

Review of Results on Leptonic Decays of D^+ and D_s^+

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Charm 2012, 14—17 May, 2012, Hawaii, USA

OUTLINE

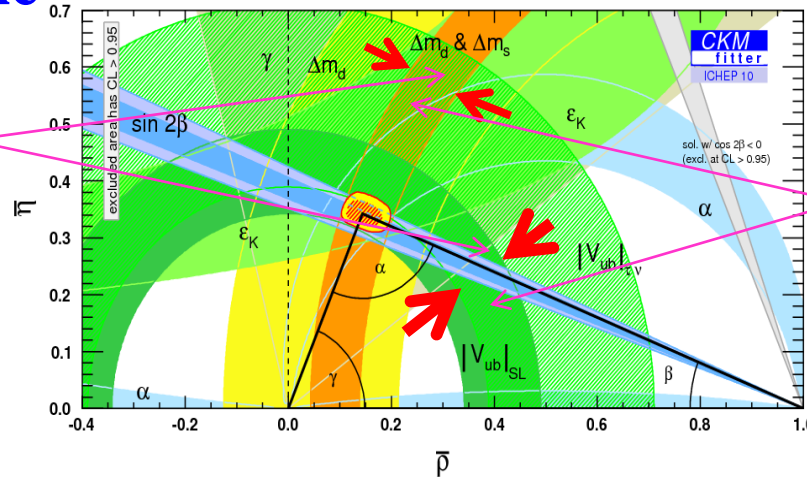
- **Charm role in test of SM**
- **D^+ leptonic decays**
- **Ds^+ leptonic decays**
- **Determination of $|V_{cd}|$ & $|V_{cs}|$**
- **Summary**

Charm role

➤ D^+ and D_S^+ leptonic decays play an important role in understanding of the SM of particle physics

➤ Unitary triangle

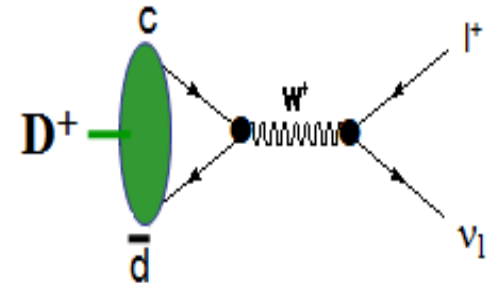
Widths of bands are dominated by errors of f_B and f_{B_s} from LQCD.



The widths of bands will be reduced if the LQCD pass the test with measured f_D , f_{D_s} .

➤ $f_{D(D_s)}$ test LQCD calculations of $f_{B(B_s)}$

$$\Gamma_{\text{SM}}(D_{(s)}^+ \rightarrow l^+ \nu) = \frac{G_F^2}{8\pi} m_l^2 m_{D_{(s)}} \left(1 - \frac{m_l^2}{m_{D_{(s)}}^2} \right)^2 |V_{cd(s)}|^2 f_{D_{(s)}}^2$$



➤ Reduced width of band in triangle would lead to precisely test the SM, and search for new physics beyond the SM.

Charm role

➤ Two charm decay constants ($f_{D(D_s)} \rightarrow f_{B(B_s)}$) affect

- $|V_{ub}|$ extracted from $B^+ \rightarrow l^+ \nu$
- $|V_{td}|$ extracted from Δm_d in $B^0 \bar{B}^0$ mixing
- $|V_{ts}|$ extracted from Δm_s in $B_s^0 \bar{B}_s^0$ mixing

These are used to
constraint the
unitary triangle

➤ Two decay branching fractions determine

- $|V_{cd}|$ extracted from $D^+ \rightarrow l^+ \nu$
- $|V_{cs}|$ extracted from $D_s^+ \rightarrow l^+ \nu$

➤ Precise measurements of f_{D_s} and f_D probe New Physics

Accumulating Evidence for Nonstandard Leptonic Decay of D_s Mesons

B.A. Dobressu and A.S. Kronfeld, PRL100, 241802 (2008)

R-parity violating supersymmetry, B_s mixing, and $D_s \rightarrow l \nu$.

A. Kundu and S. Nandi, PRD78, 015009 (2008)

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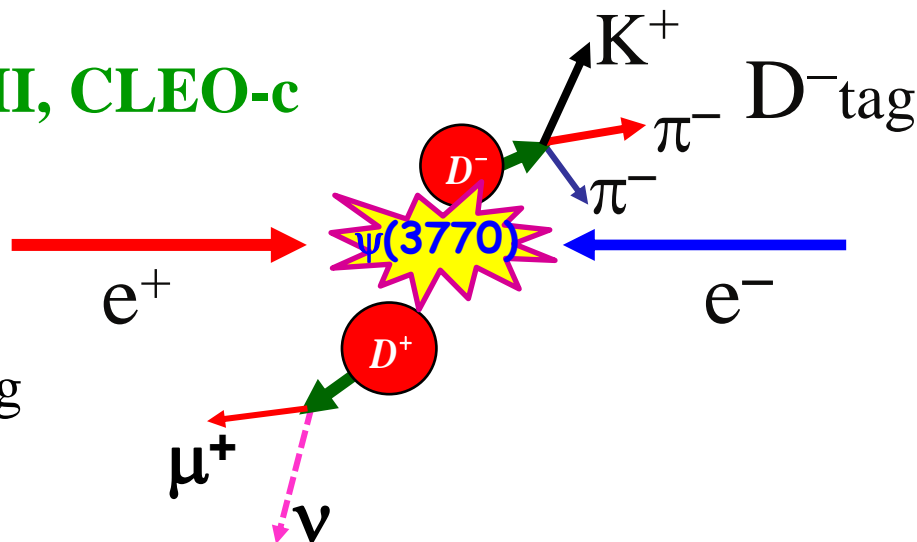
Experiments near threshold

➤ $\psi(3770) \rightarrow D\bar{D}$ events

MARK-III, BES-I, BES-II, CLEO-c
and BES-III

Single tag events

- D^+D^- production in pair
- Measure absolute branching fraction for $D^+ \rightarrow \mu^+\nu$



$$M_{\text{miss}}^2 = (E_{\text{beam}} - E_{\mu^+})^2 - (-\vec{p}_{D_{\text{tag}}^-} - \vec{p}_{\mu^+})^2$$

energy of μ^+	momentum of D_{tag}^-	momentum of μ^+
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The neutrino is reconstructed with the missing energy and missing momentum of the D^+ meson.

$$B(D^+ \rightarrow \mu^+\nu) = \frac{N_{D^+ \rightarrow \mu^+\nu}}{N_{D_{\text{tag}}^-} \epsilon_{D^+ \rightarrow \mu^+\nu}}$$

Experiments near threshold

➤ $\psi(4030) \rightarrow D_s^+ D_s^-$ events

~4.03 GeV

BES-I, and BES-III

$$B(D_s^+ \rightarrow l^+ \nu) = \frac{N_{D_s^+ \rightarrow l^+ \nu}}{N_{D_s^-} \mathcal{E}_{D_s^+ \rightarrow l^+ \nu}}$$

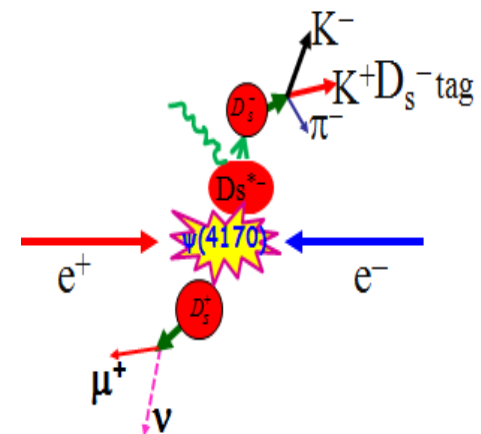
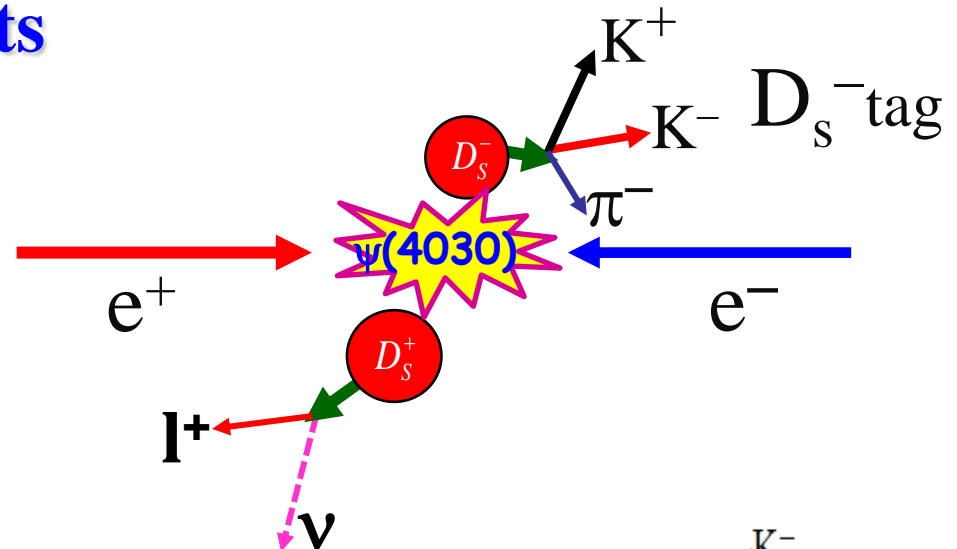
➤ $\psi(4170) \rightarrow D_s^+ D_s^{*-}$ events

~4.017 GeV

MARK-III and CLEO-c

Double tag can also be used to reconstruct the pure leptonic decays of $D_s^+ \rightarrow l^+ \nu$

Single tag events



Experiments at higher energies

➤ Fixed target experiments

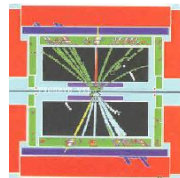
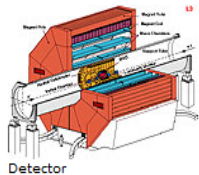
WA75, E653

➤ $e^+e^- \rightarrow Z$ @ ~91 GeV events

L3,

OPAL,

ALEPH

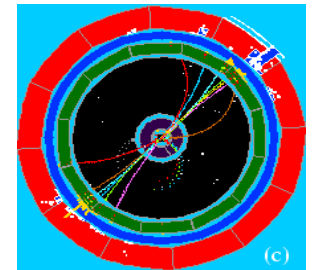


$$e^+e^- \rightarrow Z \rightarrow c\bar{c} \rightarrow D_s^{*-} X$$

$$\hookrightarrow \gamma D_s^-$$

$$\hookrightarrow \tau \bar{\nu}_\tau$$

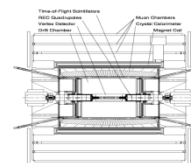
$$\hookrightarrow l^- \bar{\nu}_l \nu_\tau \quad (l = e, \mu)$$



➤ $e^+e^- \rightarrow c\bar{c}$ @ 10.6 GeV

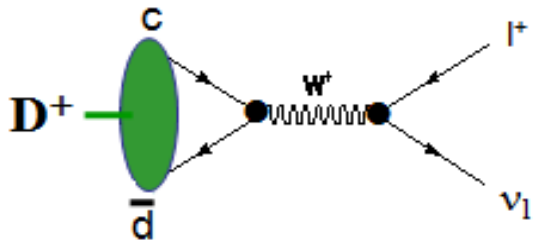
CLEO II, BaBar, Belle

$e^+e^- \rightarrow c\bar{c}$ -bar events



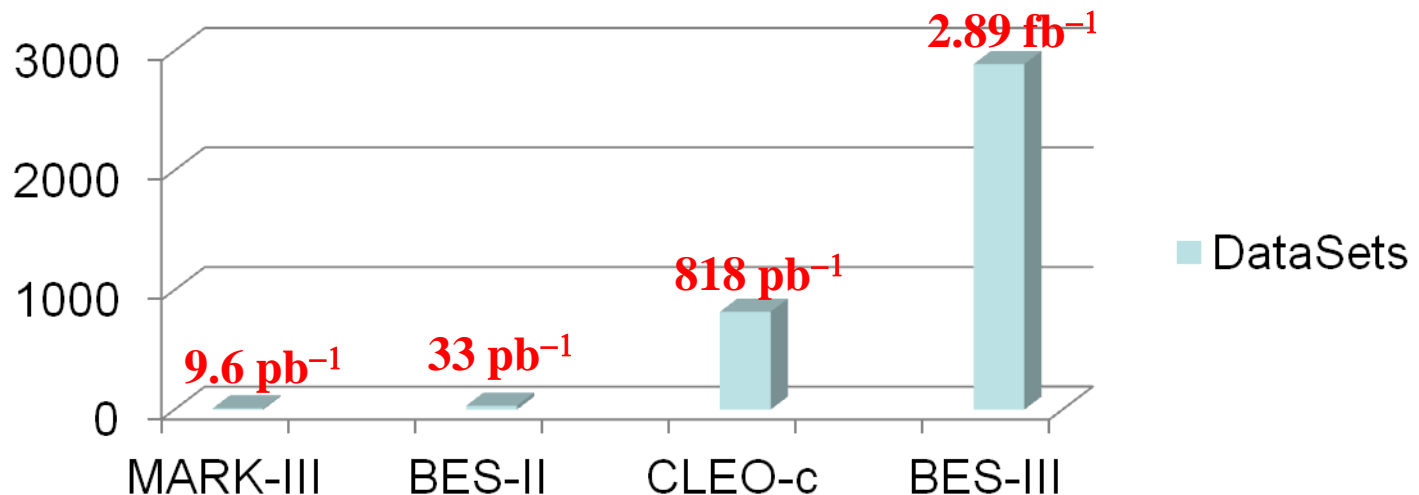
$$e^+e^- \rightarrow D_s^* D^{\pm,0} K^{\pm,0} X, \quad D_s^* \rightarrow \gamma D_s, \quad X = n\pi(\gamma)$$

D⁺ leptonic decays



Due to that this is a Cabibbo suppressed decay, measurements of this process were made at energies near threshold.

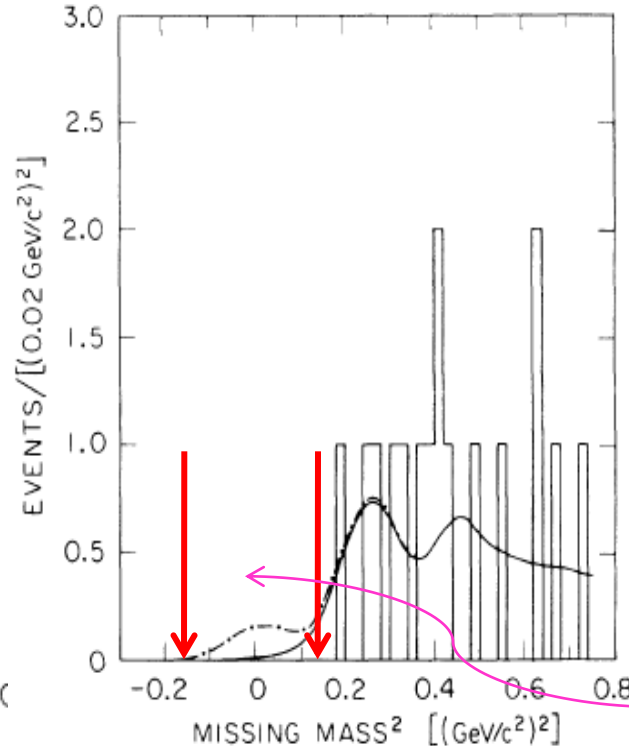
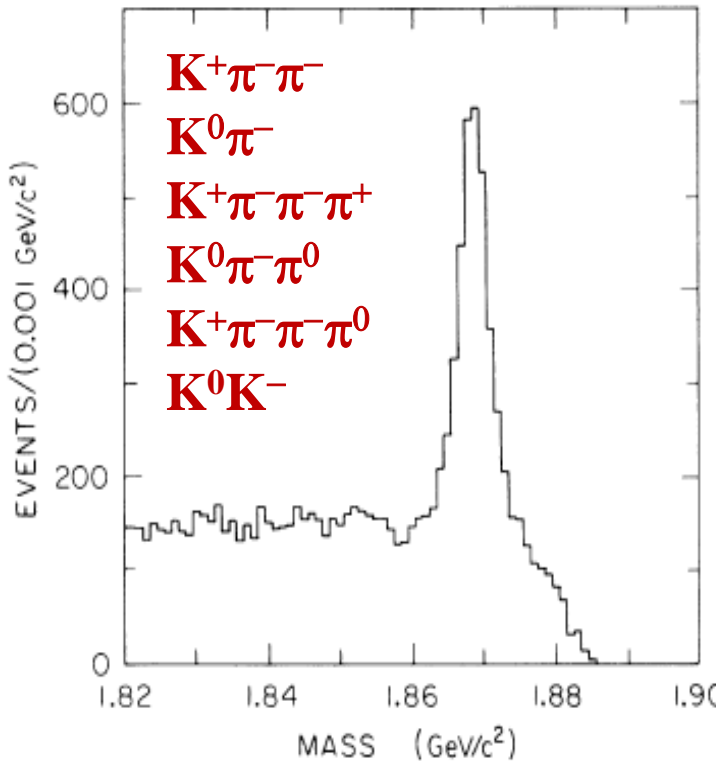
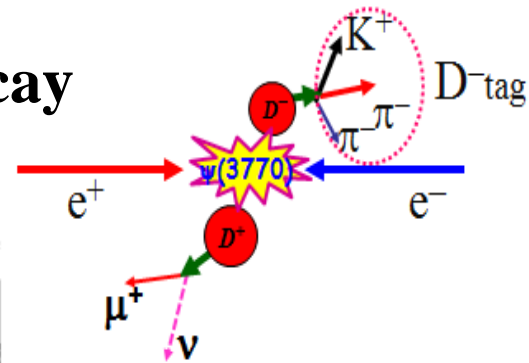
ψ(3770) Data samples in the world



D⁺ leptonic decays at MARK-III

In 1988, MARK-III first searched for the decay

PRL60, 1375(1988) 9.6 pb⁻¹ @ 3.773 GeV

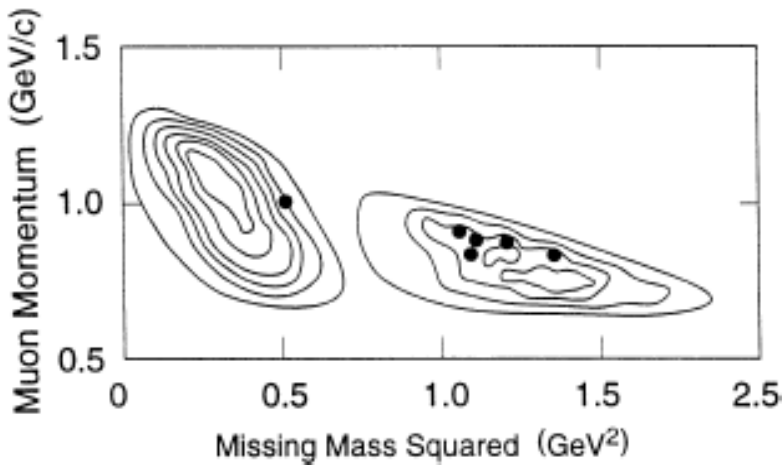
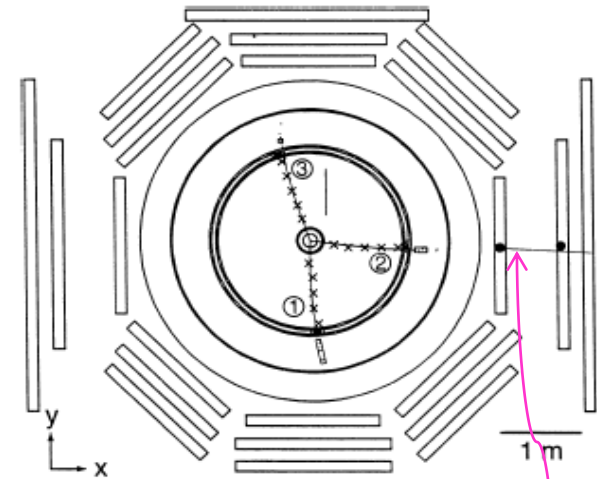
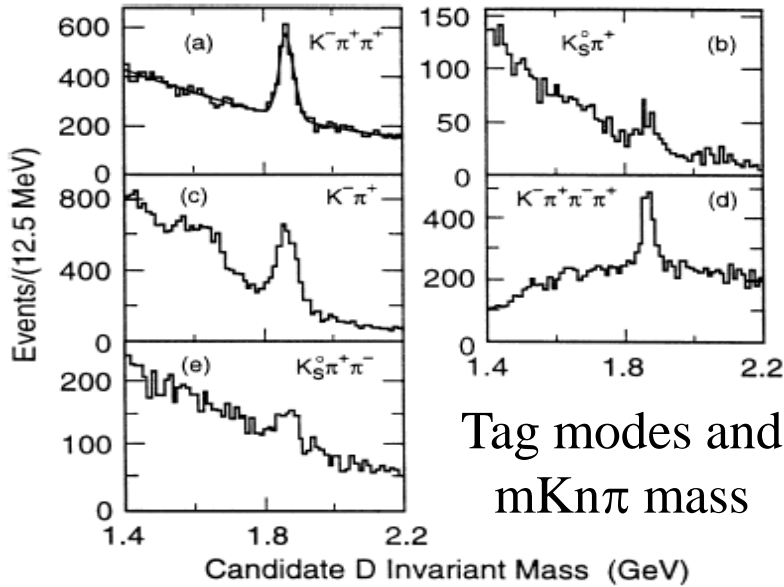


