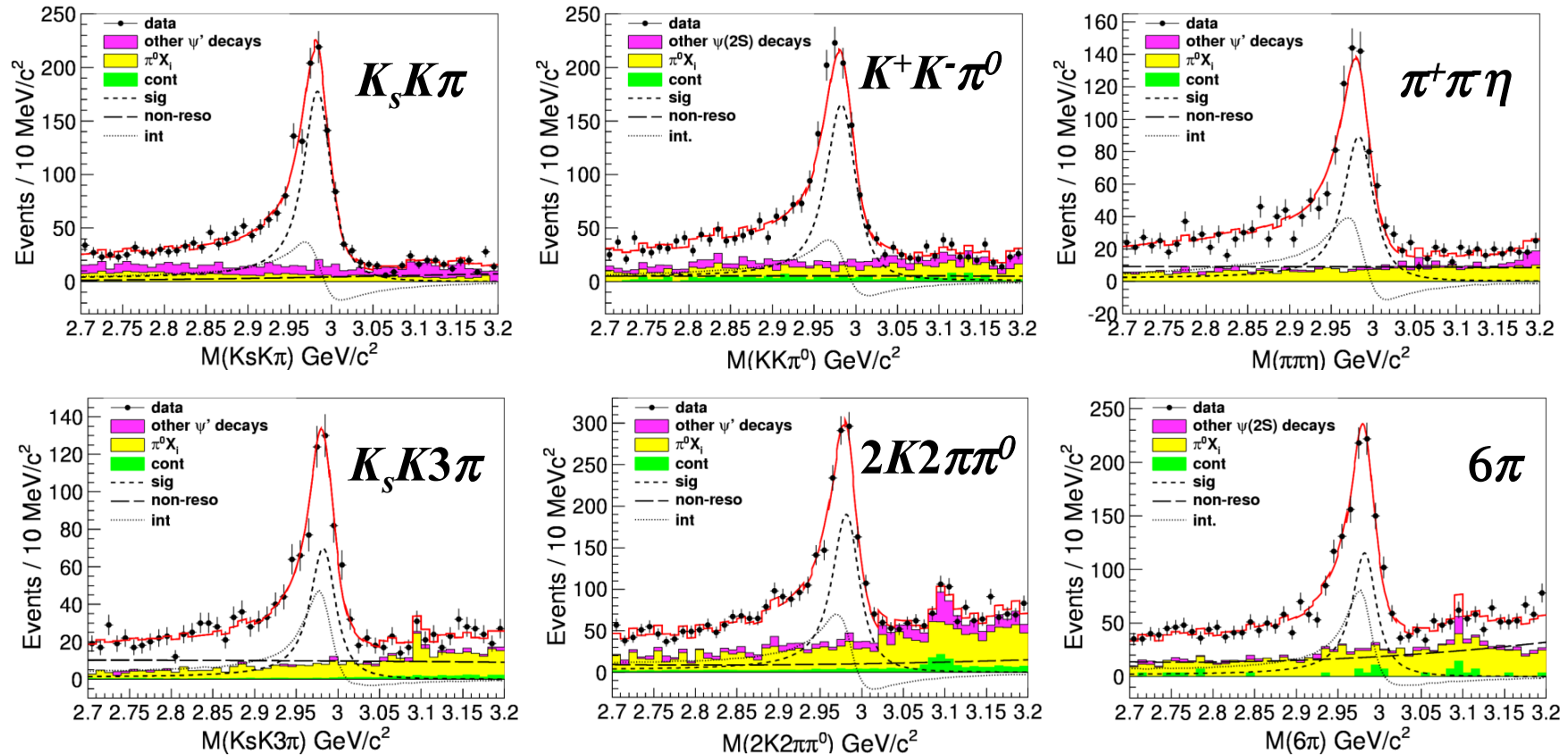
- One “surprise” was the non-trivial line-shape of the  $\eta_c$ .
- Recent Lattice QCD Results (Dudek et al, PRD73,07450(2006)) predict  $\Gamma_{\gamma \eta_c} = (2.0 \pm 0.1 \pm 0.4) \text{ keV}$   
 $\Rightarrow B(J/\psi \rightarrow \gamma \eta_c) = (2.1 \pm 0.1 \pm 0.4) \%$

*The experimental value of  $B(J/\psi \rightarrow \gamma \eta_c)$  is now in line with theoretical expectations.*

*The distortion of the  $\eta_c$  line shape in  $\psi'$  decays inspires BESIII's  $\eta_c$  study.*

# $\psi' \rightarrow \eta_c, \eta_c \rightarrow$ exclusive decays at BESIII

*interference with non-resonant background is significant!!*



$$M: 2984.4 \pm 0.5 \pm 0.6 \text{ MeV}$$

$$\Gamma: 30.5 \pm 1.0 \pm 0.9 \text{ MeV}$$

$$\phi: 2.35 \pm 0.05 \pm 0.04 \text{ rad}$$

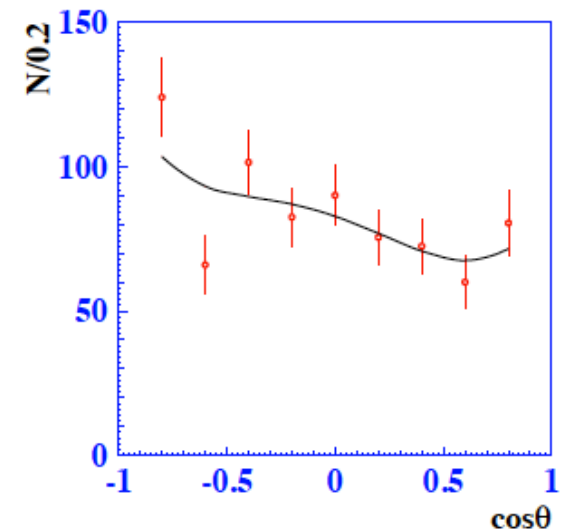
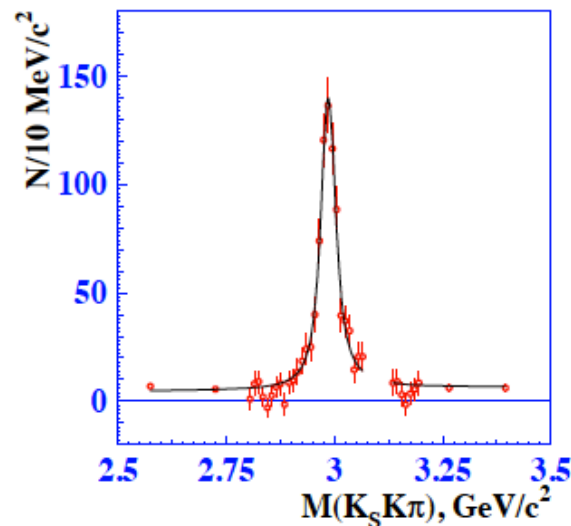
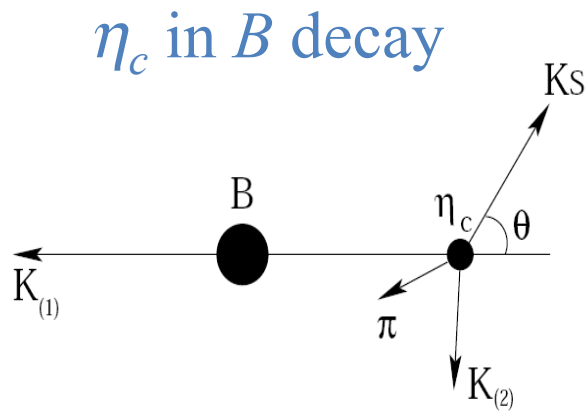
*Relative phase  $\phi$  values from each mode are consistent within  $3\sigma$ ,*