No signal event was found

MARK-III did not observe signal for this decay, they set an upper limit on decay constant $f_D < 290$ MeV

D⁺ leptonic decays at BES-I

22.3 pb⁻¹ @ 4.03 GeV PLB429, 188 (1998)



5 single tag modes

$$N_{D^+}^{\text{PRD}} = 10082$$

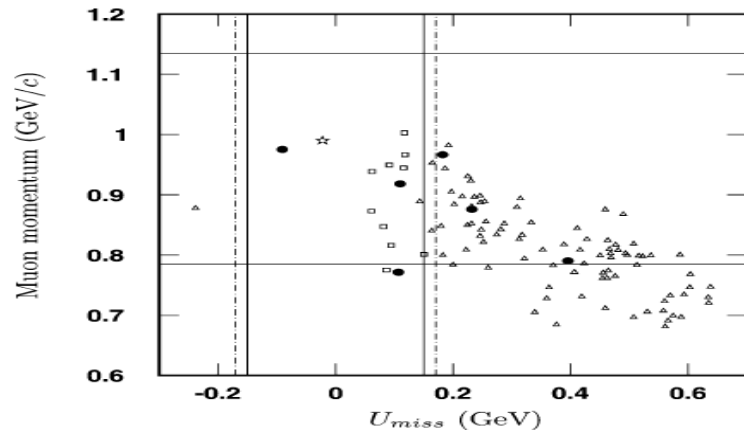
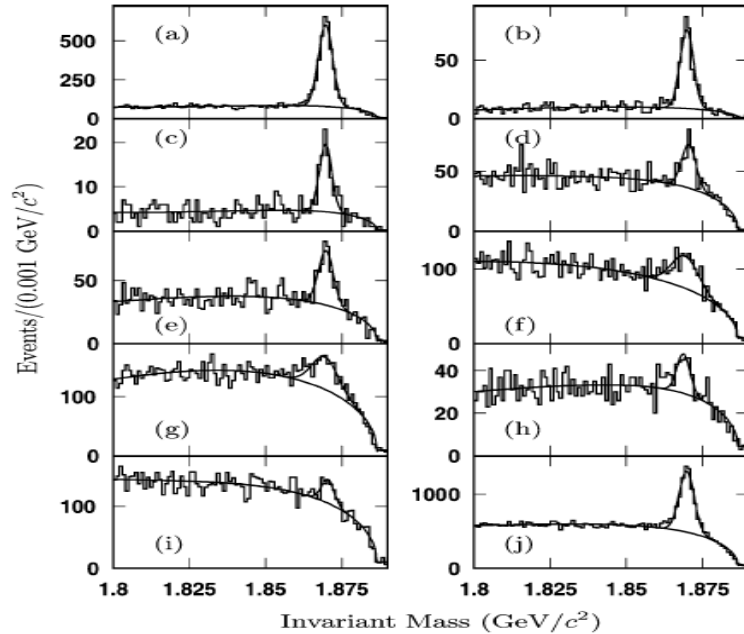
$$N_{D^+ \rightarrow \mu^+ \nu} = 1$$

One signal events observed

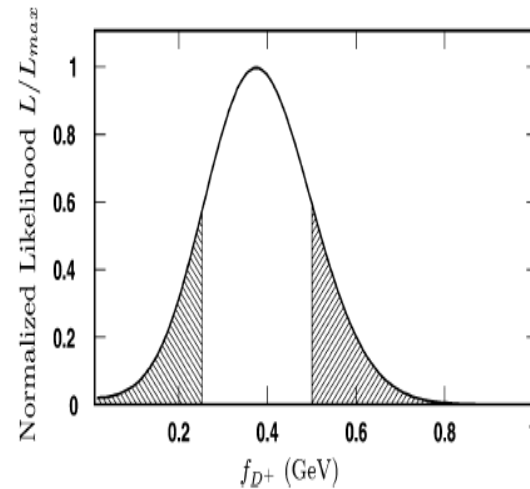
$$B(D^+ \rightarrow \mu^+ \nu) = (0.08^{+0.16+0.05}_{-0.05-0.02})\%$$

$$f_{D^+} = (300^{+180+80}_{-150-40}) \text{ MeV}$$

D⁺ leptonic decays at BES-II

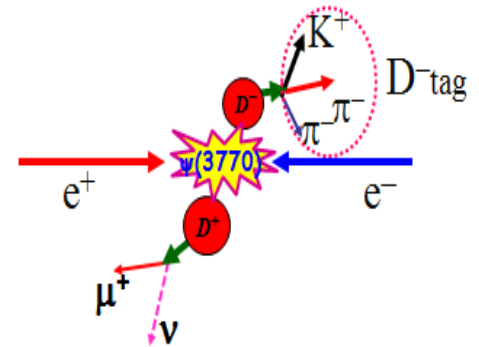


33 pb⁻¹ @ 3.773 GeV



**'04 Electroweak
Interactions &
Unified Theories**

PLB610, 183 (2005)



9 single tag modes

$$N_{D_{\text{tag}}^-} = 5321 \pm 149 \pm 160$$

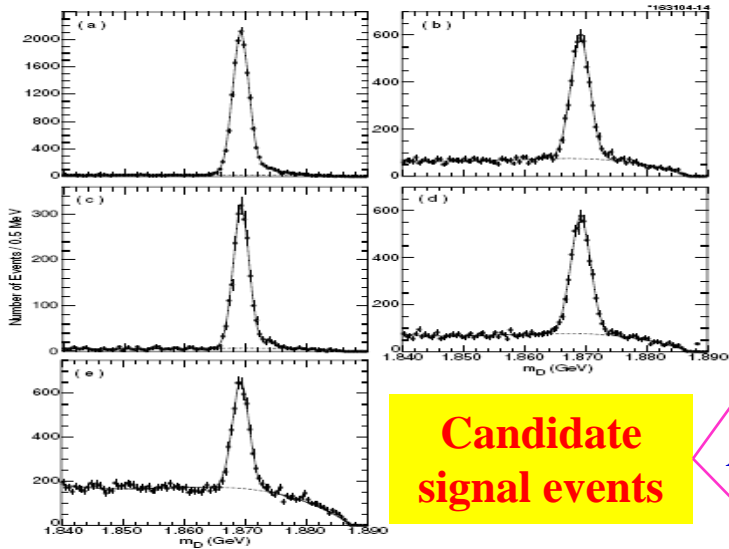
$$N_{D^+ \rightarrow \mu^+ \nu} = 2.7 \pm 1.7$$

$$B(D^+ \rightarrow \mu^+ \nu) = (0.122_{-0.053}^{+0.111} \pm 0.010)\%$$

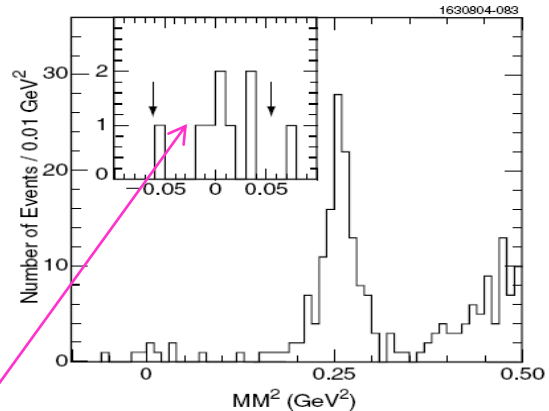
$$f_{D^+} = (371_{-119}^{+129} \pm 25) \text{ MeV}$$



D⁺ leptonic decays at CLEO-c



**Candidate
signal events**



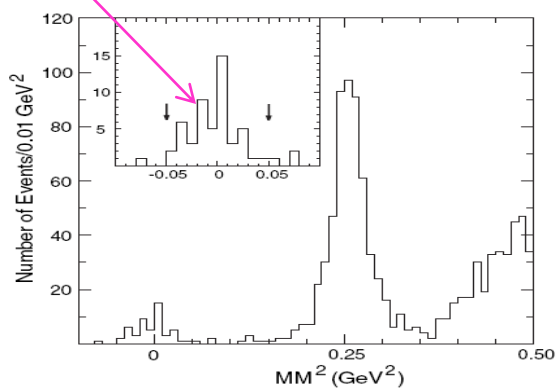
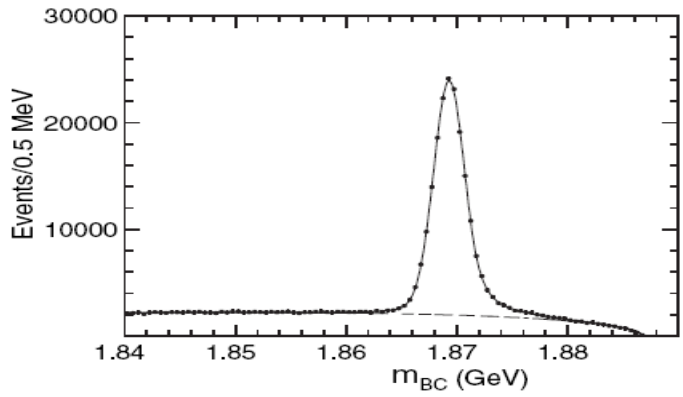
60 pb⁻¹
PRD70, 112004 (2004)

$$N_{D_{\text{tag}}^-} = 28651$$

$$N_{D^+ \rightarrow \mu^+ \nu} = 7 \pm 2.8$$

$$B(D^+ \rightarrow \mu^+ \nu) = (3.5 \pm 1.4 \pm 0.6) \times 10^{-4}$$

$$f_{D^+} = (202 \pm 41 \pm 17) \text{ MeV}$$



281 pb⁻¹

PRL95 251801 (2005)

$$N_{D_{\text{tag}}^-} = 158354 \pm 496$$

$$N_{D^+ \rightarrow \mu^+ \nu} = 47.2 \pm 7.1$$

$$B(D^+ \rightarrow \mu^+ \nu) = (4.40 \pm 0.66_{-0.12}^{+0.09}) \times 10^{-4} \quad f_{D^+} = (222.6 \pm 16.7_{-3.4}^{+2.8}) \text{ MeV} \quad 12$$



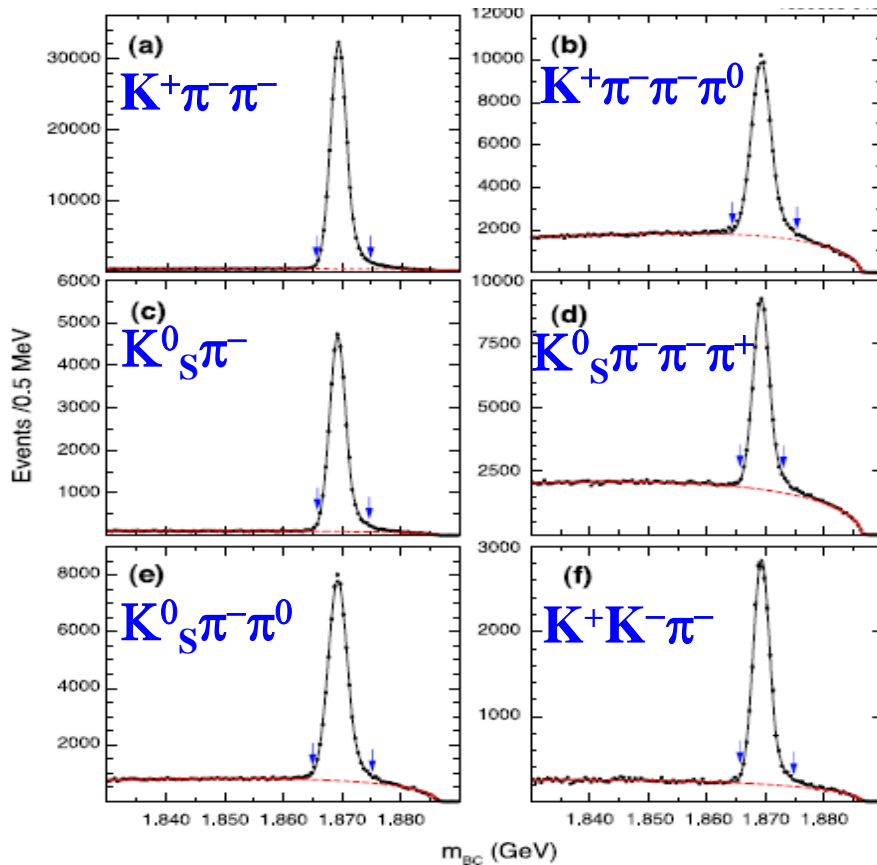
D⁺ leptonic decays at CLEO-c

PHYSICAL REVIEW D 78, 052003 (2008)

818 pb⁻¹

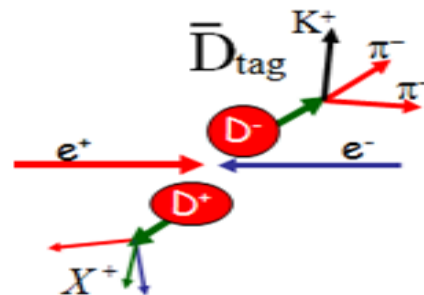
Precision measurement of $\mathcal{B}(D^+ \rightarrow \mu^+ \nu)$ and the pseudoscalar decay constant f_{D^+}

B. I. Eisenstein,¹ I. Karliner,¹ S. Mehrabyan,¹ N. Lowrey,¹ M. Selen,¹ E. J. White,¹ J. Wiss,¹ R. E. Mitchell,² M. R. Shepherd,² D. Besson,³ T. K. Pedlar,⁴ D. Cronin-Hennessy,⁵ K. Y. Gao,⁵ J. Hietala,⁵ Y. Kubota,⁵ T. Klein,⁵



Mode	Signal	Background
$K^+ \pi^- \pi^-$	$24\,778 \pm 497$	5957
$K^+ \pi^- \pi^- \pi^0$	$71\,605 \pm 359$	37\,119
$K_S \pi^-$	$32\,696 \pm 189$	1576
$K_S \pi^- \pi^- \pi^+$	$52\,554 \pm 315$	26\,352
$K_S \pi^- \pi^0$	$59\,298 \pm 289$	14\,837
$K^+ K^- \pi^-$	$19\,124 \pm 159$	3631
Sum	$460\,055 \pm 787$	89\,472

$$N_{D_{\text{tag}}^-} = 0.46 \times 10^6$$



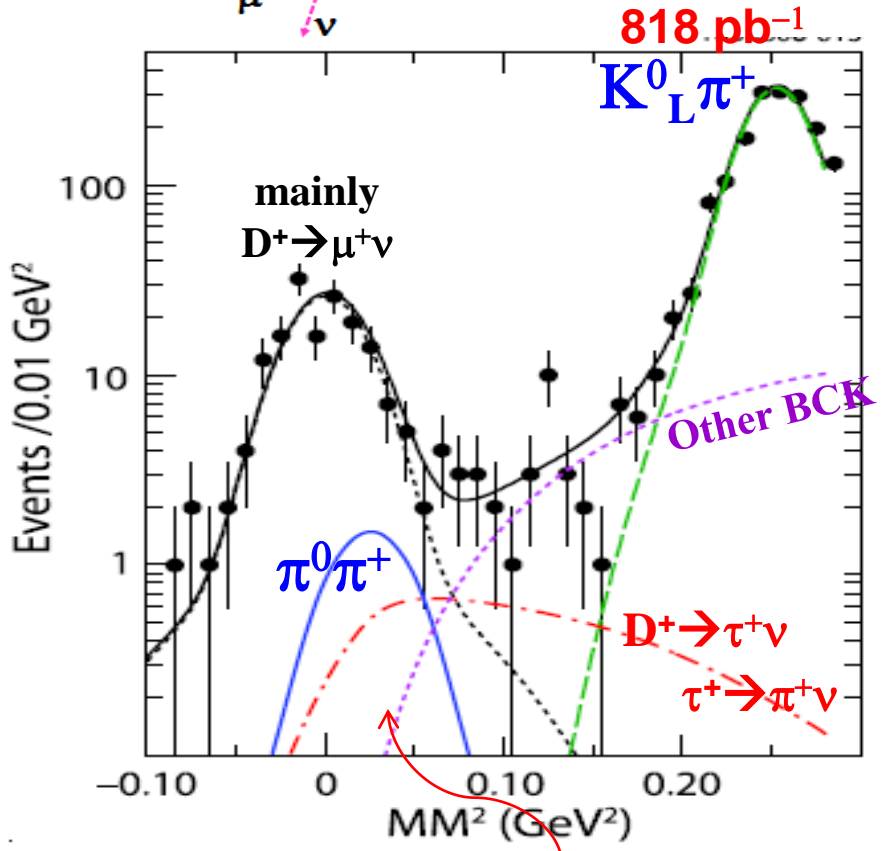
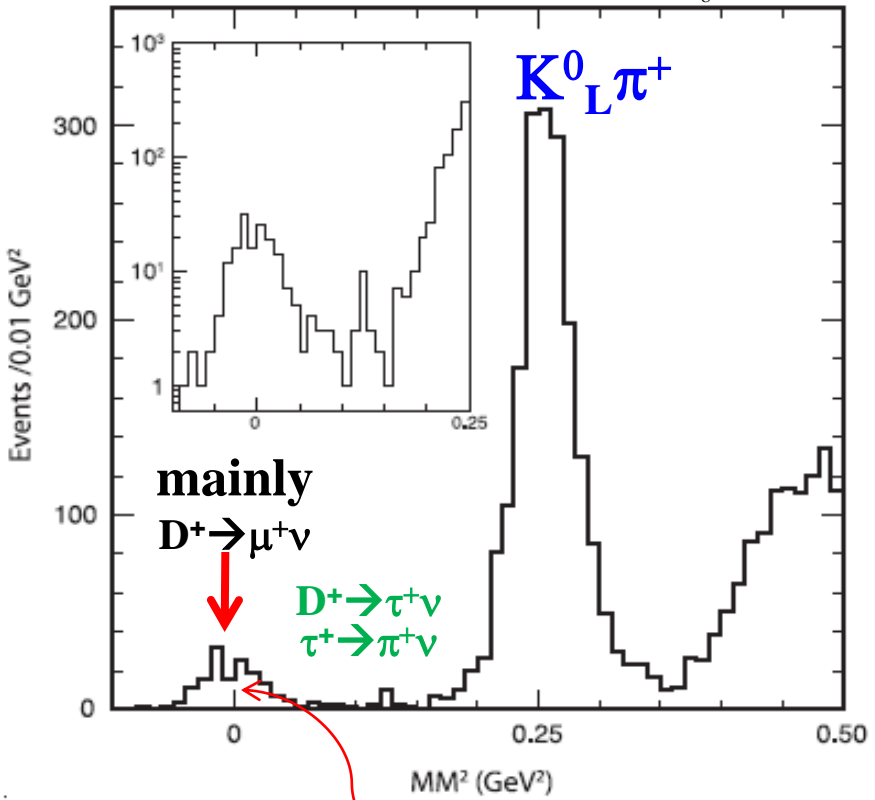
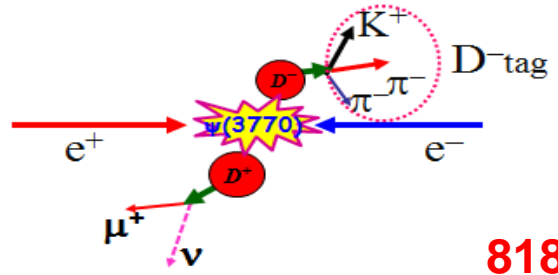
CLEO-c
D⁻ tags



D⁺ leptonic decays at CLEO-c

Recoil side is one track plus one missing neutrino

$$M_{\text{miss}}^2 = (E_{\text{beam}} - E_{\mu^+})^2 - (-\vec{p}_{D_{\text{tag}}^-} - \vec{p}_{\mu})^2$$



There are also some background events



D⁺ leptonic decays at CLEO-c

Results:

$$N(D^+ \rightarrow \mu^+ \nu) = 149.7 \pm 12.0$$

The statistical error is a little bit smaller than square root of 149.7

$$N(D^+ \rightarrow \tau^+ \nu) = 25.8 \text{ (fixed in fit)}$$

$$N(D^+ \rightarrow \pi^0 \pi^+) = 9.2 \text{ (fixed in fit)}$$

$$\text{Other background events : } 2.4 \pm 1.0$$

**37.4 BCK
Events**

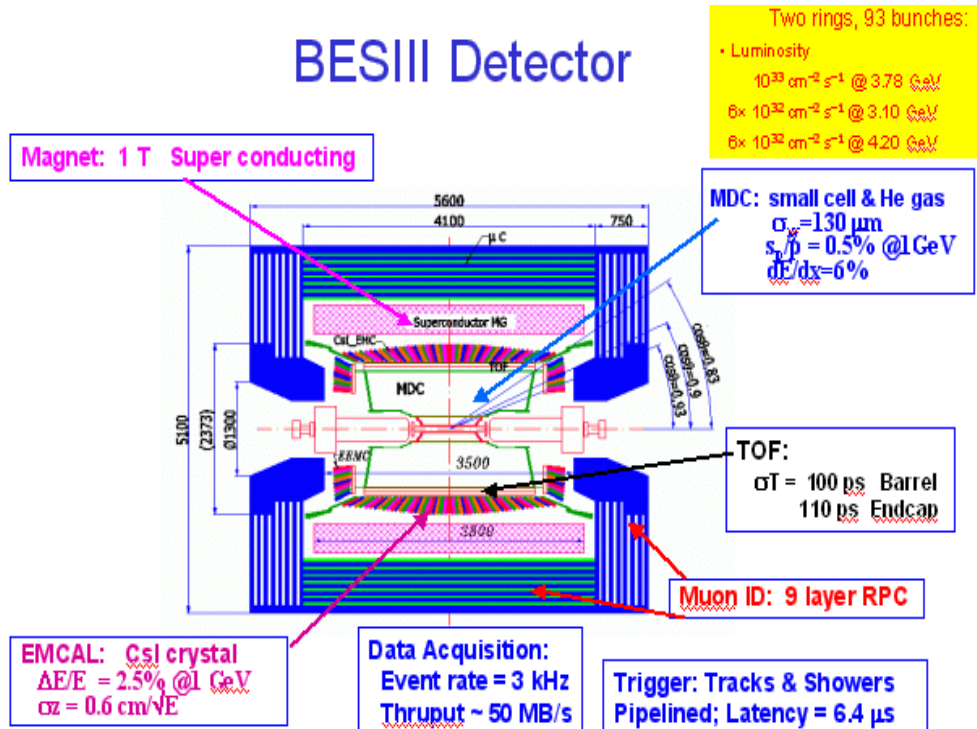
Mode	# of Events
Continuum	0.8 ± 0.4
$\bar{K}^0 \pi^+$	1.3 ± 0.9
D^0 modes	0.3 ± 0.3
Sum	2.4 ± 1.0

	Systematic errors (%)
Track finding	0.7
PID cut	1.0
MM ² width	0.2
Minimum ionization cut	1.0
Number of tags	0.6
Extra showers cut	0.4
Radiative corrections	1.0
Background	0.7
Total	2.2

$$Br(D^+ \rightarrow \mu^+ \nu) = (0.0382 \pm 0.0032 \pm 0.0009)\%$$

$$f_{D^+} = (205.8 \pm 8.5 \pm 2.5) \text{ MeV}$$

D⁺ leptonic decays at BES-III



The detector is hermetic for neutral and charged particle with excellent resolution, PID, and large coverage.