*→ use a common phase value in the simultaneous fit.*

BESIII arXiv:1111:0398  
accepted by PRL

# New mass and width measurement for $\eta_c$ in $B$ decays at Belle

$B^+ \rightarrow K^+ \eta_c, \eta_c \rightarrow K_S K^+ \pi^+$  535 million  $B\bar{B}$ -meson pairs



Phys.Lett. B706 (2011) 139-149

2-dim fit of angle( $K^+ K_S$ ) vs.  $M(K_S K \pi)$

$$M = 2985.4 \pm 1.5_{-2.0}^{+0.5} \text{ MeV}$$

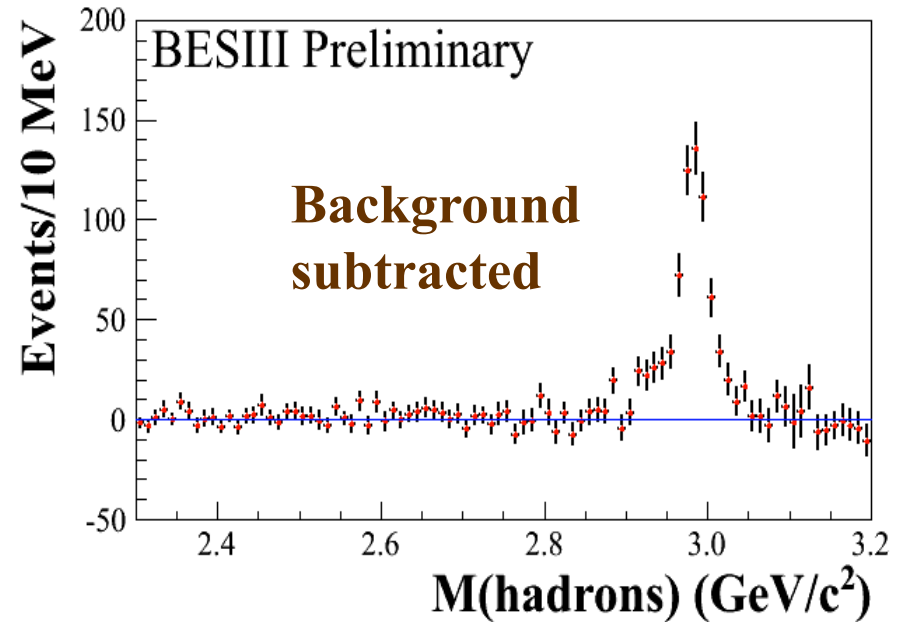
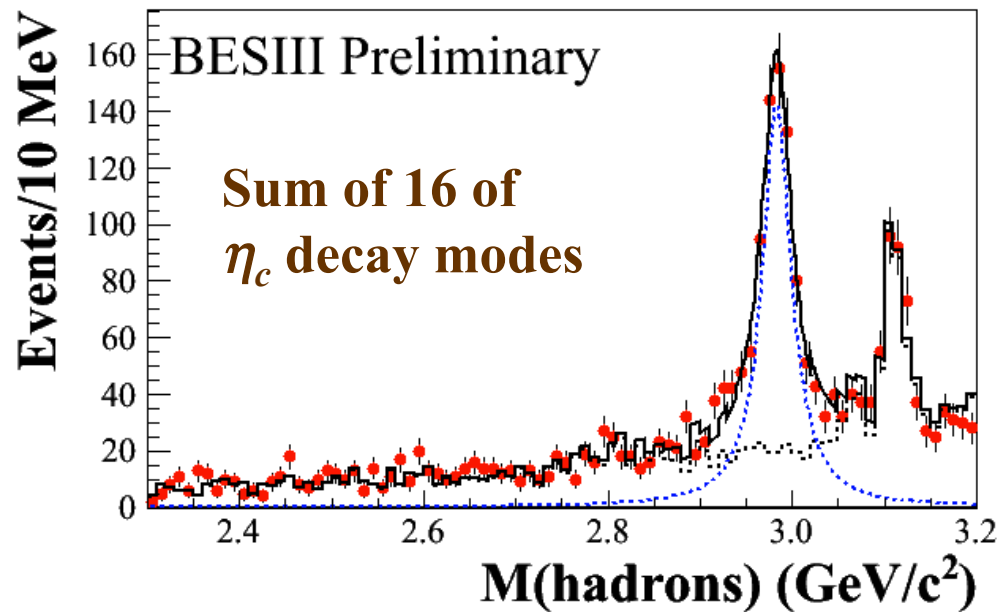
$$\Gamma = 35.1 \pm 3.1_{-1.6}^{+1.0} \text{ MeV}$$

Agreement with BaBar result  
in  $\gamma \rightarrow \eta_c$

Agreement with BESIII result  
in  $\psi' \rightarrow \gamma \eta_c$



# $\eta_c$ lineshape from $\psi' \rightarrow \pi^0 h_c, h_c \rightarrow \gamma \eta_c$ at BESIII



The  $\eta_c$  lineshape in  $h_c \rightarrow \gamma \eta_c$  is not as distorted as in  $\psi' \rightarrow \gamma \eta_c$  decays because the non-resonant interfering bkg is small ( $B(h_c \rightarrow \gamma \eta_c) = 54\%$ ,  $B(\psi' \rightarrow \gamma \eta_c) = 0.34\%$ ). Ultimately, this channel will be best suited to determine  $\eta_c$  resonance parameters.

Yesterday's search  $\rightarrow$  today's discovery  $\rightarrow$  tomorrow's calibration

# $\eta_c(2S)$

Crystal Ball's "first observation" of  $\psi' \rightarrow \gamma X$  never been confirmed.