Background level for D⁺ leptonic decays at the BES-III is lower than that at the CLEO-c

L=2.89 fb⁻¹ @ 3.773 GeV

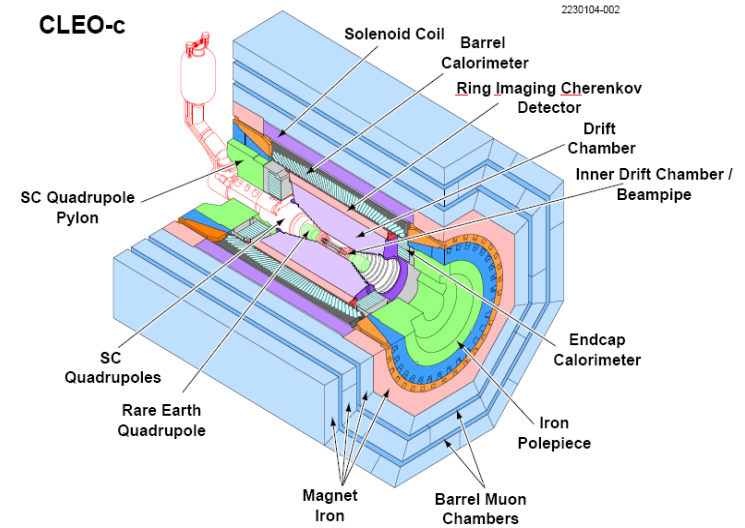
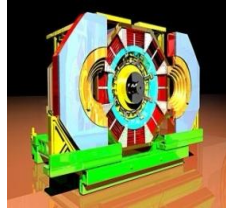


Figure 2.4: The CLEO-c detector.

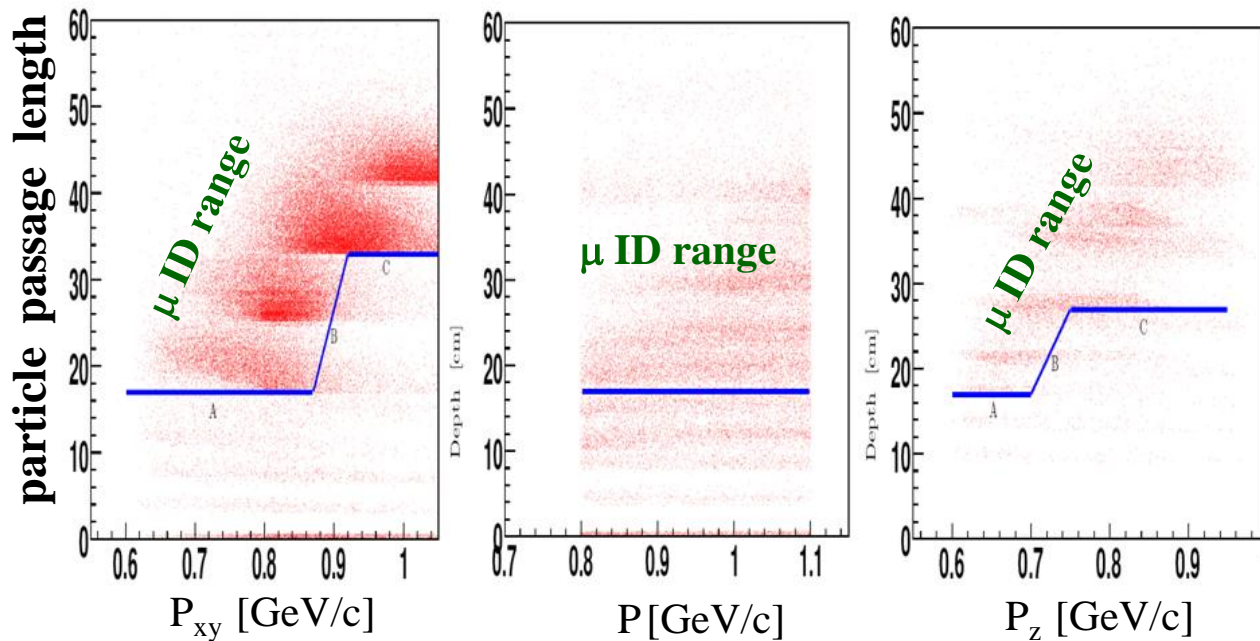
Advantage of the BES-III detector over CLEO-c is the MUC chamber with which BES-III can identify muon

L=818 pb⁻¹ @ 3.773 GeV

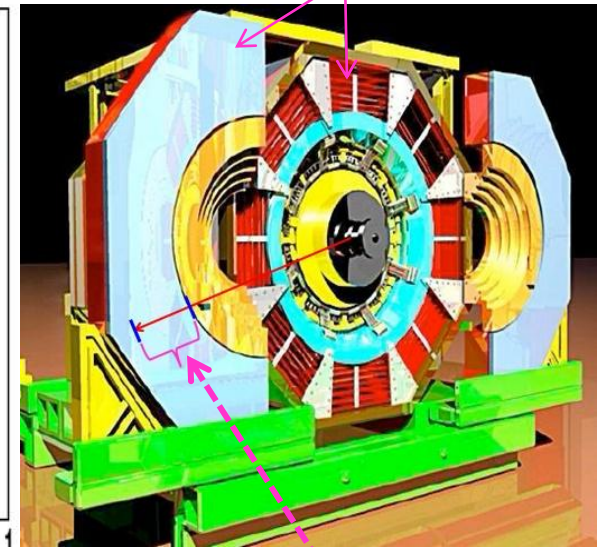
μ ID for $D^+ \rightarrow \mu^+ \nu_\mu$ at BES-III



Particle passage length in MUC VS momentum



μ chamber

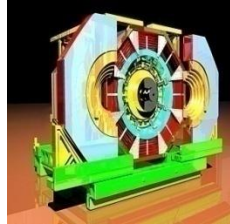


BES-III Detector

passage length of particle going through MUC

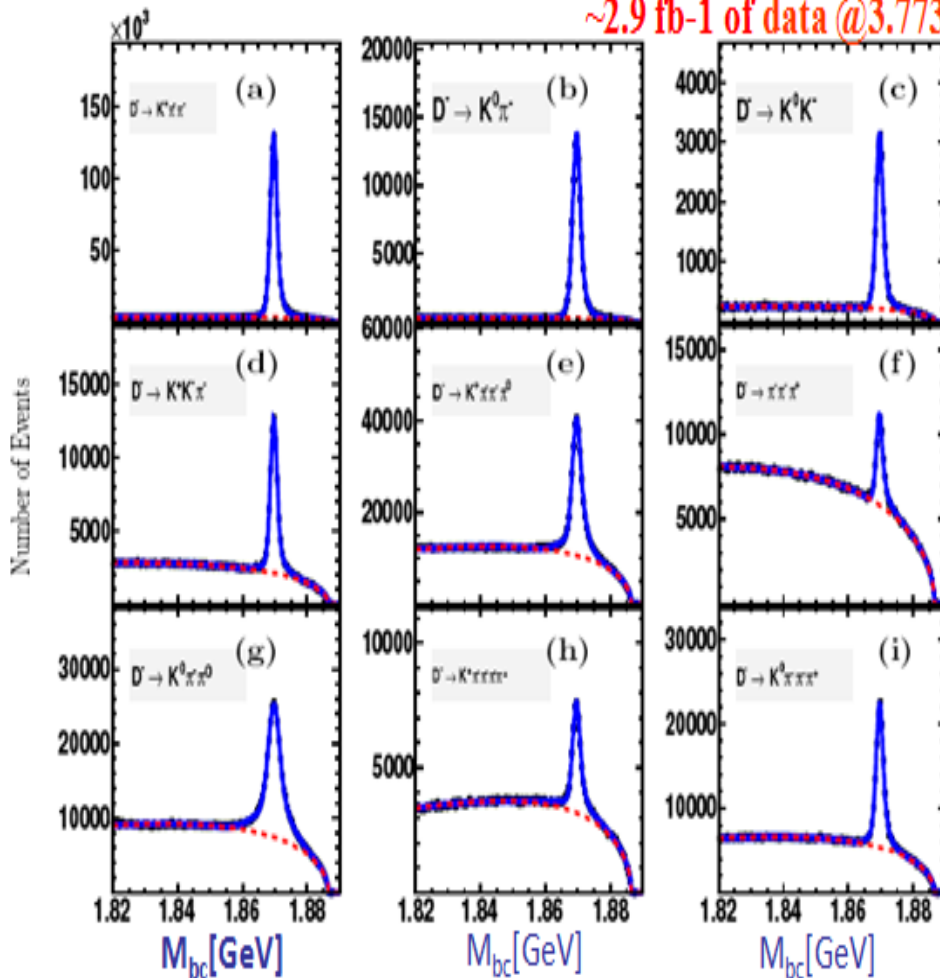
- Muon can be well identified with the passage length of a particle going through the MUC.
- If the passage length is greater than the one marked by the blue lines, the particle is assigned to be μ .

D⁺ leptonic decays at BES-III



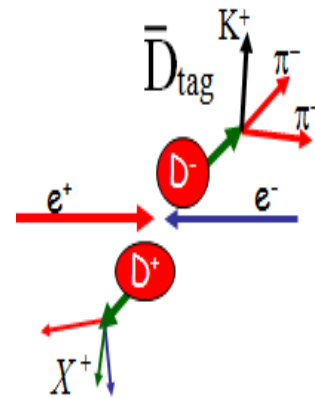
BES-III D⁻ tags

~2.9 fb⁻¹ of data @3.773



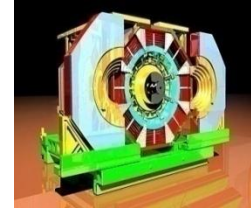
Single tag channels

- $D^- \rightarrow K^+ \pi^- \pi^-$
- $D^- \rightarrow K^- \pi^+ \pi^+ \pi^0$
- $D^- \rightarrow K^0 \pi^-$
- $D^- \rightarrow \pi^- \pi^- \pi^+$
- $D^- \rightarrow K^0 K^-$
- $D^- \rightarrow K^0 \pi^- \pi^0$
- $D^- \rightarrow K^+ K^- \pi^-$
- $D^- \rightarrow K^+ \pi^- \pi^- \pi^- \pi^+$
- $D^- \rightarrow K^0 \pi^+ \pi^- \pi^-$



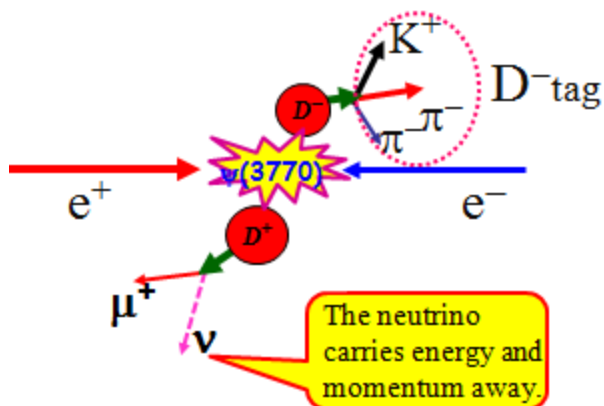
Using 9 singly tagged D⁻ modes to accumulate the D⁺D⁻ events.

$$N_{D_{tag}^-} = (1.57 \pm 0.2) \times 10^6$$



$D^+ \rightarrow \mu^+ \nu$ at BES-III

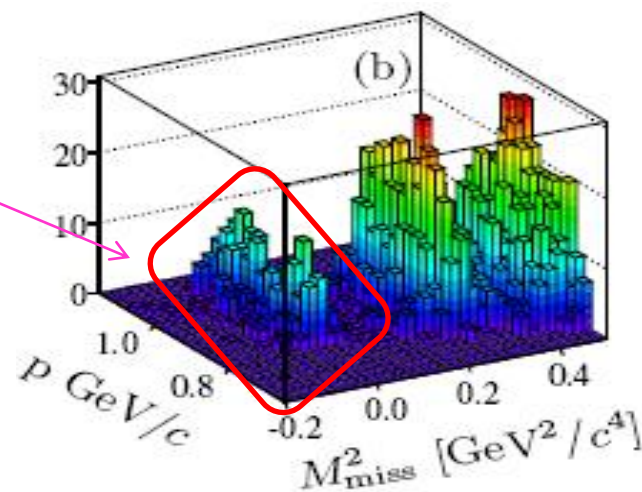
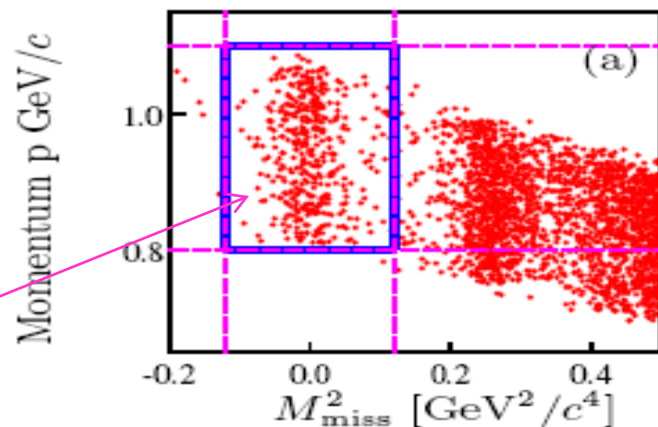
In the system recoiling against the singly tagged D^- , BES-III selected the purely leptonic decay events for $D^+ \rightarrow \mu^+ \nu$

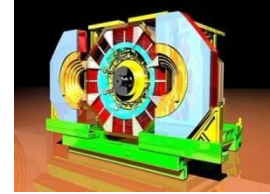


425 candidates for $D^+ \rightarrow \mu^+ \nu$

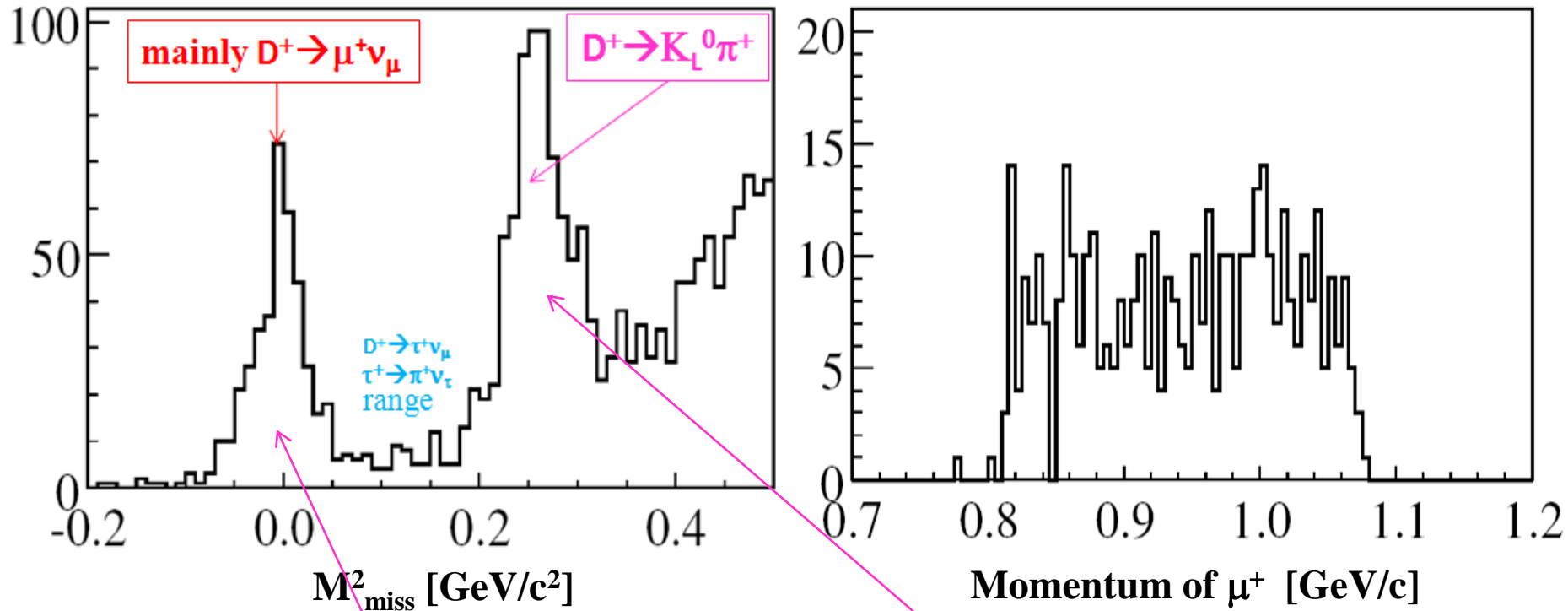
they require:

- One charged track only
- Positively identified μ
- No isolate photon





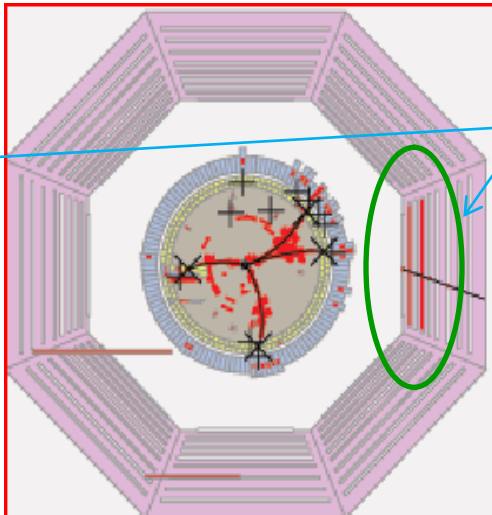
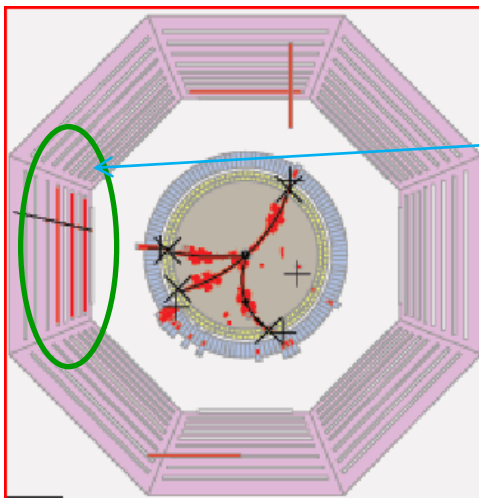
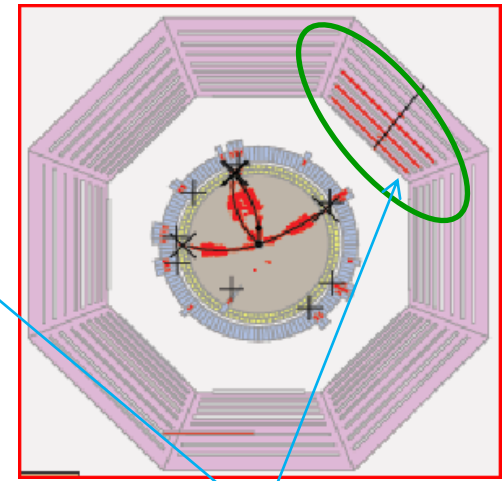
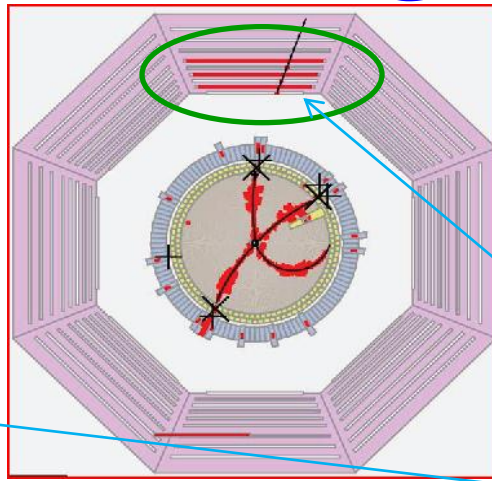
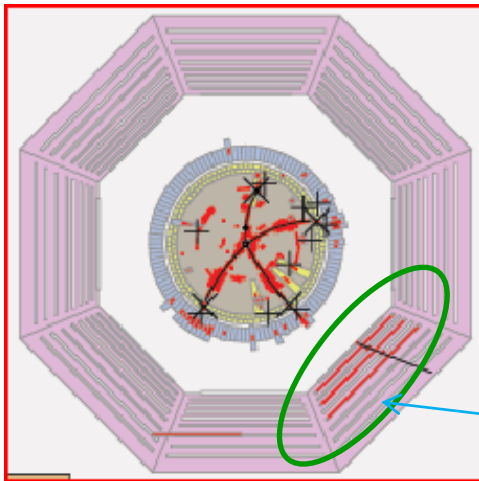
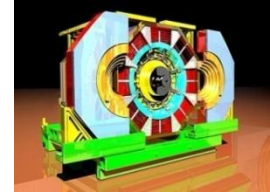
$D^+ \rightarrow \mu^+ \nu$ at BES-III



The K_L^0 escape from the detector.

There are still some backgrounds

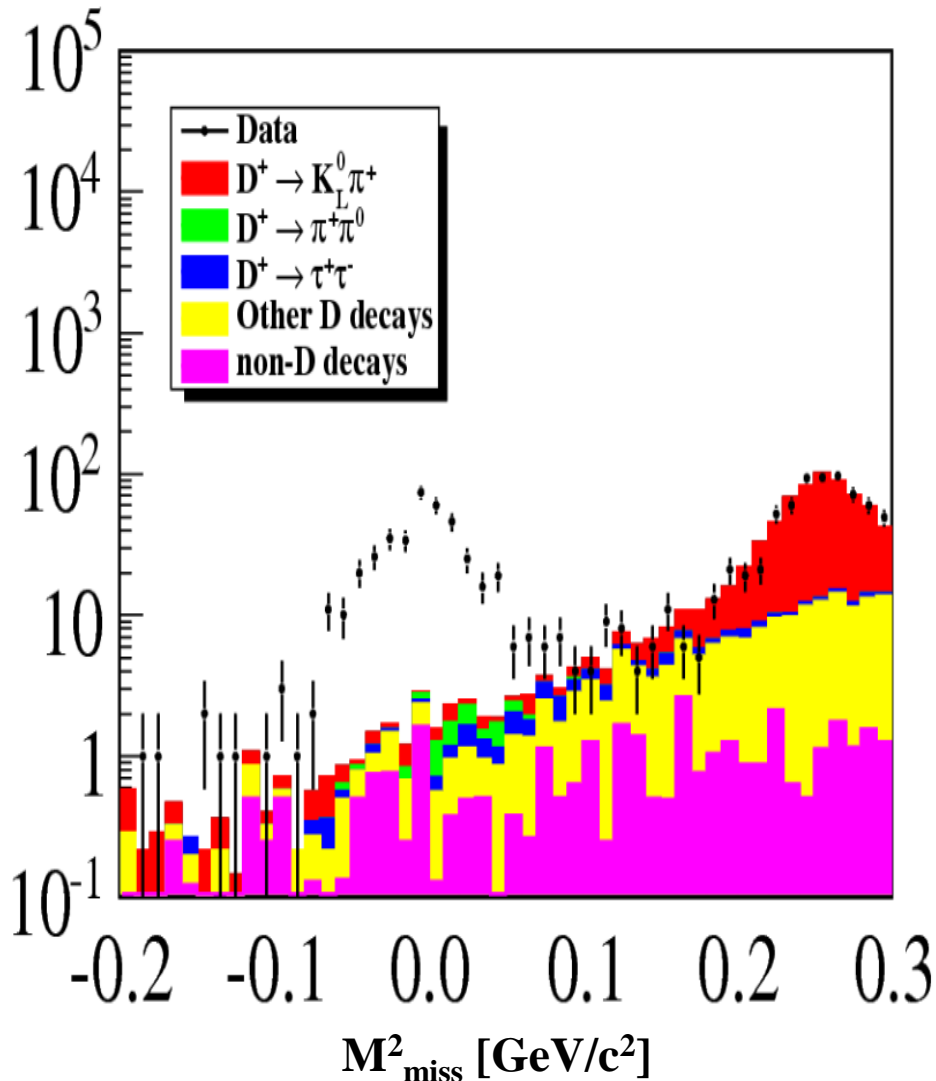
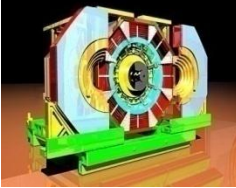
Event display for $D^+ \rightarrow \mu^+ \nu$ VS D^- tags



The muon can well be identified by MUC chamber

Each of the events is with a good μ hit in the μ chamber

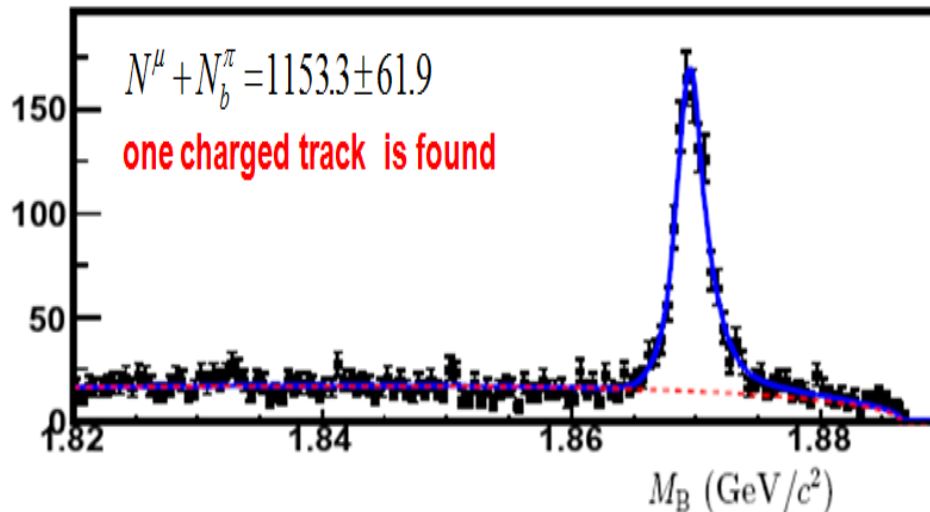
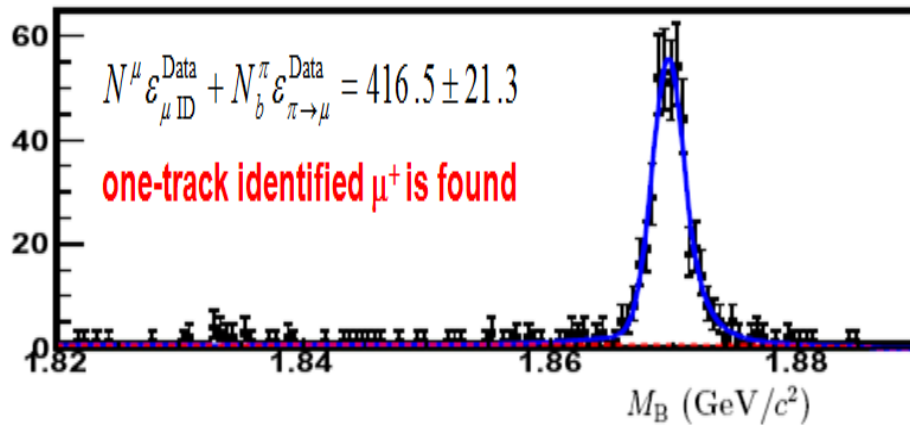
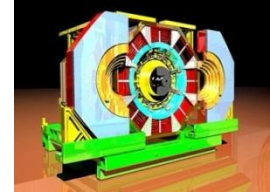
Backgrounds for $D^+ \rightarrow \mu^+ \nu_\mu$



Estimated with Monte Carlo events

Source mode	Number of events
$D^+ \rightarrow K_L^0 \pi^+$	7.9 ± 0.8
$D^+ \rightarrow \pi^+ \pi^0$	3.8 ± 0.5
$D^+ \rightarrow \tau^+ \nu_\tau$	6.9 ± 0.7
Other decays of D mesons	17.9 ± 1.1
$e^+ e^- \rightarrow \gamma \psi(3686)$	0.2 ± 0.2
$e^+ e^- \rightarrow \gamma J/\psi$	0.0 ± 0.0
$e^+ e^- \rightarrow \text{light hadron (continuum)}$	8.2 ± 1.4
$e^+ e^- \rightarrow \tau^+ \tau^-$	1.9 ± 0.5
$\psi(3770) \rightarrow \text{non-} D\bar{D}$	0.9 ± 0.4
Total	47.7 ± 2.3

Backgrounds for $D^+ \rightarrow \mu^+ \nu_\mu$



The number of backgrounds is also estimated with data.

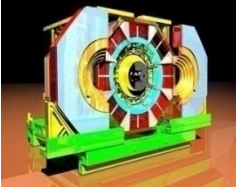
By examining number of events with only one charged track in recoil side of the D^- tags, one can estimate number of background events as well.

$$N_b^{D \text{ Decays}} = 29.0 \pm 3.4$$

$$N_b^{\text{cmb}} = 19.9 \pm 3.4$$

$$N_b^{\text{tot}} = 48.9 \pm 4.8$$

Br. & f_{D^+} at BES-III



Results:

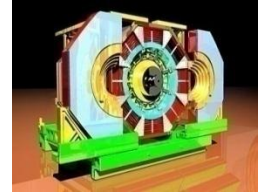
$$N(D^+ \rightarrow \mu^+ \nu) = 377.3 \pm 20.6$$

$$BF(D^+ \rightarrow \mu^+ \nu) = (3.74 \pm 0.21 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} = (203.91 \pm 5.72 \pm 1.97) \text{ MeV}$$

**These are
Preliminary !**

Source	Systematic uncertainty [%]
Number of D^- tags ($N_{D_{tag}^-}$)	0.6
Muon tracking	0.5
μ selection	0.3
$E_{\gamma_{max}}$ cut	0.7
Muon momentum cut	0.1
M_{miss}^2 cut	0.5
Background estimation	0.7
Monte Carlo statistics	0.2
Radiative correction	1.0
Total	1.7



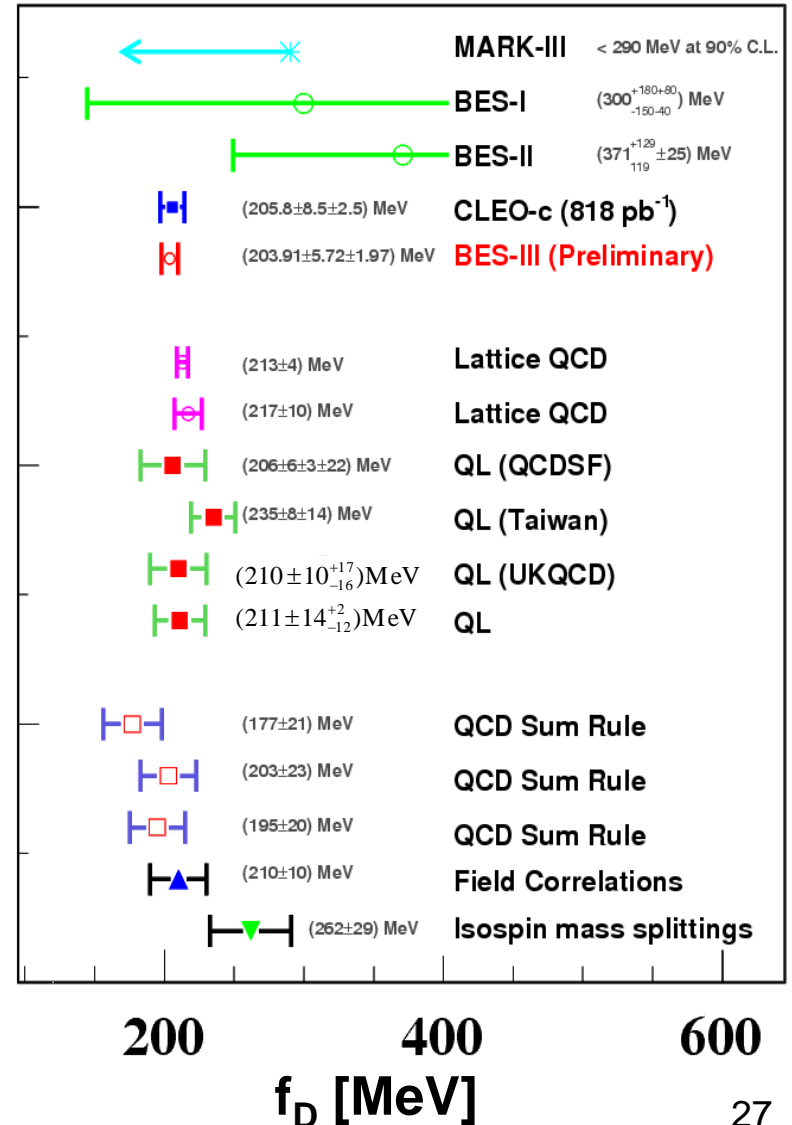
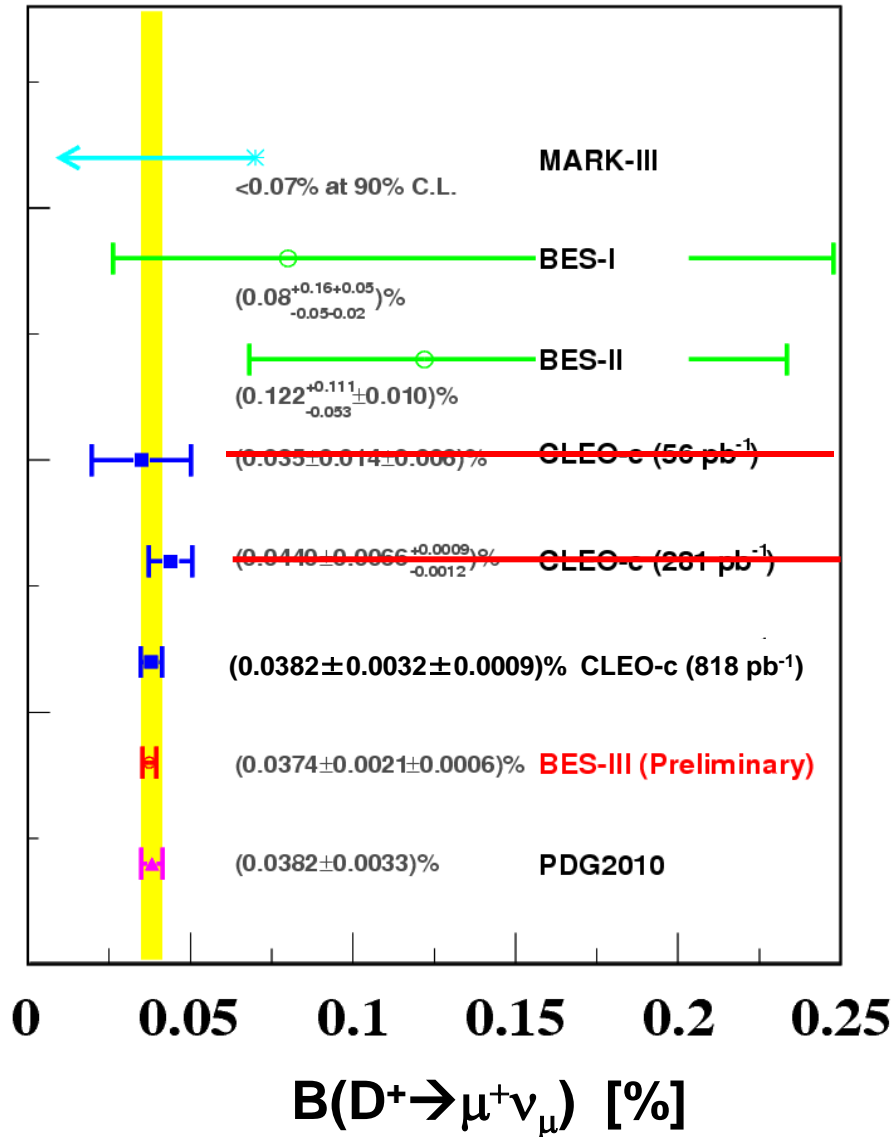
Average of Br. & f_D

Experiment	$B(D^+ \rightarrow \mu^+ \nu_\mu) (\times 10^{-4})$	Average
CLEO-c	$(3.82 \pm 0.32 \pm 0.09)$	(3.76 ± 0.18)
BES-III(PRLMNR)	$(3.74 \pm 0.21 \pm 0.06)$	

Experiment	f_D (MeV)	Average
CLEO-c	$(205.8 \pm 8.5 \pm 2.5)$	(204.5 ± 5.0)
BES-III(PRLMNR)	$(203.91 \pm 5.72 \pm 1.97)$	

At present, the error is still dominated by statistics, needing more data to be taken at 3.773 GeV to reduce the error.

Comparison of $B(D^+ \rightarrow \mu^+ \nu)$ & f_D



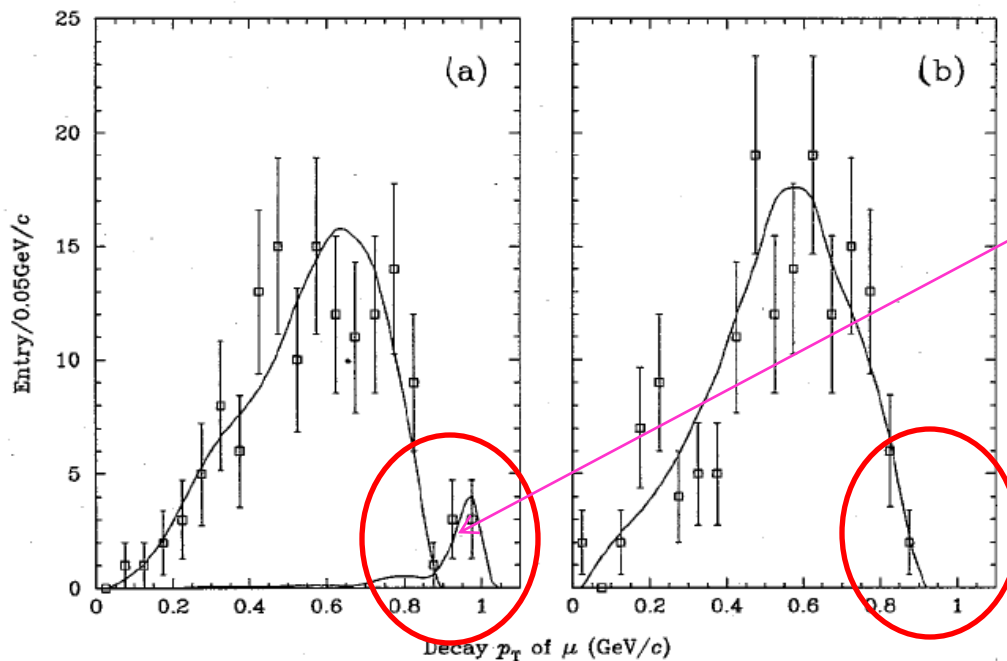
D_s^+ leptonic decays

$D_s^+ \rightarrow l^+ \nu$ at WA75 Experiment

Fixed target experiment

PTP,89, 131(1993)

A π^- beam is incident on an emulsion target and muon is required in the online trigger.