*PRL 48 70 (1982)*

*"Seen"  $\eta_c(2S)$  from inclusive photon spectrum of  $\psi'$  decays.*

*Branch ratios and parameters are far from modern measurements.*

Observed in different processes other than radiative transition,

1.  $B \rightarrow K \eta_c(2S)$

*Belle: PRL 89 102001 (2002)*

2.  $\gamma\gamma \rightarrow \eta_c(2S) \rightarrow KK\pi$

*CLEO: PRL 92 142001 (2004)*

*Belle: NPPS.184 220 (2008); PRL 98 082001(2007)*

3. double charmonium  
production

*BaBar: PRL 92 142002 (2004); PR D72 031101(2005)*

*BaBar: PR D84 012004 (2011)*

M1 transition  $\psi' \rightarrow \gamma \eta_c(2S)$

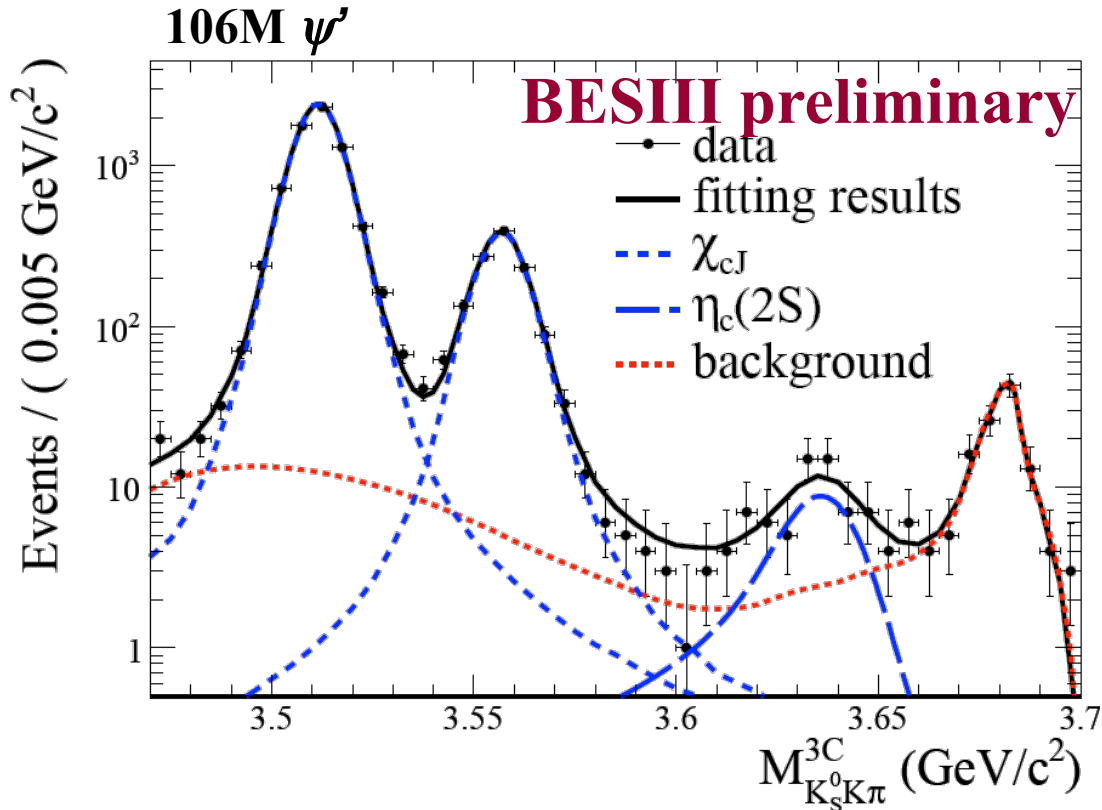
CLEO found no signals in 25M  $\psi'$ .

$BF(\psi' \rightarrow \gamma \eta_c(2S)) < 7.6 \times 10^{-4}$

CLEO: PRD 81 052002 (2010)

*Experimental challenge : search for photons of 50 MeV*

# Observation of $\psi' \rightarrow \gamma \eta_c(2S) \rightarrow \gamma(K_S K \pi)$ at BESIII



$$BF(\psi' \rightarrow \gamma \eta_c(2S) \rightarrow \gamma K_S K \pi) = (2.98 \pm 0.57 \pm 0.48) \times 10^{-6}$$

$$BF(\eta_c(2S) \rightarrow \bar{K} K \pi) = (1.9 \pm 0.4 \pm 1.1)\%$$

BaBar: PR D78 012006 (2008)

$$BF(\psi' \rightarrow \gamma \eta_c(2S)) = (4.7 \pm 0.9 \pm 3.0) \times 10^{-4}$$

CLEO-c:  $< 7.6 \times 10^{-4}$   
PR D81 052002 (2010)

Width fixed to 12 MeV (world ave.)

Events:  $50.6 \pm 9.7$ ; Significance  $> 6.0\sigma$ !

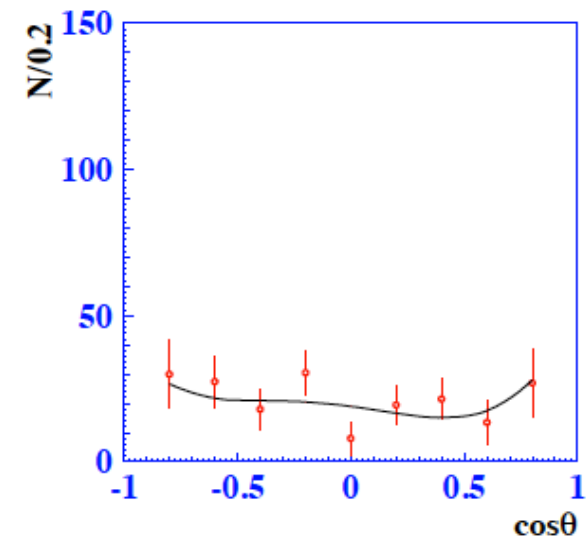
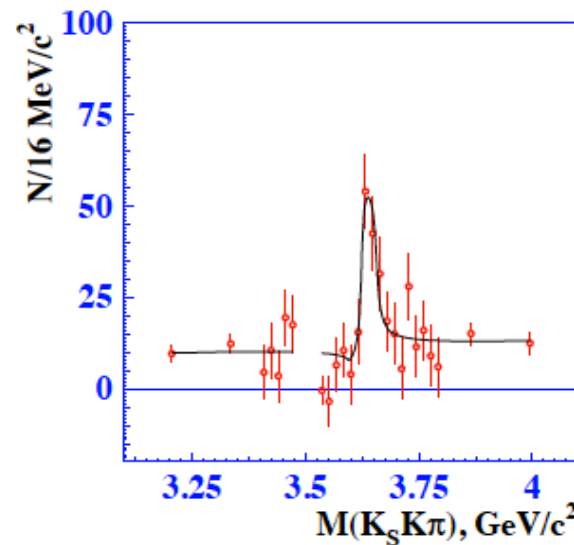
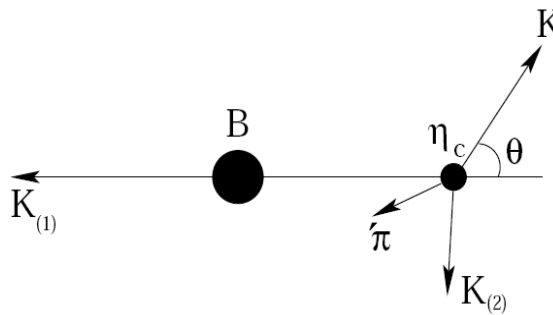
Mass =  $3638.5 \pm 2.3 \pm 1.0 \text{ MeV}/c^2$