They found 9.1 ± 3.8
 $D_s^+ \rightarrow \mu^+ \nu$ decays

$$B(D_s^+ \rightarrow \mu^+ \nu) = (0.40_{-0.14-0.06}^{+0.18+0.08} \pm 0.18)\%$$

$$f_{D_s^+} = 232 \pm 45 \pm 20 \pm 48 \text{ MeV}$$

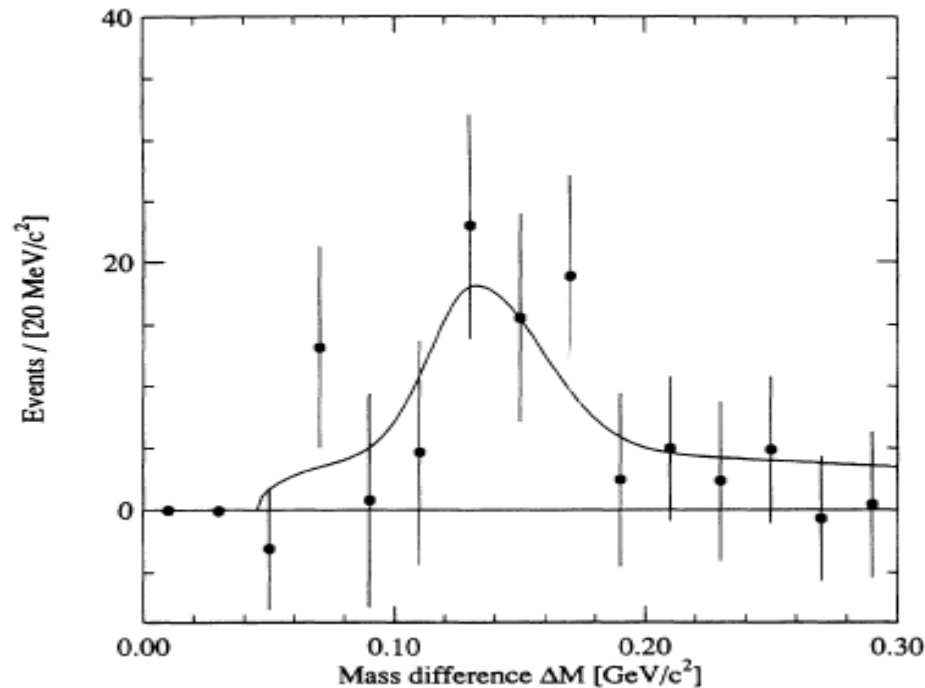
This is the first measurement of f_{D_s} . But, it is not an absolute measurement.

Charged D decays

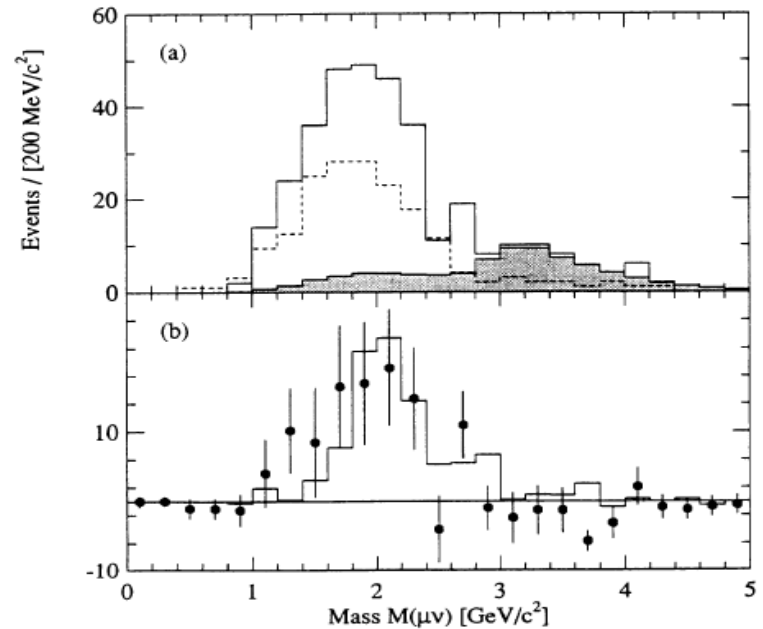
Neutral D decays

$D_s^+ \rightarrow l^+ \nu$ at CLEO II

In 1994, the CLEO II observed 38 ± 10 events for $D_s^{*+} \rightarrow \gamma D_s^+$ followed by $D_s^+ \rightarrow \mu^+ \nu$ by analyzing 2.13 fb^{-1} data taken at 10.6 GeV.



PRD49, 5690 (1994)



$$f_{D_s^+} = 344 \pm 37 \pm 52 \pm 42 \text{ MeV}$$

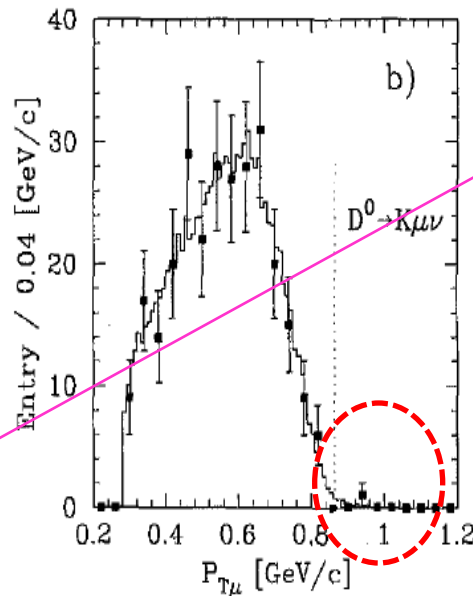
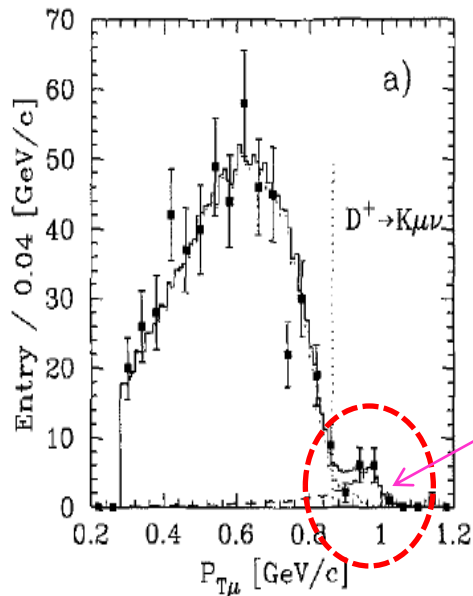
It is not an absolute measurement.

$D_s^+ \rightarrow l^+ \nu$ at E653 Experiment

Fermilab fixed target experiment

PLB,382, 299(1996)

A π^- beam is incident on an emulsion target and muon is required in the online trigger.



They found 23 $D_s^+ \rightarrow \mu^+ \nu$

$$B(D_s^+ \rightarrow \mu^+ \nu) = (0.30 \pm 0.12 \pm 0.06 \pm 0.05)\%$$

$$f_{D_s^+} = 194 \pm 35 \pm 20 \pm 14 \text{ MeV}$$

Charged D decays

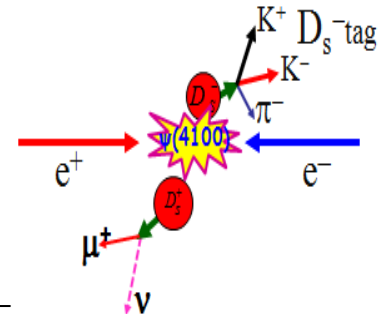
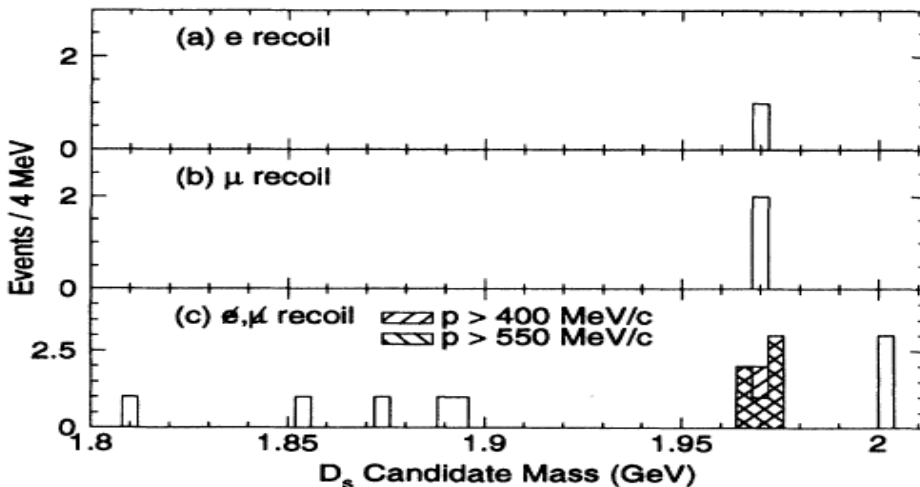
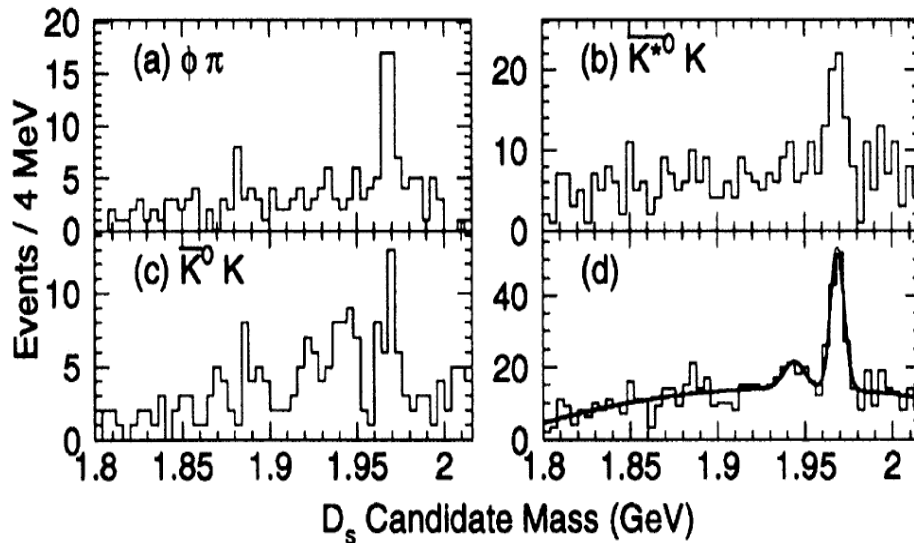
Neutral D decays

It is not an absolute measurement, it needs branching fraction for $D_s^+ \rightarrow \phi \pi^+$ to make normalization

$D_s^+ \rightarrow l^+ \nu$ at BES-I

PRL74, 4599 (1995)

22.3 pb⁻¹ @4.03 GeV



$$e^+e^- \rightarrow D_s^+ D_s^-$$

3 singly tagged D_s^- modes
94 singly tagged D_s^-

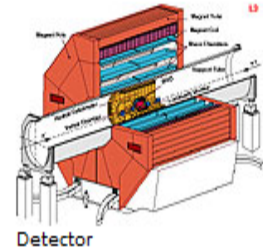
3 events for $D_s^+ \rightarrow l^+ \nu$

$$B(D_s^+ \rightarrow \mu^+ \nu) = (1.5_{-0.6-0.2}^{+1.3+0.3})\%$$

$$f_{D_s^+} = 430_{-130-40}^{+150+40} \text{ MeV}$$

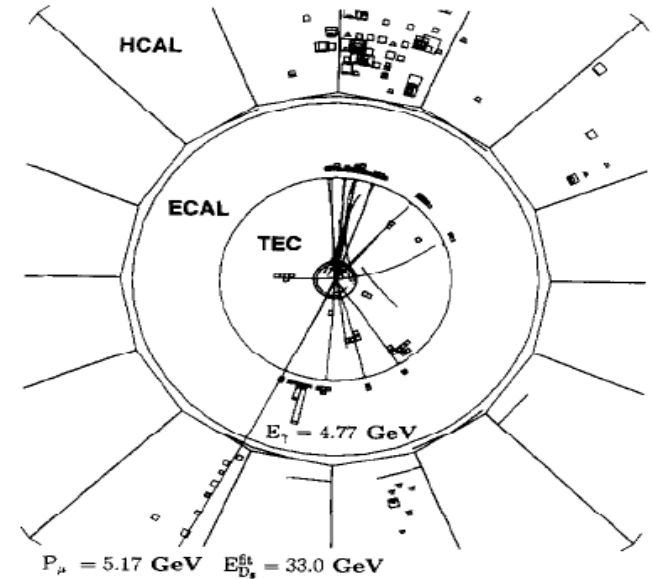
It is the first absolute measurement.

$D_s^+ \rightarrow \tau^+ \nu$ at L3 Experiment



LB396P, 327 (1997)

$D_s^+ \rightarrow \tau^+ \nu$ selected from analysis of fragmentation and decay chain
 $Z \rightarrow c\bar{c}$, $c\bar{c} \rightarrow D_s^{*-}$ followed by
 $D_s^{*-} \rightarrow \gamma D_s^-$, $D_s^- \rightarrow \tau^- \nu$, $\tau^- \rightarrow l^- \nu \nu$

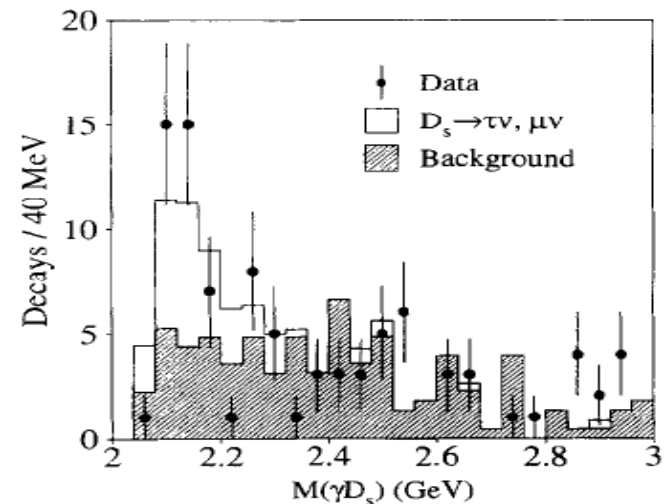


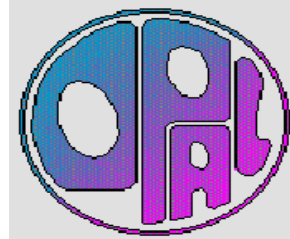
1.5×10^6 $Z \rightarrow q\bar{q}(\gamma)$ events

15.6 ± 6.0 $D_s^+ \rightarrow \tau^+ \nu$ events

$B(D_s^+ \rightarrow \tau^+ \nu) = (7.4 \pm 2.8 \pm 1.6 \pm 1.8)\%$

$f_{D_s^+} = 309 \pm 58 \pm 33 \pm 38$ MeV





$D_s^+ \rightarrow \tau^+ \nu$ at OPAL

PLB516 236 (2001)

The measurements were made based on reconstruction of decay sequence

$$\begin{aligned}
 e^+e^- &\rightarrow Z \rightarrow c\bar{c} \rightarrow D_s^{*-} X \\
 &\quad \hookrightarrow \gamma D_s^- \\
 &\quad \quad \hookrightarrow \tau \bar{\nu}_\tau \\
 &\quad \quad \quad \hookrightarrow \ell^- \bar{\nu}_\ell \nu_\tau \quad (\ell = e, \mu)
 \end{aligned}$$

3.9×10^6 $Z \rightarrow qq\text{-bar}(\gamma)$ events

22.5 ± 6.9 $D_s^+ \rightarrow \tau^+ \nu$ events

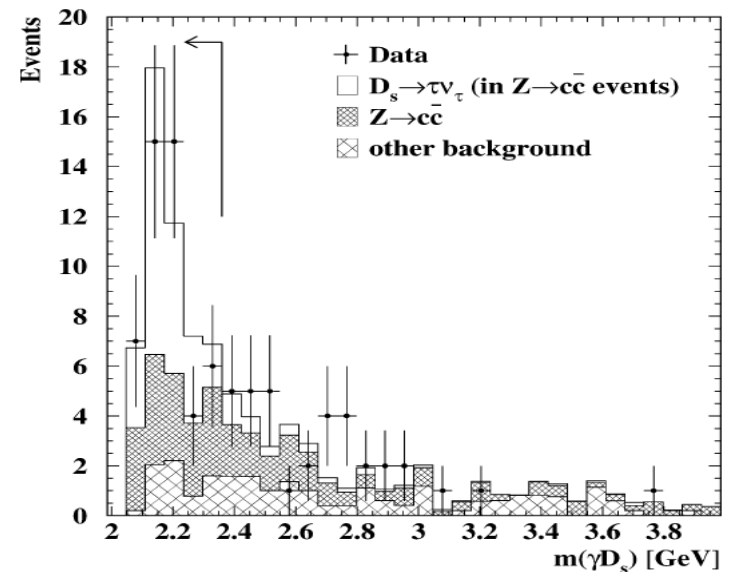
$B(D_s^+ \rightarrow \tau^+ \nu) = (7.0 \pm 2.1 \pm 2.0)\%$

$f_{D_s^+} = 286 \pm 44 \pm 41$ MeV

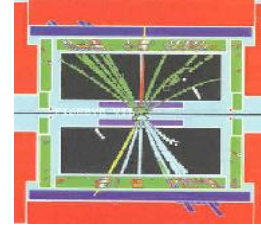
$$\vec{P}_{D_s} = - \sum_{i \neq \text{lepton}} \vec{p}_i,$$

$$E_{D_s} = \sqrt{s} - \sum_{i \neq \text{lepton}} E_i,$$

$$\sqrt{E_{D_s}^2 - P_{D_s}^2} = M_{D_s}.$$



$D_s^+ \rightarrow \tau^+ \nu$ at ALEPH



PLB528, 1 (2002)

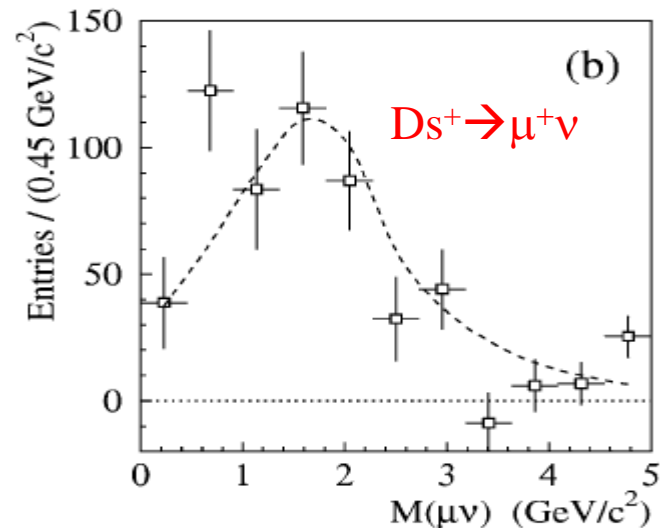
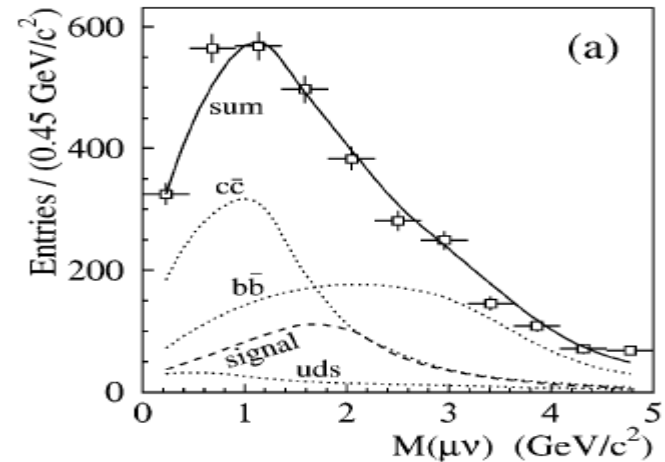
The measurements were made based on almost the same technique as used by L3 and OPAL. But the ALEPH reconstructed the $D_s^+ \rightarrow \mu^+ \nu$ decay in their invariant mass.

3.97×10^6 hadronic Z decays

$$B(D_s^+ \rightarrow \tau^+ \nu) = (5.79 \pm 0.77 \pm 1.84)\%$$

$$B(D_s^+ \rightarrow \mu^+ \nu) = (0.68 \pm 0.11 \pm 0.18)\%$$

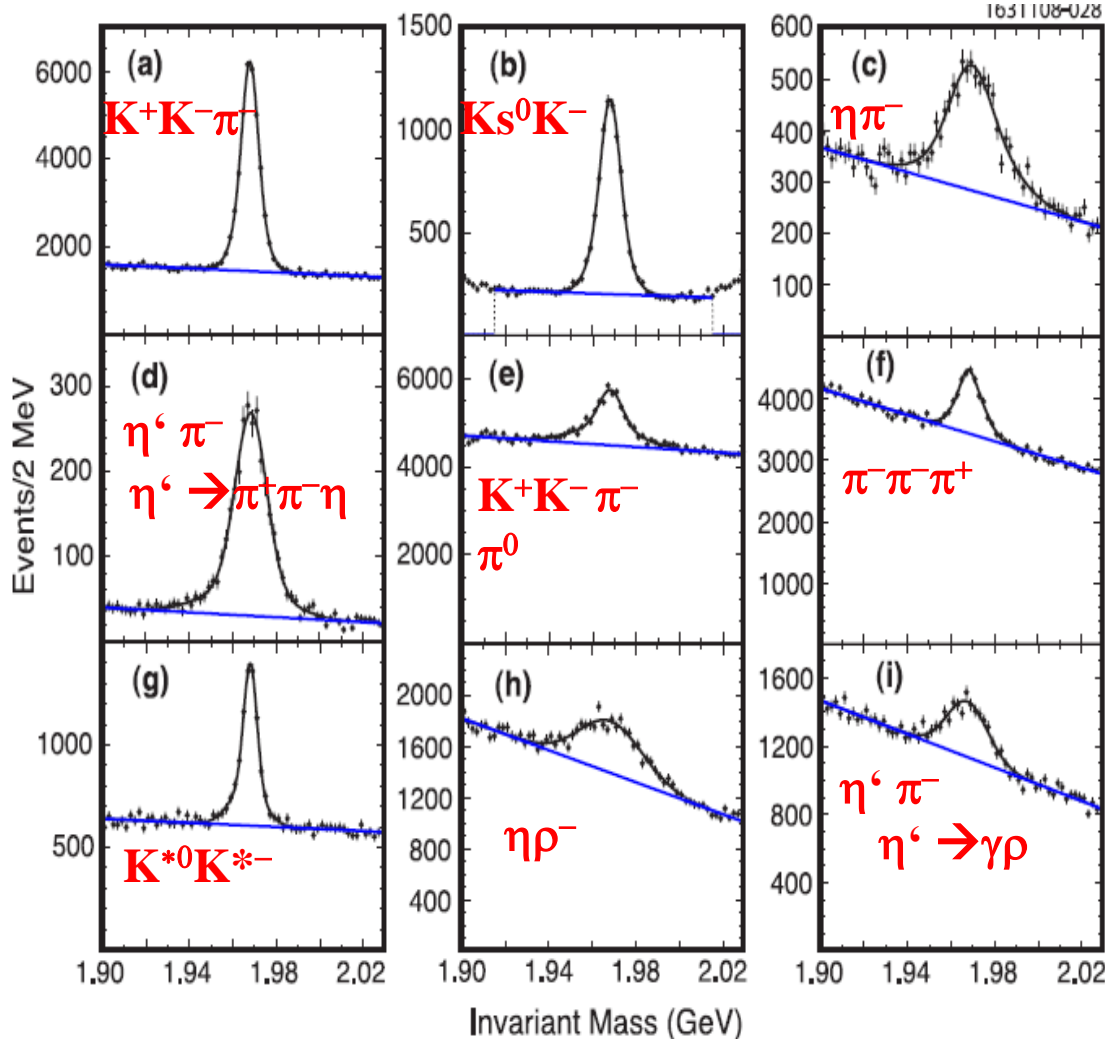
$$f_{D_s^+} = 285 \pm 19 \pm 40 \text{ MeV}$$



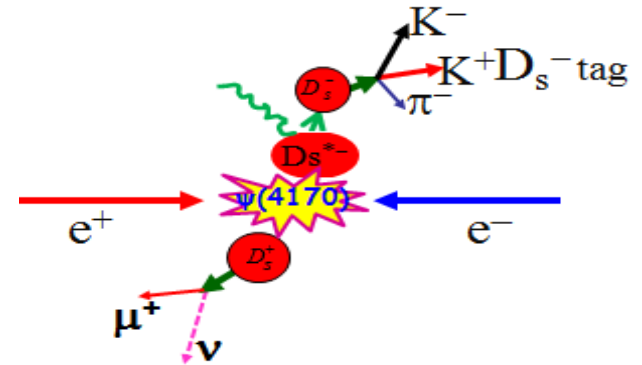


D_s^- tags at CLEO-c

PRD79, 052001 (2009)



$600 \text{ pb}^{-1} @ 4.170 \text{ GeV}$

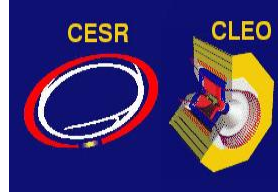


$$e^+e^- \rightarrow D_s^+ D_s^{*-}$$

$$D_s^{*-} \rightarrow \gamma D_s^-$$

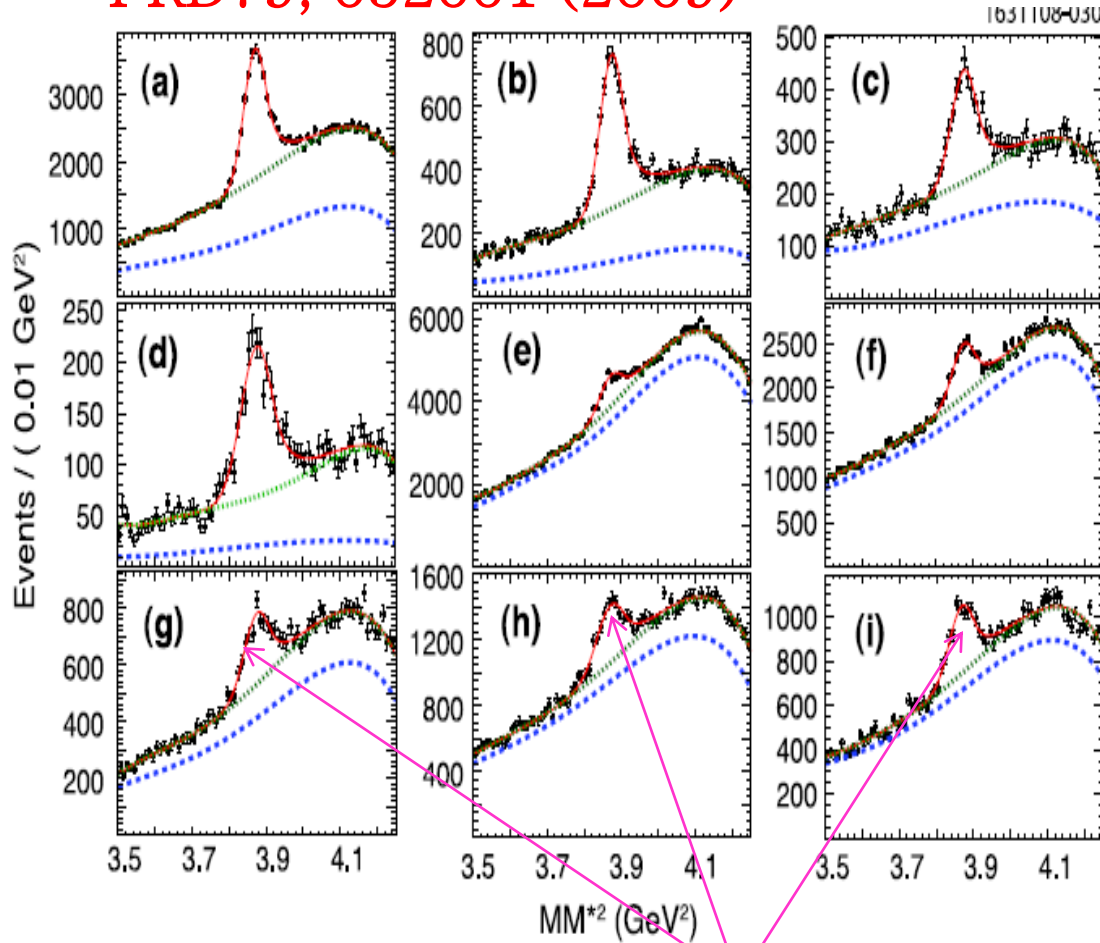
**9 singly tagged
 D_s^- modes**

Absolute measurement.



D_s^{*-} tags at CLEO-c

PRD79, 052001 (2009)



Needing reconstruction of D_s^{*-}

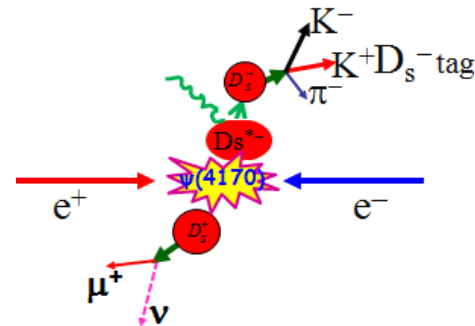
$$e^+e^- \rightarrow D_s^+ D_s^{*-}$$

$$D_s^{*-} \rightarrow \gamma D_s^-$$

$$MM^2 = (E_{CM} - E_{D_s^-} - E_\gamma)^2 - (-\vec{p}_{CM} - \vec{p}_{D_s^-} - \vec{p}_\gamma)^2$$

MM^{*2} is the missing mass square of the system recoiling against the γD_s^-

These peaks indicate that the D_s^{*-} are well reconstructed





$D_s^+ \rightarrow l^+ \nu$ at CLEO-c

PRD79, 052001 (2009)

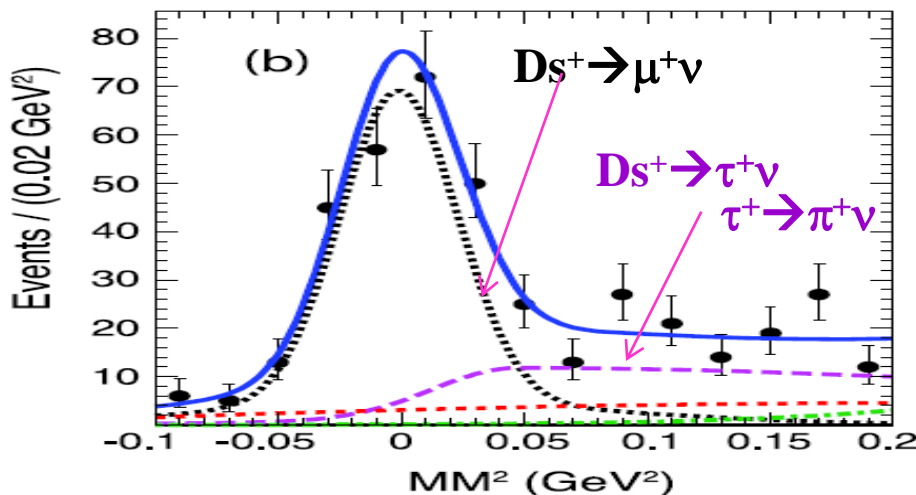
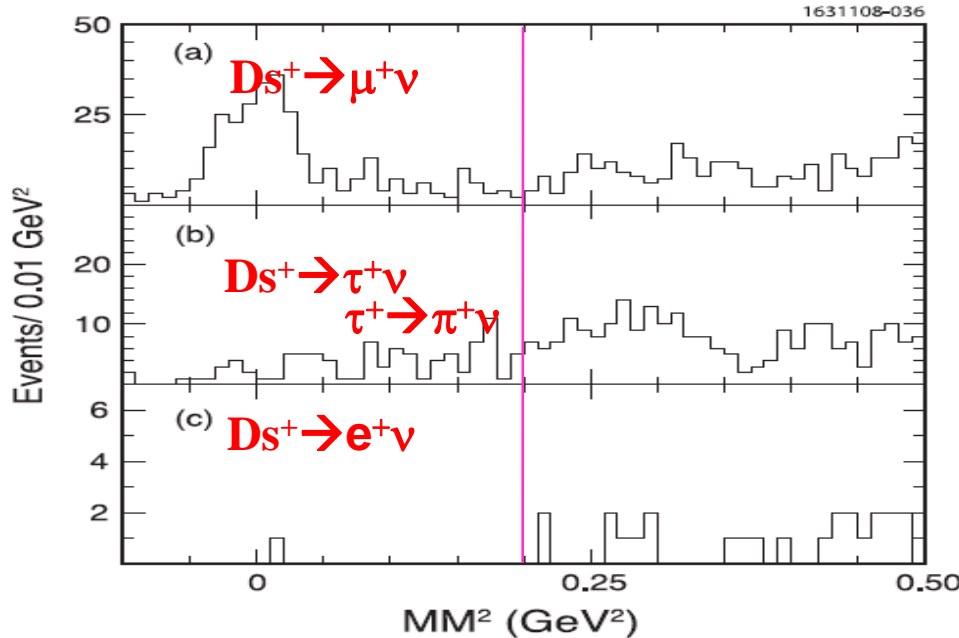
$$MM^2 = (E_{\text{CM}} - E_{D_S^-} - E_\gamma - E_\mu)^2 - (-\vec{p}_{\text{CM}} - \vec{p}_{D_S^-} - \vec{p}_\gamma - \vec{p}_\mu)^2$$

$$B(D_s^+ \rightarrow \mu^+ \nu) = (0.591 \pm 0.037 \pm 0.018)\%$$

$$B(D_s^+ \rightarrow \tau^+ \nu) = (6.42 \pm 0.81 \pm 0.18)\%$$

$$f_{D_s^+} = 263.3 \pm 8.2 \pm 3.9 \text{ MeV}$$

Absolute measurement.

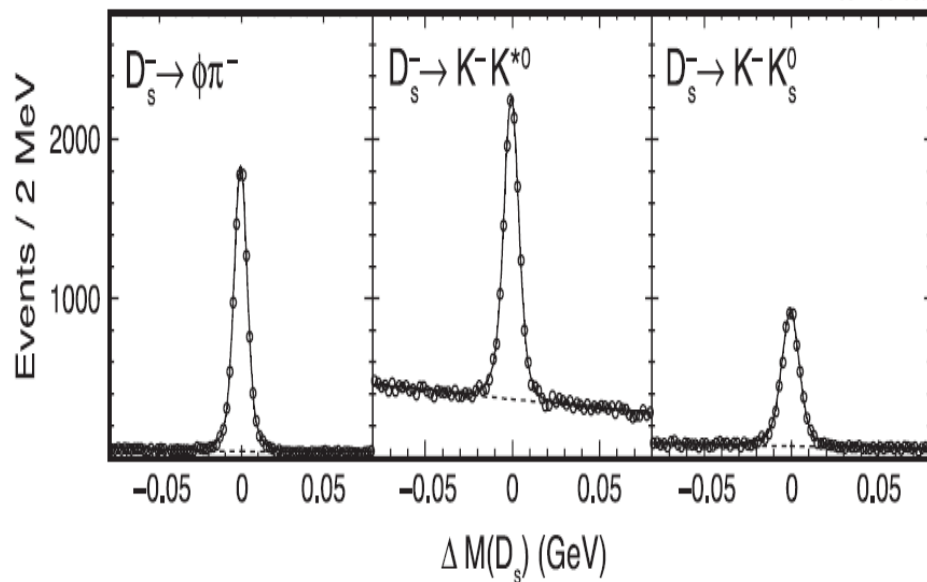




$D_s^+ \rightarrow \tau^+ \nu$ at CLEO-c

600 pb⁻¹ PRD79, 052002 (2009)

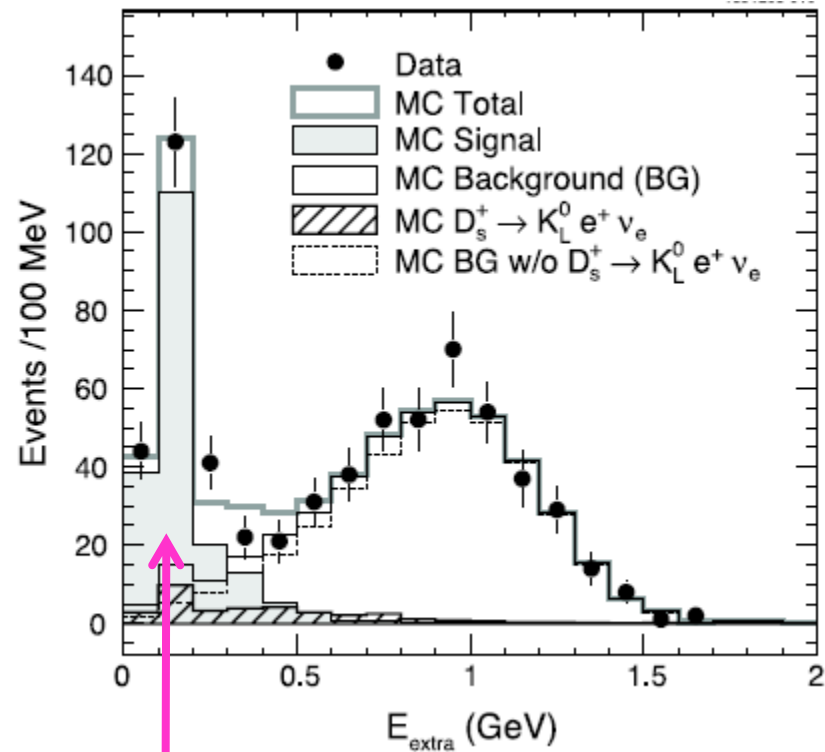
$D_s^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow e^+ \nu \nu$



Three cleanest single tag Ds mode were used

$$f_{D_s^+} = 252.5 \pm 11.1 \pm 5.2 \text{ MeV}$$

Absolute measurement.



Signal for $D_s^+ \rightarrow \tau^+ \nu$

E_{extra} is the total energy of rest of the event measured in the electromagnetic calorimeter

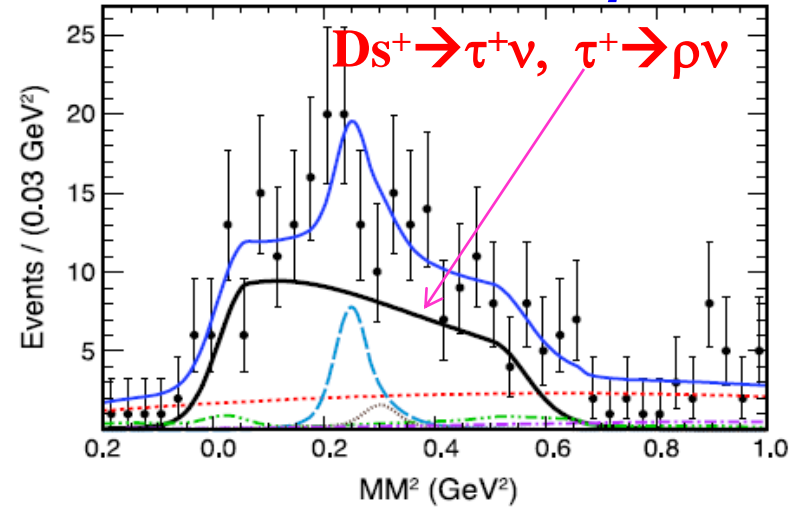
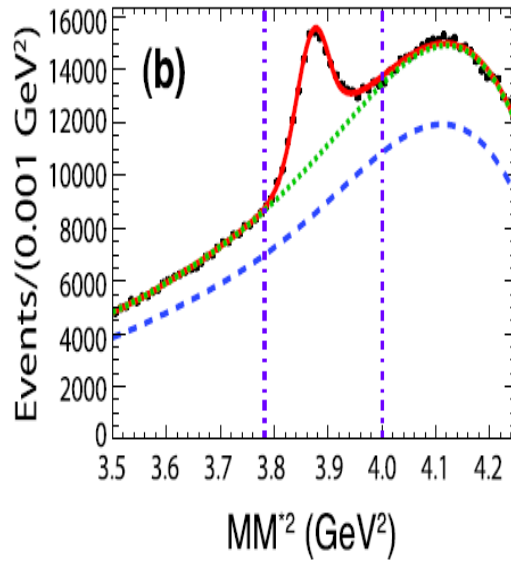
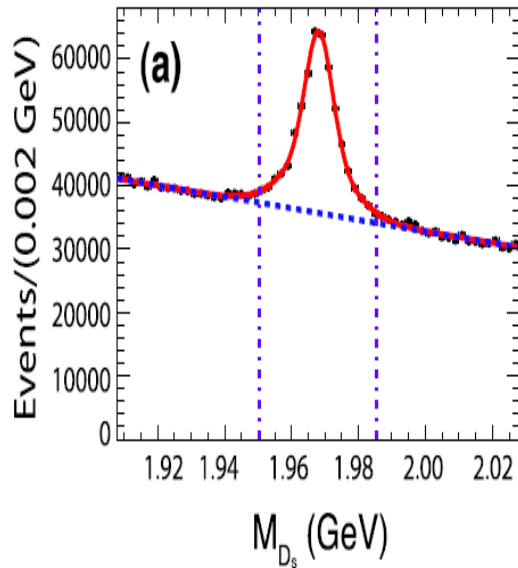


$D_s^+ \rightarrow \tau^+ \nu$ at CLEO-c

PRD80, 112004 (2009)

D_s^- tags

$600 \text{ pb}^{-1} \quad D_s^+ \rightarrow \tau^+ \nu, \tau^+ \rightarrow \rho \nu$



$$B(D_s^+ \rightarrow \tau^+ \nu)$$

$$= (5.52 \pm 0.57 \pm 0.21)\%$$

$$f_{D_s^+} = 257.8 \pm 13.3 \pm 5.2 \text{ MeV}$$

Absolute measurement.