Potential model predicts  
 $(0.1 \sim 6.2) \times 10^{-4}$

PRL 89 162002 (2002)

# New mass and width measurement of $\eta_c(2S)$ in $B$ decays at Belle

$$B^+ \rightarrow K^+ \eta_c(2S), \eta_c(2S) \rightarrow K_S K^\pm \pi^\mp$$



Phys.Lett. B706 (2011) 139-149

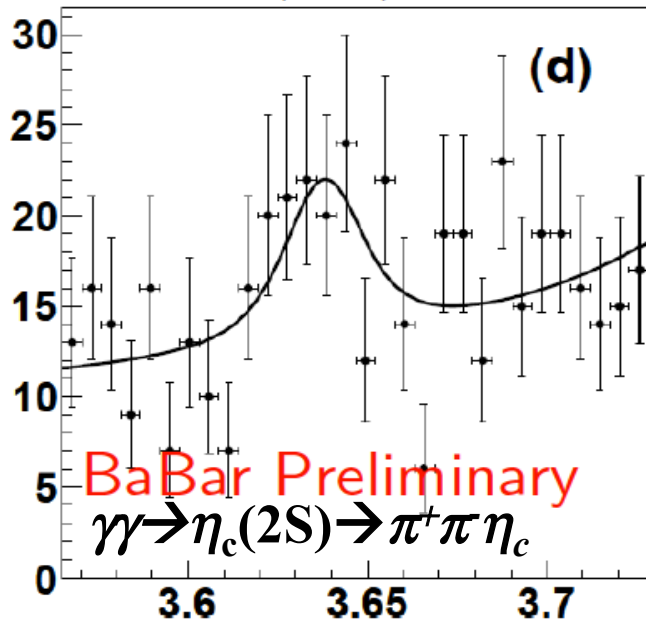
Interference of signal and non-resonant background important

fit with interference  $\Gamma = 6.6_{-5.1}^{+8.4}(\text{stat.}+\text{model})_{-0.9}^{+2.6}(\text{syst.}) \text{ MeV}$

fit w/o interference  $\Gamma = 41.1 \pm 12.0(\text{stat.})_{-10.9}^{+6.4}(\text{syst.}) \text{ MeV}$

# $\eta_c(1S)$ & $\eta_c(2S)$ new BaBar results

$\eta_c(2S)$  QNP2012



$\mathcal{B}(\eta_c(2S) \rightarrow \eta_c \pi^+ \pi^-) < 7.4\%$

(compatible with prediction  $< 2.2\%$ )

$$m(\eta_c(1S)) = 2982.5 \pm 0.4 \pm 1.4 \text{ MeV}/c^2$$

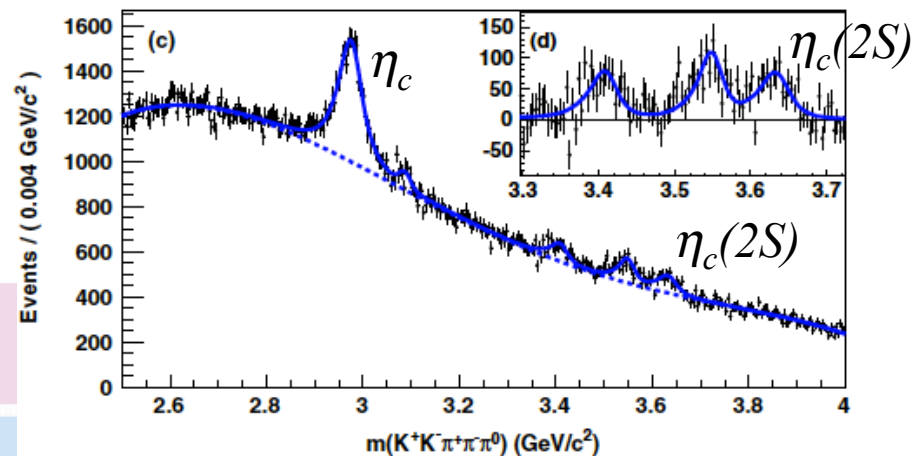
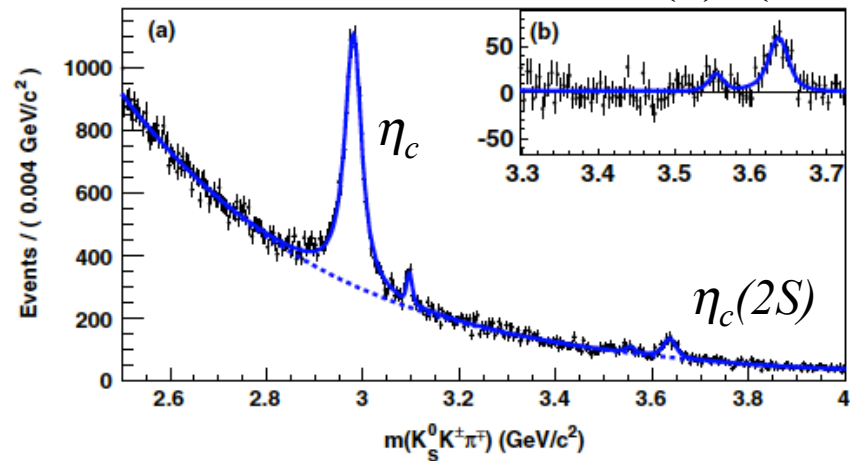
$$\Gamma(\eta_c(1S)) = 32.1 \pm 1.1 \pm 1.3 \text{ MeV}$$

$$m(\eta_c(2S)) = 3638.5 \pm 1.5 \pm 0.8 \text{ MeV}/c^2$$

$$\Gamma(\eta_c(2S)) = 13.4 \pm 4.6 \pm 3.2 \text{ MeV}$$

PRD 84, 012004 (2011)