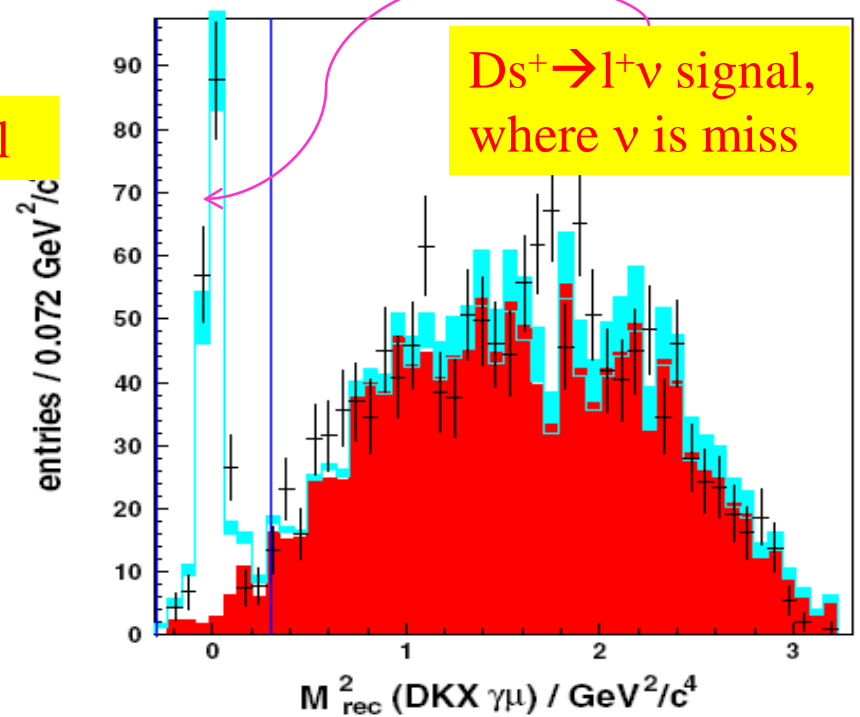
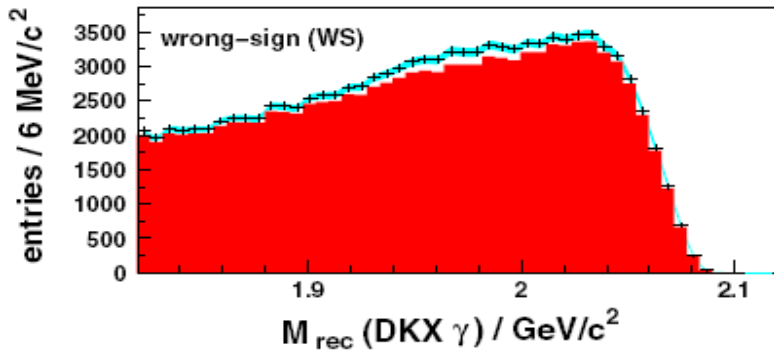
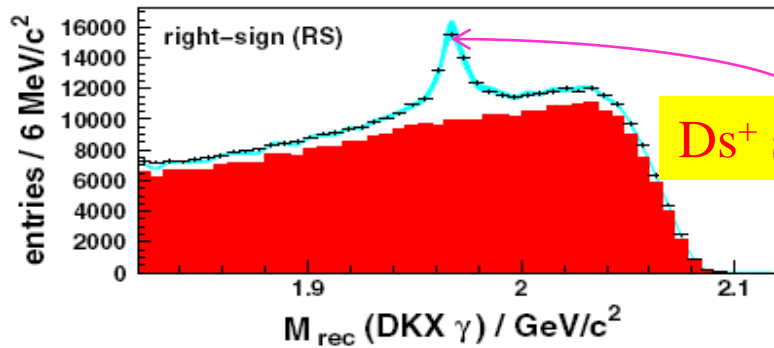
$D_s^+ \rightarrow l^+ \nu$ at Belle

$e^+e^- \rightarrow cc\text{-bar}$ events

PRL100, 241801(2008)

$e^+e^- \rightarrow D_S^* D^{\pm,0} K^{\pm,0} X, D_S^* \rightarrow \gamma D_S, X = n\pi(\gamma)$

548 fb-1 @ 10.6 GeV



$$N_{D_S}^{\text{REC}} = 32100 \pm 870(\text{stat}) \pm 1210(\text{syst})$$

$$B(D_S^+ \rightarrow \mu^+ \nu) = [0.644 \pm 0.076 \pm 0.057]\%$$

$$N_{\mu\nu}^{\text{REC}} = 169 \pm 16(\text{stat}) \pm 8(\text{syst})$$

$$f_{D_S^+} = [275 \pm 16 \pm 12] \text{ MeV}$$

Absolute measurement.

$D_s^+ \rightarrow l^+ \nu$ at BaBar

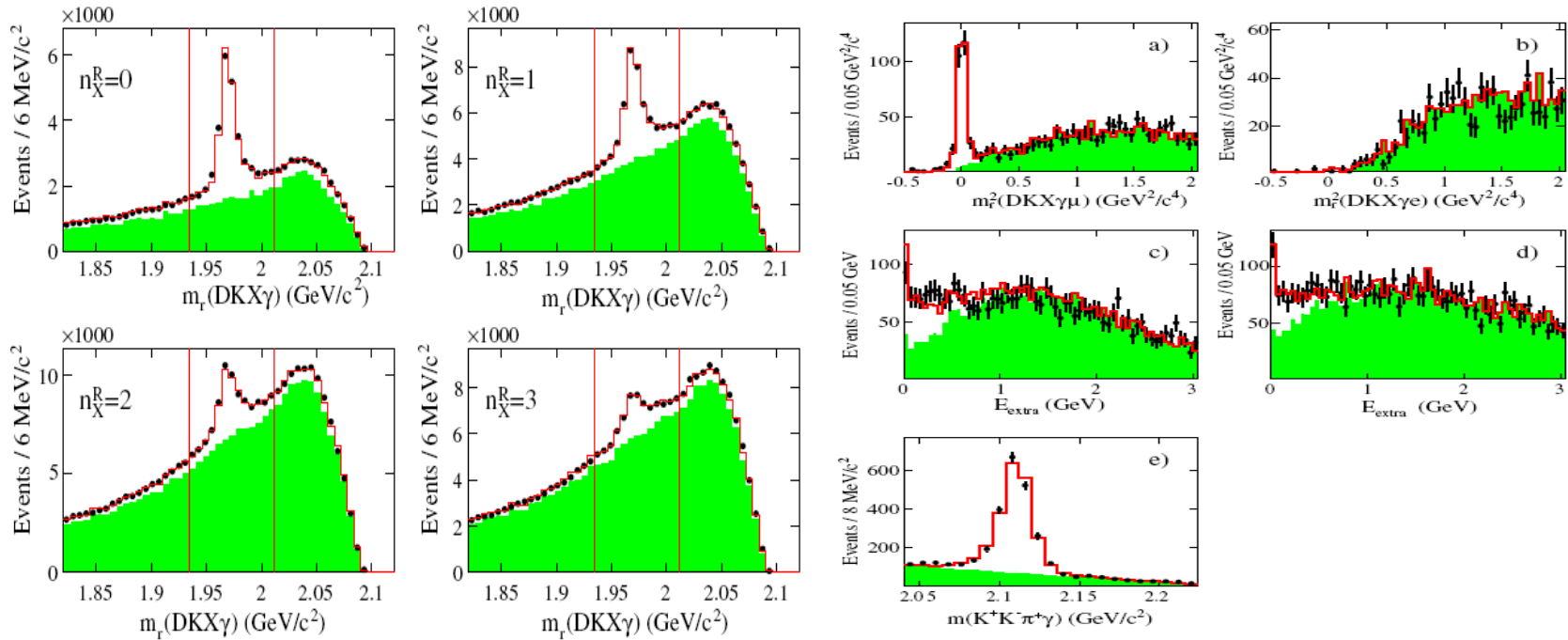


$e^+e^- \rightarrow cc\text{-bar}$ events

PRD82, 091103(R) (2010)

$e^+e^- \rightarrow D_s^* D^{\pm,0} K^{\pm,0} X, D_s^* \rightarrow \gamma D_s, X = n\pi(\gamma)$

521fb⁻¹ @ 10.6 GeV



$$B(D_s^+ \rightarrow \mu^+ \nu) = [0.602 \pm 0.038 \pm 0.034] \%$$

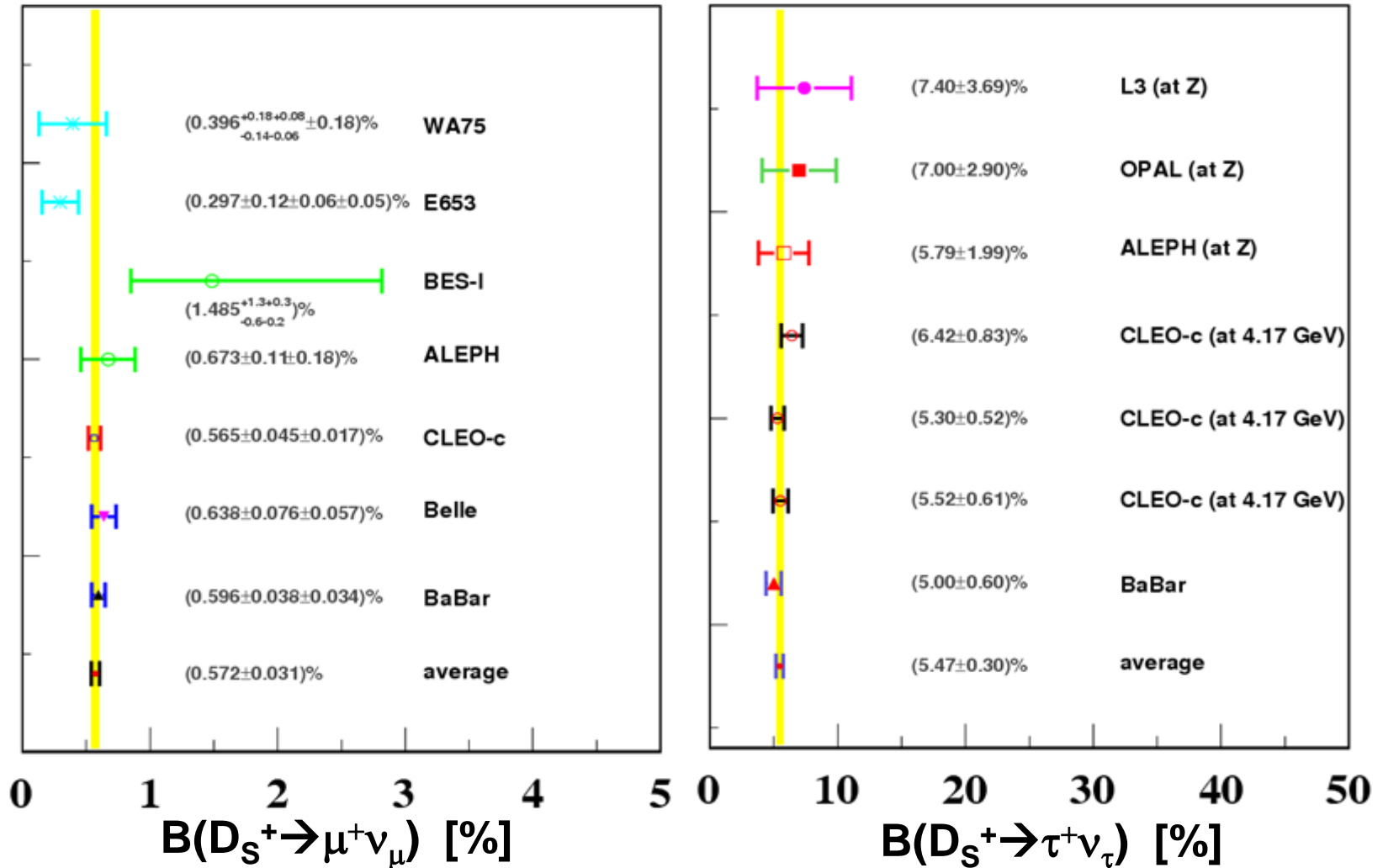
$$B(D_s^+ \rightarrow \tau^+ \nu) = [5.07 \pm 0.52 \pm 0.68] \% \quad (\tau^+ \rightarrow e \nu \nu)$$

$$B(D_s^+ \rightarrow \tau^+ \nu) = [4.91 \pm 0.47 \pm 0.54] \% \quad (\tau^+ \rightarrow \mu \nu \nu)$$

$$f_{D_s^+} = (258.6 \pm 6.4 \pm 7.5) \text{ MeV}$$

Absolute measurement.

Comparison of the measured Br.

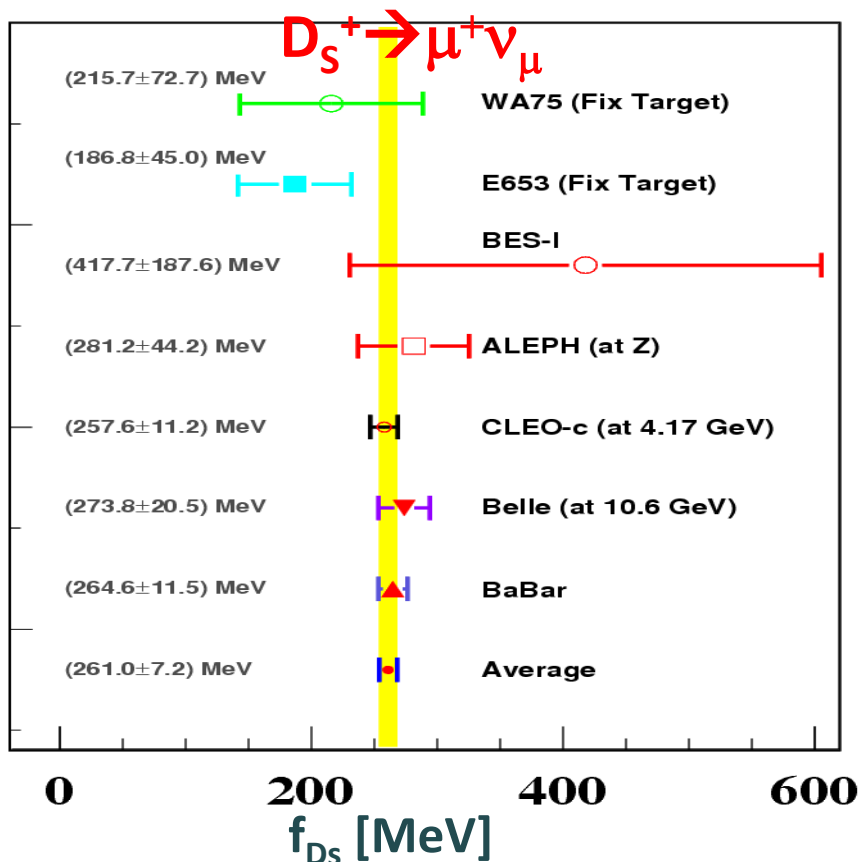


$B(D_S^+ \rightarrow \tau^+ \nu_\tau) = (0.572 \pm 0.031)\%$

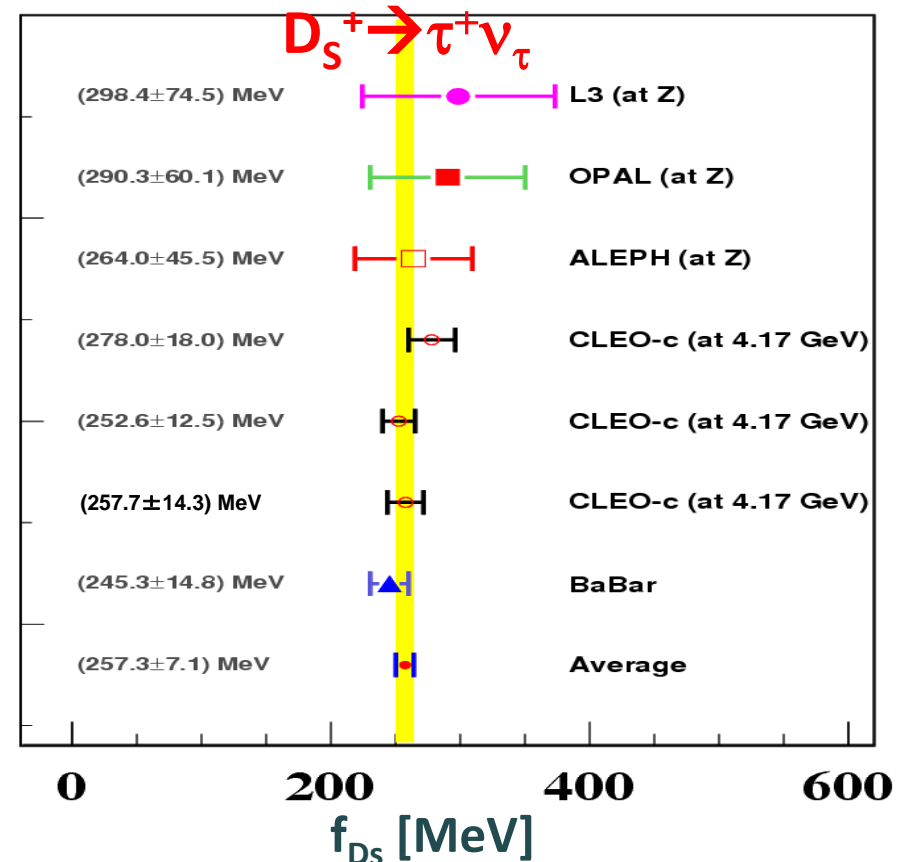
$B(D_S^+ \rightarrow \tau^+ \nu_\tau) = (5.45 \pm 0.30)\%$

Comparison of the measured f_{D_S}

Based on the measured branching fractions of D_S^+ leptonic decays (after radiative correction), and with inputs of D_S^+ mass, lepton mass, D_S^+ lifetime and $|V_{cs}|=0.97345$ from CKMfiter, we calculate the f_{D_S} .



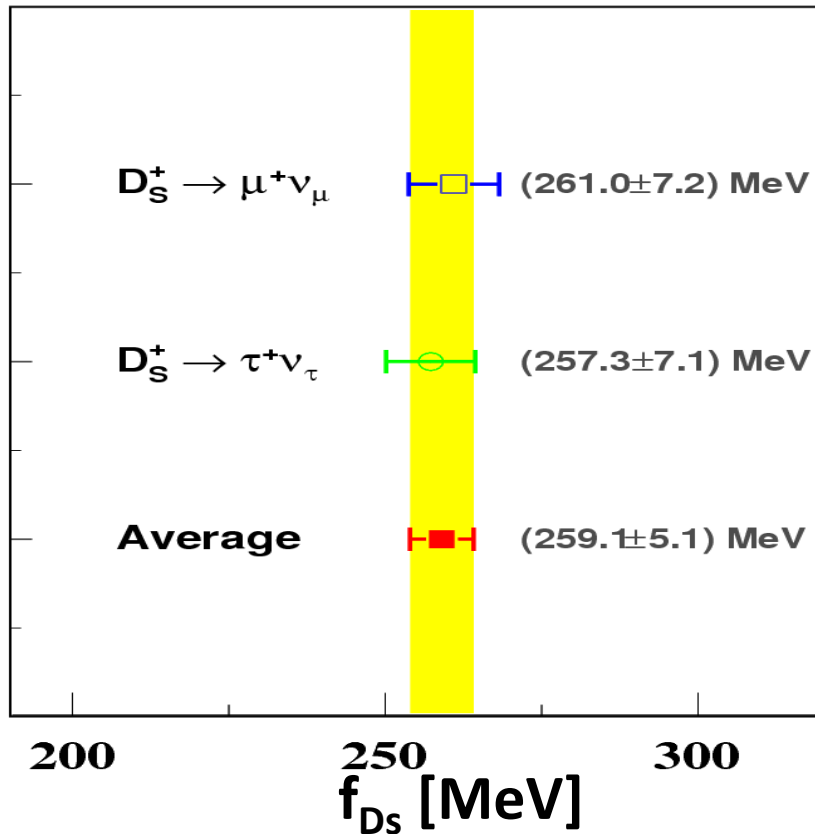
$$f_{D_S^+} = (261.0 \pm 7.2) \text{ MeV}$$



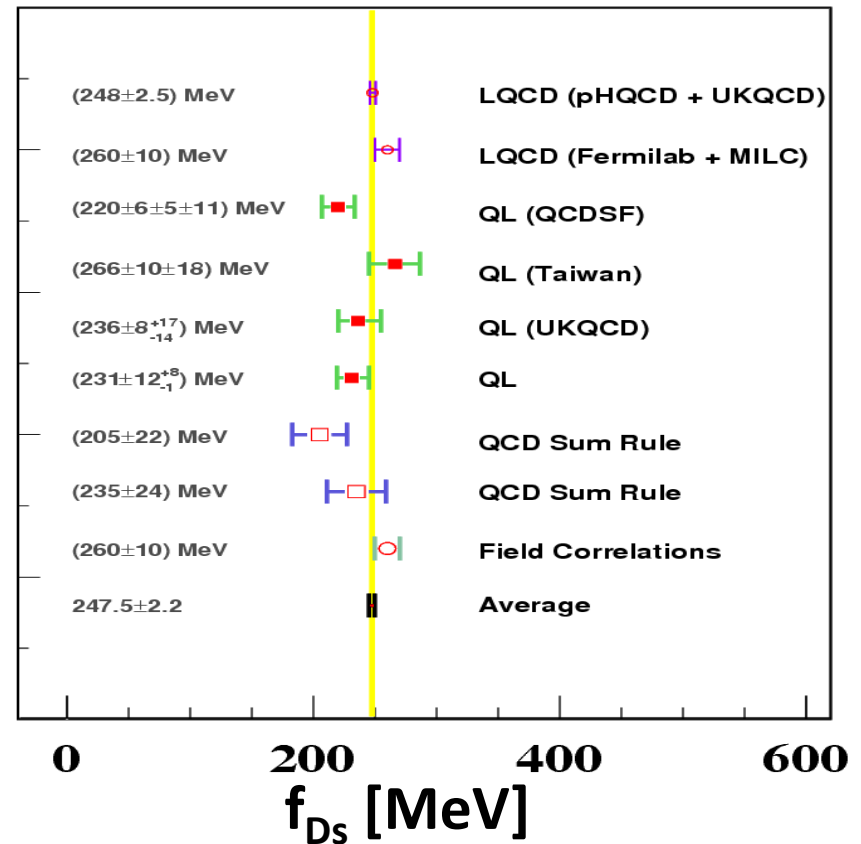
$$f_{D_S^+} = (257.3 \pm 7.1) \text{ MeV}$$

Measured & calculated f_{D_s}

f_{D_s} measured at different experiments



Calculations of f_{D_s}



$f_{D_s} = (259.1 \pm 5.1) \text{ MeV}$ (Weighted Average) | $f_{D_s} = (247.5 \pm 2.2) \text{ MeV}$ (Weighted Average)

The measured f_{D_s} is 2.09σ larger than the one expected by theories.