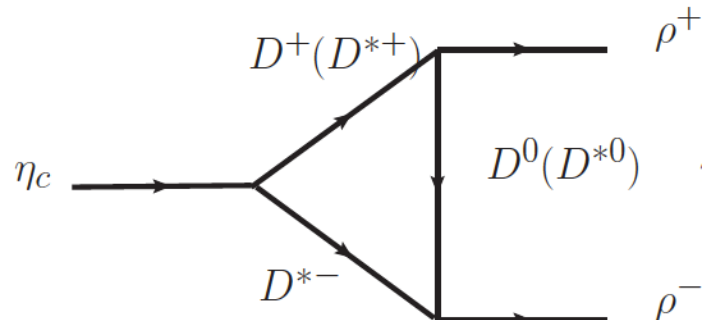
$519.2 \text{ fb}^{-1}$  near the  $Y(n)$ s ( $n=2, 3, 4$ )



$\gamma\gamma \rightarrow \eta_c \eta_c(2S) \rightarrow K_S K^\pm \pi^\mp$

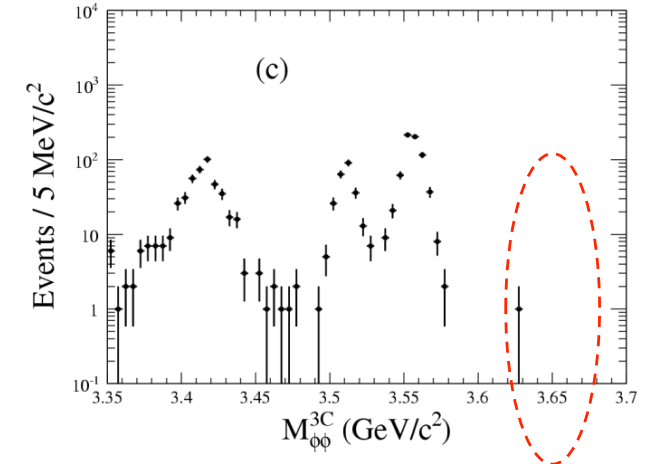
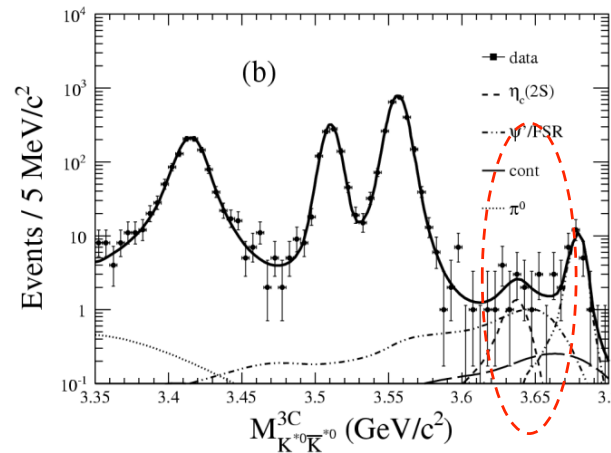
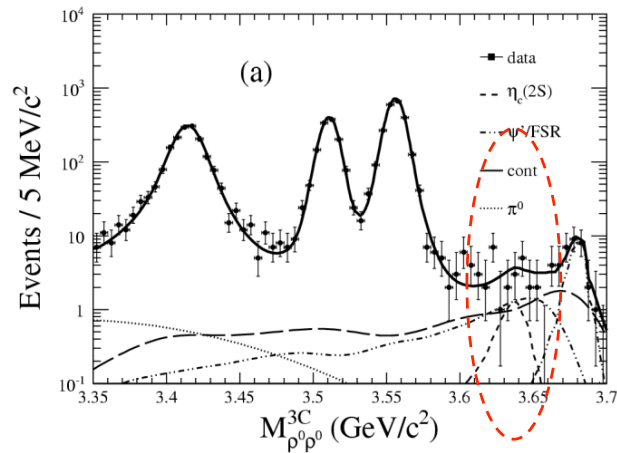
$\gamma\gamma \rightarrow \eta_c \eta_c(2S) \rightarrow K^+ K^- \pi^+ \pi^0 (5.3\sigma)$

# Search for $\eta_c(2S) \rightarrow VV$ at BESIII



Test for the “Intermediate charmed meson loops” to evade HSR

Phys. Rev. D 84, 091102 (2011)

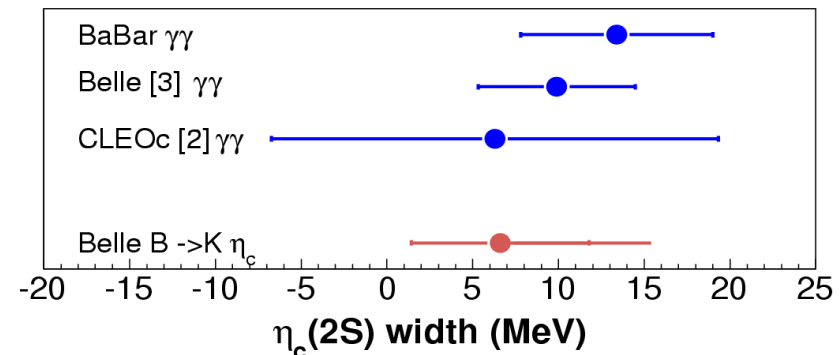
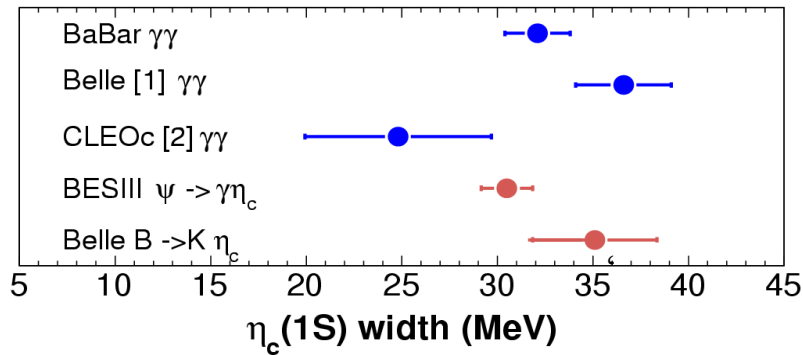
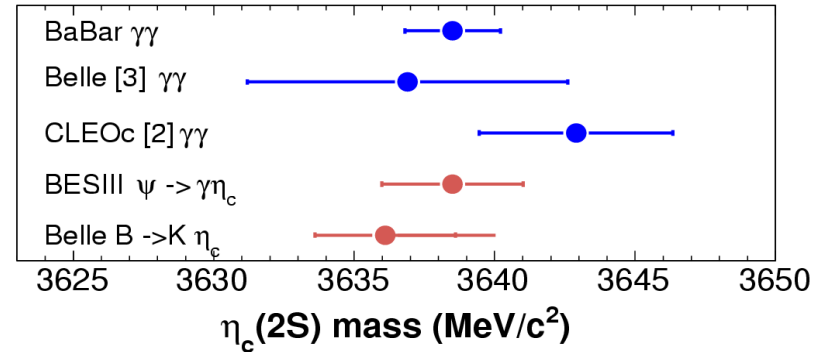
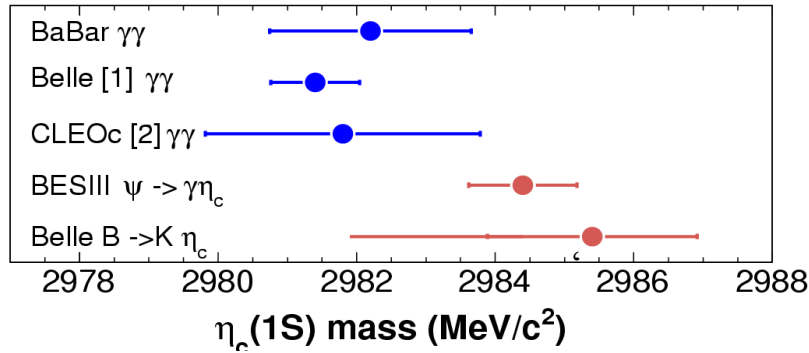


	$\text{BF}(\psi' \rightarrow \eta_c(2S) \rightarrow \gamma VV) (10^{-7})$	$\text{BF}(\eta_c(2S) \rightarrow VV) (10^{-3})$	Theory $\text{BF}(\eta_c(2S) \rightarrow VV) (10^{-3})$
$\rho^0 \rho^0$	$< 11.4$	$< 3.1$	$6.4 \sim 28.9$
$K^{*0} K^{*0}$	$< 19.4$	$< 5.3$	$7.9 \sim 35.8$
$\phi \phi$	$< 7.8$	$< 2.0$	$2.1 \sim 9.8$

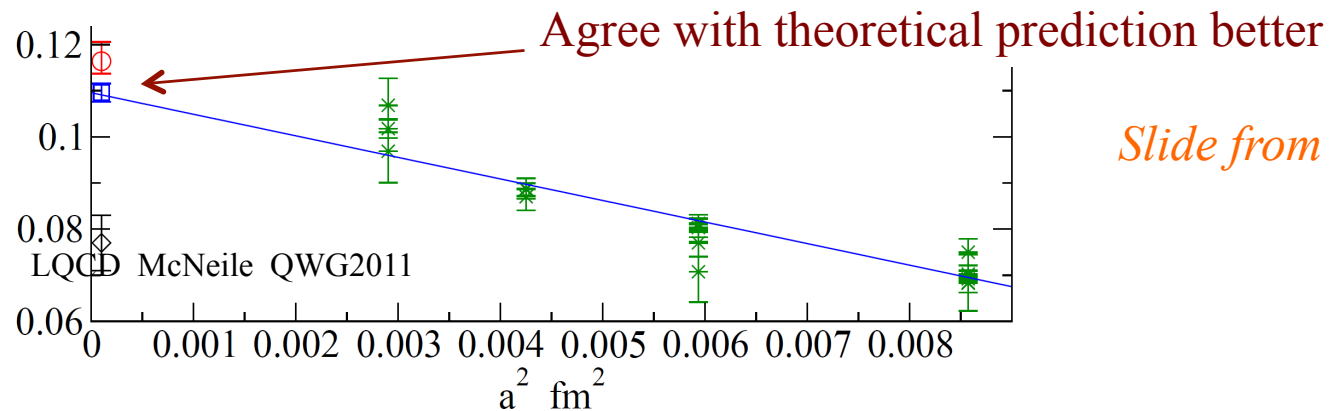
No signals observed in  $\eta_c \rightarrow \rho\rho, K^{*0} K^{*0}, \phi\phi$ ;  
more stringent UL's are set. CHARM2012 - Jianming Bian

arxiv1010.1343

# Summary of recent $\eta_c, \eta_c(2S)$ results



Hyperfine splitting:  $\Delta M(1S) = 112.5 \pm 0.8$  MeV (earlier results:  $\sim 117$  MeV)



*Slide from Steven Olsen*

# Summary

- $h_c(1P)$ :
  - Nailed down key branching ratios  $\psi' \rightarrow \pi^0 h_c$  and  $h_c \rightarrow \gamma \eta_c$ , so the absolute  $h_c$  cross sections/branching ratios are available.
  - New prolific production mode found:  $e^+e^- \rightarrow \pi^+\pi^- h_c$ .
- $\eta_c(1S)$ :
  - Mass and width are more consistent in  $\psi$  decays,  $B$  decays and  $\gamma\gamma$  production than previously.
  - $h_c \rightarrow \gamma \eta_c$  can provide an interference free lab for  $\eta_c$  lineshape study. (BESIII collected  $\sim 0.4\text{b}$   $\psi'$  data this year, making this approach possible)
- $\eta_c(2S)$ :
  - First observed in  $\psi'$  decays.
  - Decay modes other than  $KK\pi$  are observed.

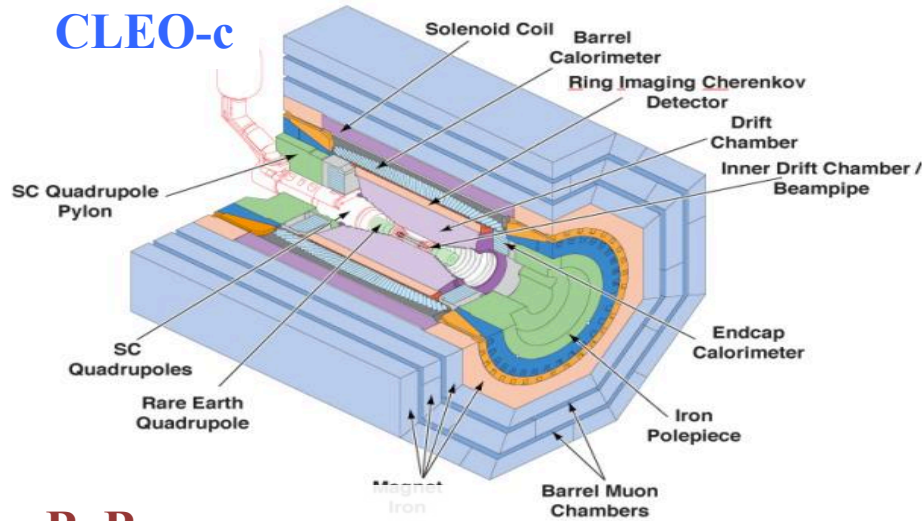


*Thank you!*

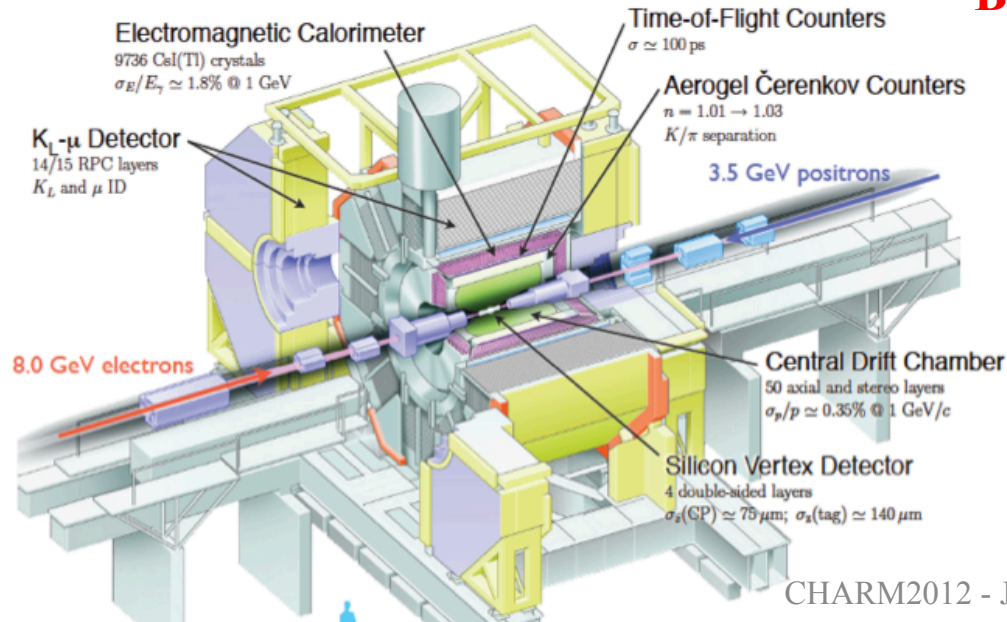
# *Backup*

# Detectors

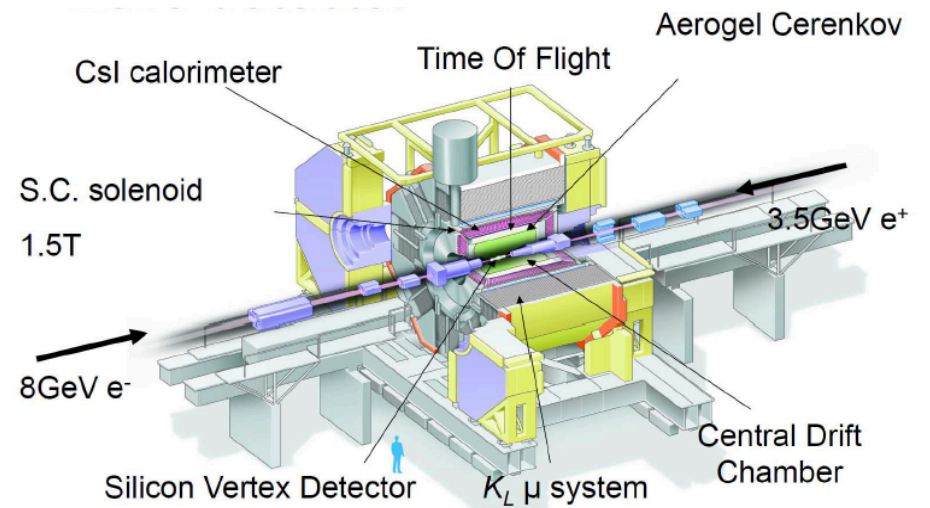
## CLEO-c



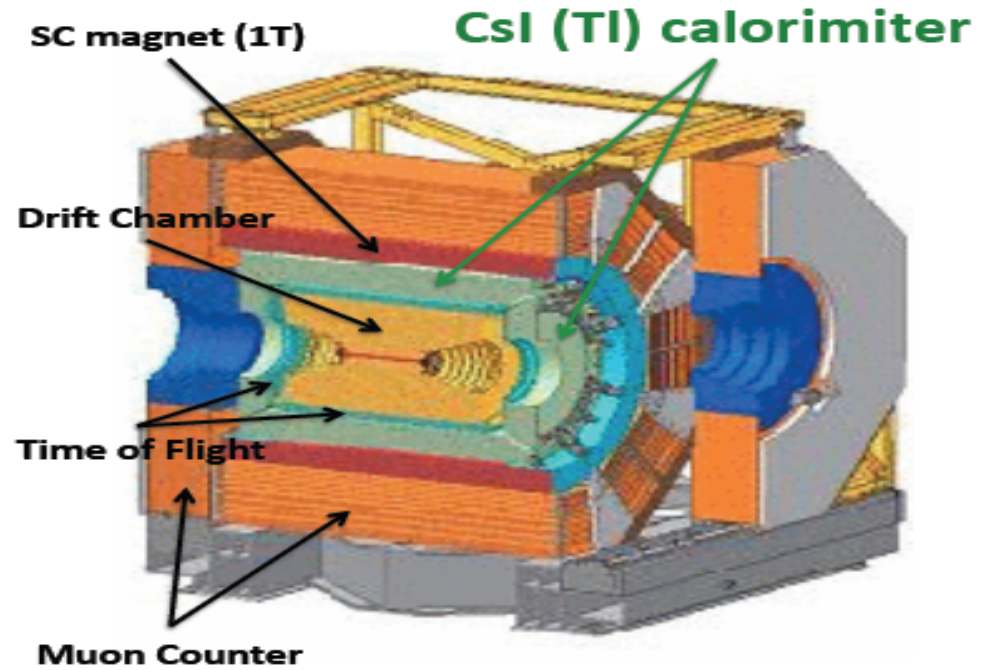
## BaBar



## Belle



## BESIII



# An example of intermediate charmed meson loops

arxiv1010.1343

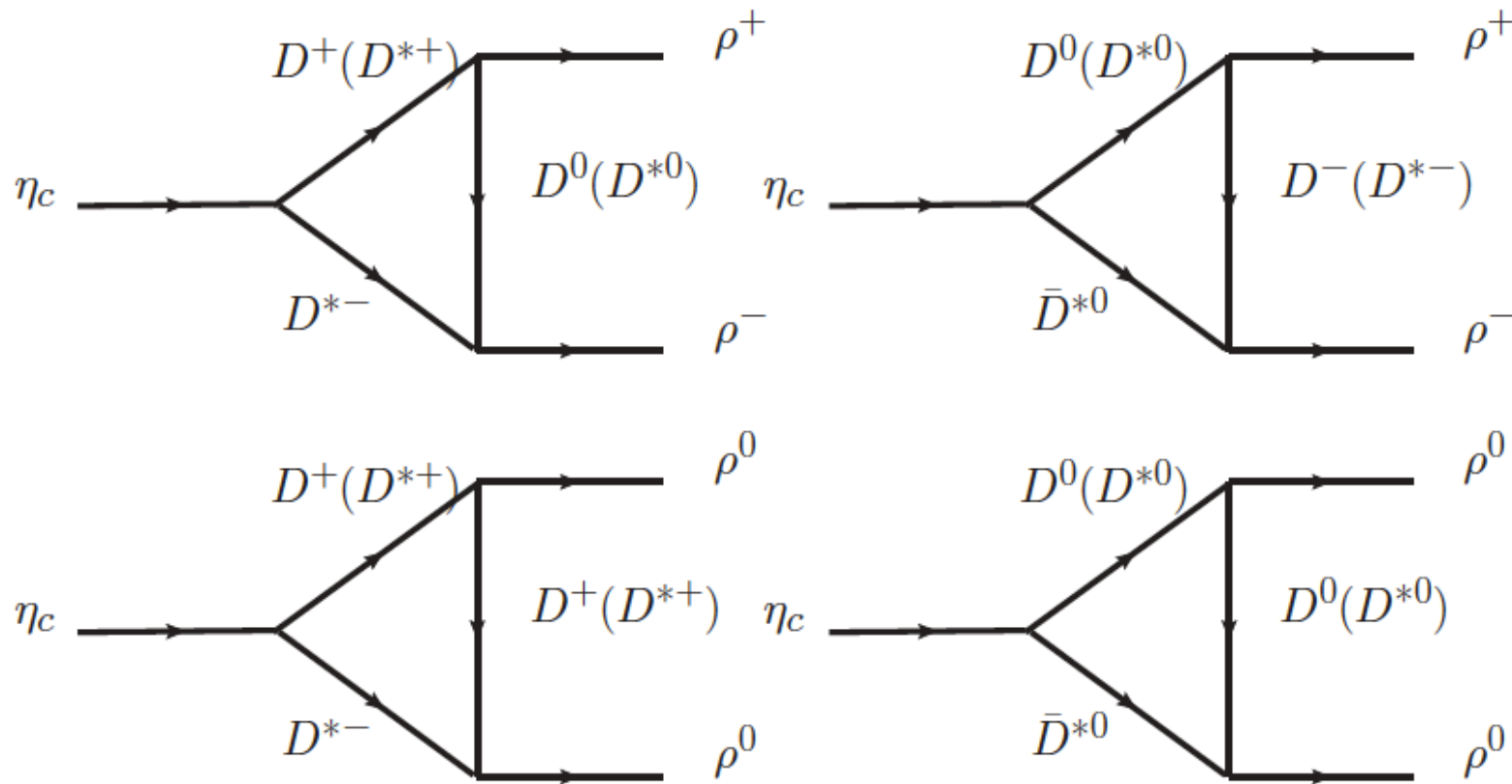


FIG. 1: Feynman diagrams for  $\eta_c \rightarrow \rho\rho$  via intermediate charmed meson loops.

# $\eta_c(\eta_c(2S))$ fitting formula at Belle

Phys.Lett. B706 (2011) 139-149

The fitting function can be represented as the square of the absolute value of the sum of the signal and non-resonant amplitudes integrated over all variables except  $M(K_S K \pi)$  and  $\cos \theta$ :

$$F(s, x) = \int \int \int \int_{x-\frac{\delta}{2}}^{x+\frac{\delta}{2}} \int_{s-\frac{\Delta}{2}}^{s+\frac{\Delta}{2}} (1 + \varepsilon_1 x' + \varepsilon_2 x'^2) \cdot \left| \left( \frac{\sqrt{N}}{s' - M^2 + iM\Gamma} A_\eta(q_1^2, q_2^2) + \alpha A_S(q_1^2, q_2^2) \right) S(x') + \beta A_P(q_1^2, q_2^2) P(x') + \gamma A_D(q_1^2, q_2^2) D(x') \right|^2 ds' dx' dq_1^2 dq_2^2 d\phi, \quad (1)$$

where  $x = \cos \theta$ ,  $s = M^2(K_S K \pi)$ ;  $q_1^2$  and  $q_2^2$  are Dalitz plot variables;  $\varepsilon_1$  and  $\varepsilon_2$  are constants that characterize the efficiency dependence on  $x$  and are

# $\eta_c(\eta_c(2S))$ fitting formula at Belle

determined from MC;  $\delta$  and  $\Delta$  are the bin widths in  $\cos\theta$  and  $M(K_S K \pi)$  invariant mass, respectively;  $M$  and  $\Gamma$  are mass and width of the  $\eta_c$  ( $\eta_c(2S)$ ) meson;  $N$  is the  $\eta_c$  ( $\eta_c(2S)$ ) signal yield;  $\alpha$ ,  $\beta$ ,  $\gamma$  are the relative fractions of the S-, P-, and D-waves, respectively;  $S = \frac{1}{\sqrt{2}}$ ,  $P = \sqrt{\frac{3}{2}}x$ ,  $D = \frac{3}{2}\sqrt{\frac{5}{2}}(x^2 - \frac{1}{3})$  are the functions characterizing the angular dependence of the S-, P-, and D-waves, respectively;  $A_\eta$  is the signal S-wave amplitude,  $A_{S,P,D}$  are the background S-, P-, and D-wave amplitudes, respectively. The absolute values of the amplitudes squared are normalized to unity:

$$\int \int \int |A_{\eta,S,P,D}(q_1^2, q_2^2)|^2 dq_1^2 dq_2^2 d\phi = 1. \quad (2)$$

To account for the momentum resolution, Eq. (1) is convolved with a Gaussian detector resolution function that is determined from the MC and calibrated from the  $J/\psi$  ( $\chi_{c1}$ ) width in data.