Comparison of f_{D_s}/f_D

Experiments

Theoretical calculations

Weighted Average

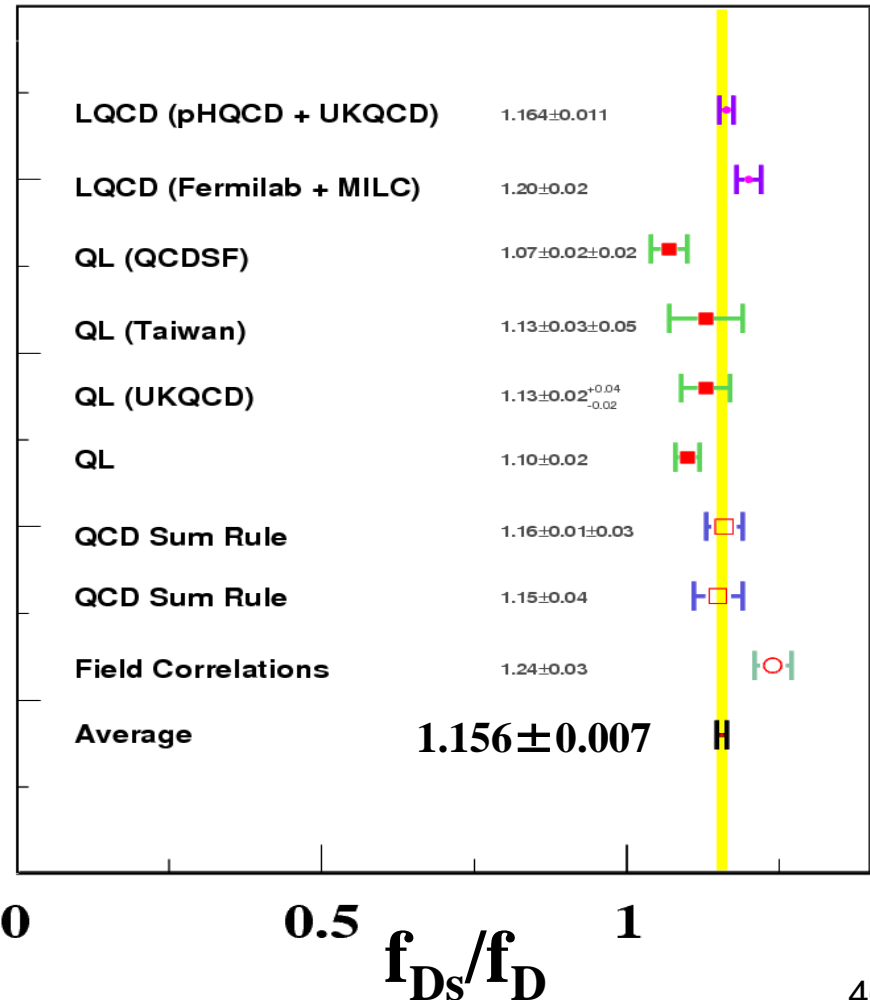
$$f_{D_s} = (259.1 \pm 5.1) \text{ MeV}$$

$$f_D = (204.5 \pm 5.0) \text{ MeV}$$



$$f_{D_s}/f_D = (1.267 \pm 0.040)$$

The measured ratio of the f_{D_s}/f_D is 2.7σ larger than that predicted by theoretical calculations



Determination of $|V_{cs}|$ and $|V_{cd}|$

$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D_{(s)}^+}^2}{8\pi} |V_{cd(s)}|^2 m_l^2 m_{D_{(s)}^+} \left(1 - \frac{m_l^2}{m_{D_{(s)}^+}^2}\right)^2$$

$f_{D(D_s)}$ can be well calculated (LQCD, ...)

$\Gamma[D_{(s)}^+ \rightarrow l^+ \nu]$ can be well measured

One can extract CKM matrix elements $|V_{cs}|$ and $|V_{cd}|$

CKM matrix element $|V_{cd}|$

The $|V_{cd}|$ could be extracted with

$$\Gamma(D^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 f_{D^+}^2}{8\pi} |V_{cd}|^2 m_l^2 m_{D^+} \left(1 - \frac{m_l^2}{m_{D^+}^2}\right)^2$$

Inserting the quantities

$$\tau_{D^+} = (1040 \pm 7) \text{ fs},$$

$$M_{D^+} = (1896.60 \pm 0.16) \text{ MeV}$$

$$M_{\mu^+} = (105.658 \pm 0.000) \text{ MeV}$$

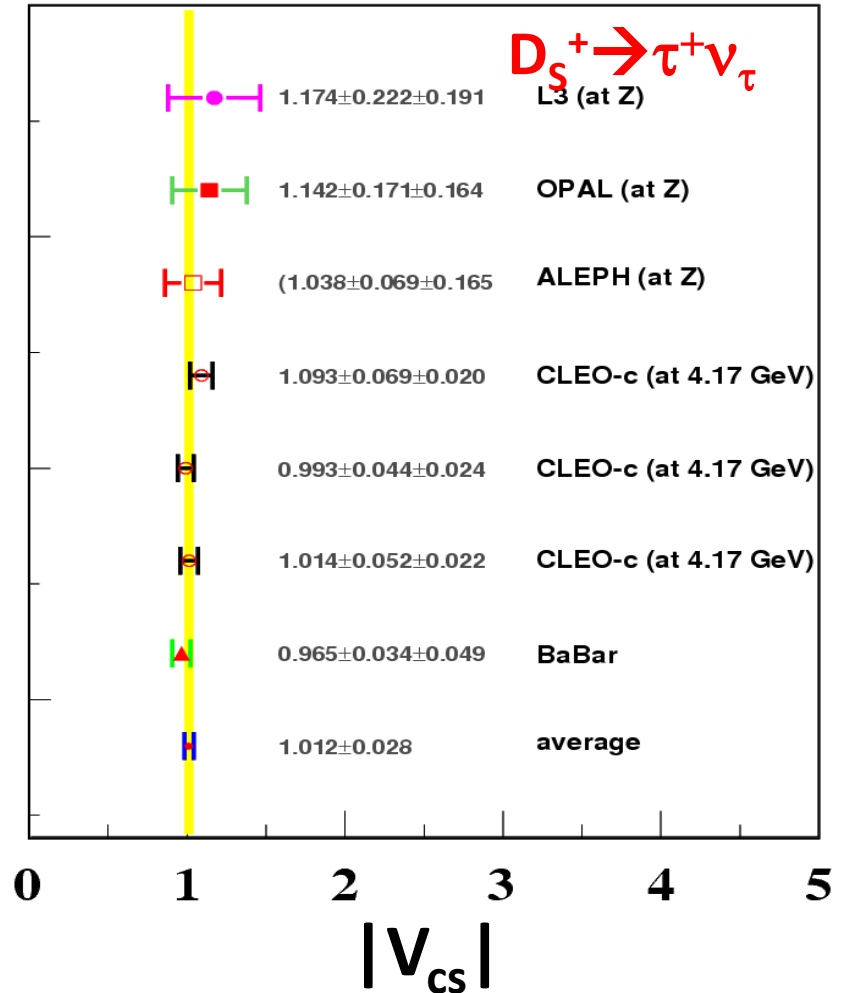
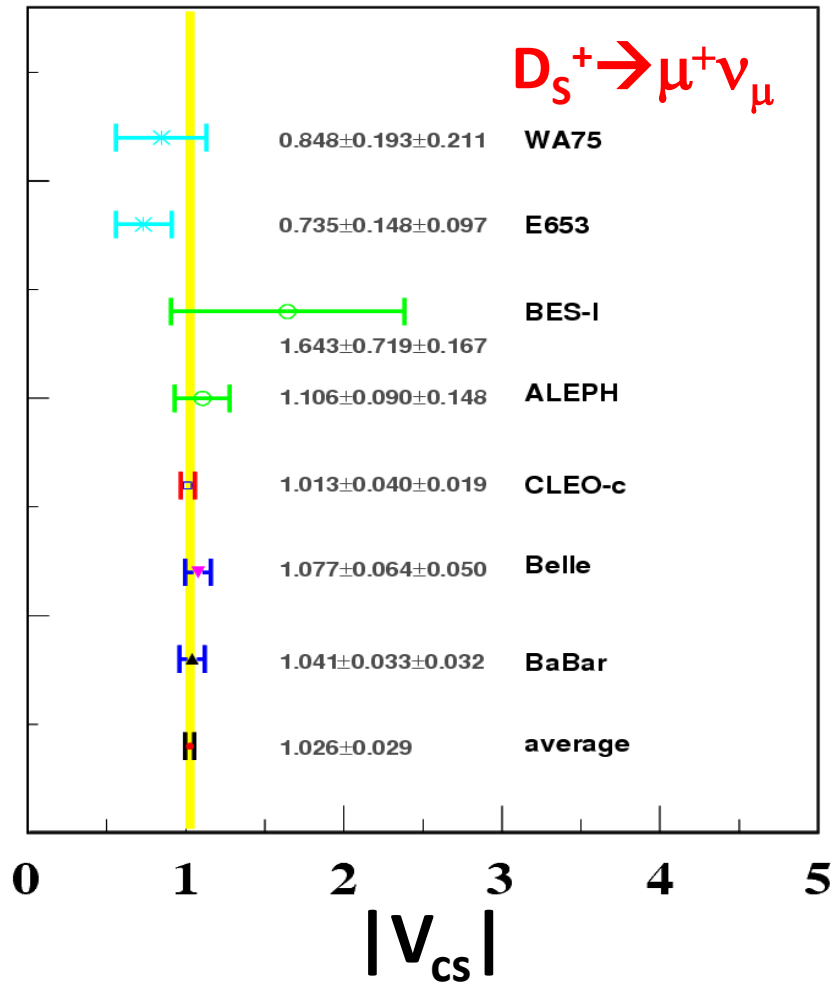
$$f_{D^+} = 207 \pm 4 \text{ MeV (from LQCD)}$$

yields

$$|V_{cd}| = (0.222 \pm 0.006 \pm 0.005) \text{ (BES-III Preliminary)}$$

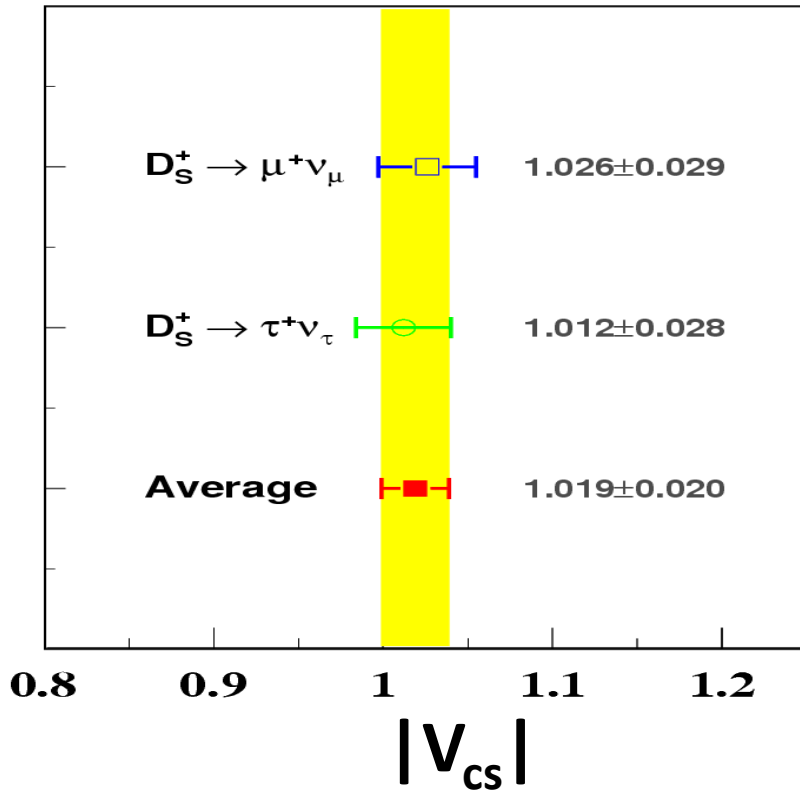
From $D^+ \rightarrow \mu^+ \nu$ leptonic decay

CKM matrix element $|V_{cs}|$



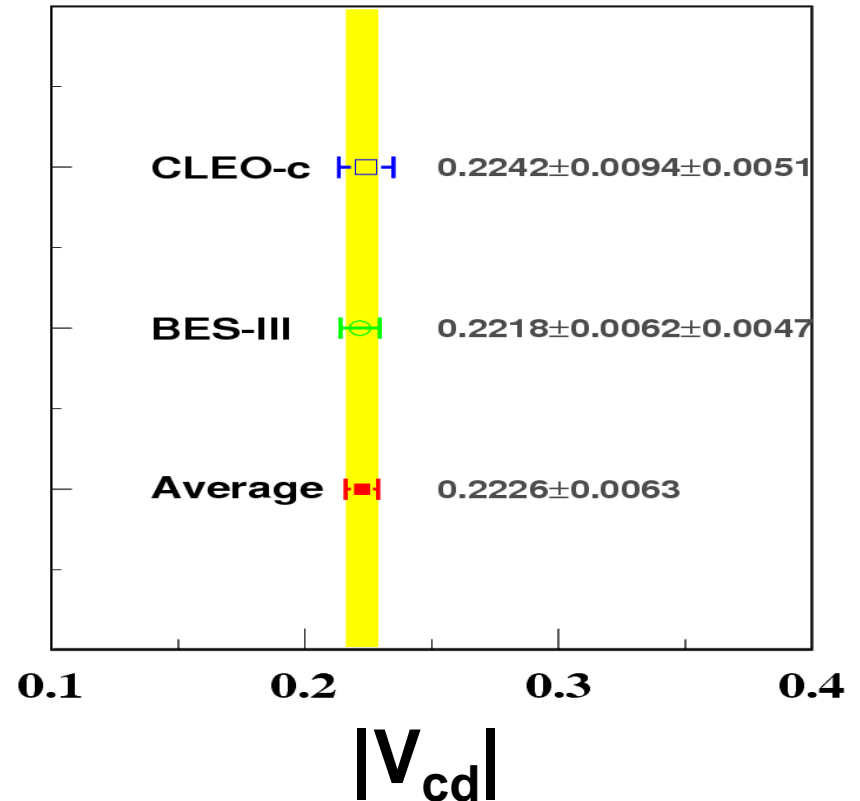
In the calculation we use $f_{D_S} = (247.5 \pm 2.2)$ MeV (the average of calculations)

$|V_{cs}|$ & $|V_{cd}|$



$$|V_{cs}| = 1.019 \pm 0.020$$

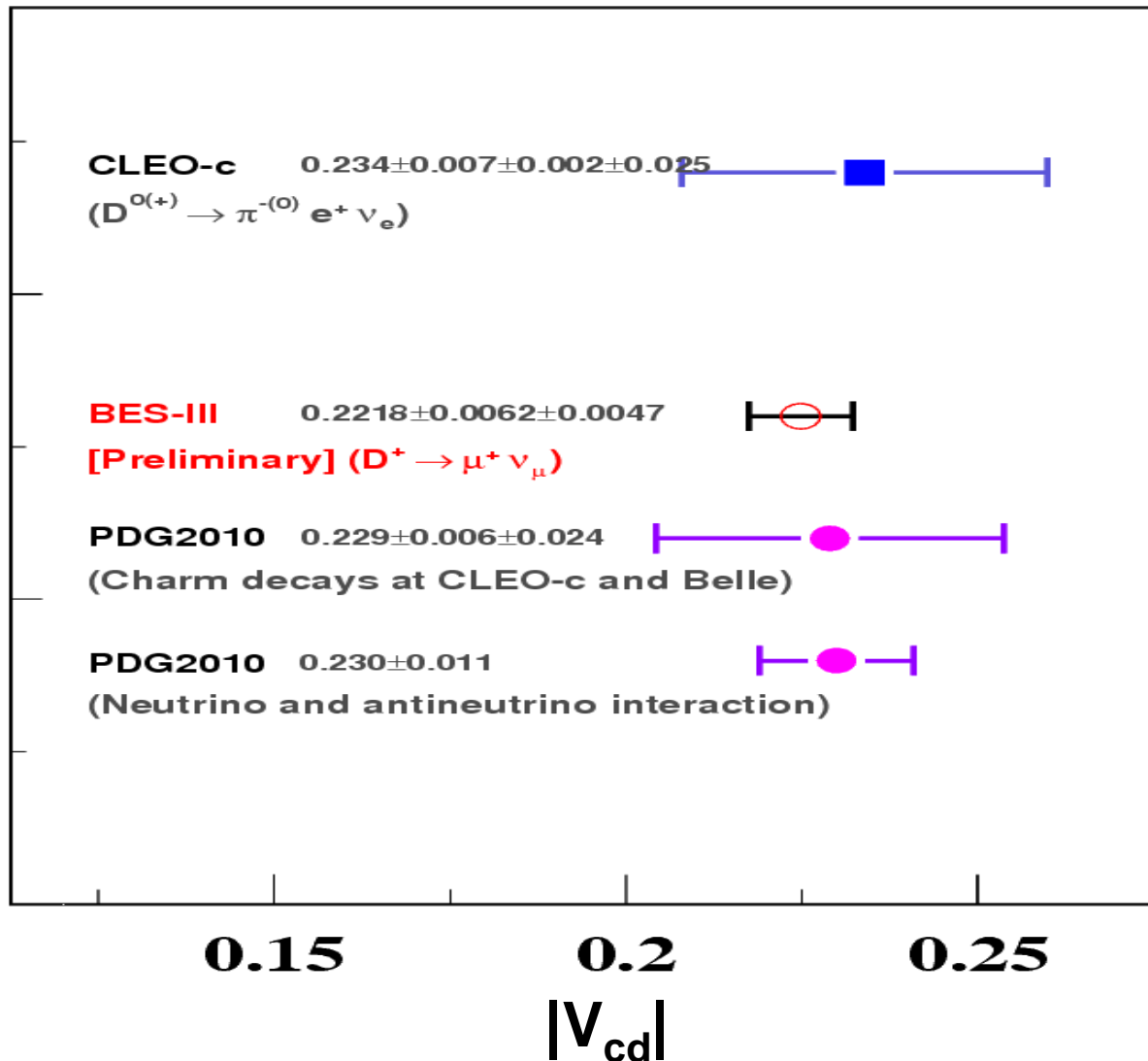
From D_S^+ leptonic decays



$$|V_{cd}| = 0.223 \pm 0.006$$

From D^+ leptonic decays

Comparison of $|V_{cd}|$



The most
precise
determination
of $|V_{cd}|$ is
from the
BES-III

Discussions of $|V_{cd}|$ & $|V_{cs}|$

Carefully comparing these CKM matrix elements obtained by analyzing $D_{(s)}^+$ leptonic decays with these obtained by analyzing D meson semileptonic decays provide some useful information about New Physics

Effects of nonstandard leptonic decay of D_S^+ would enhance D_S^+ leptonic decay rate, resulting in a larger $|V_{cs}|$ than that obtained from D meson semileptonic decays

Accumulating Evidence for Nonstandard Leptonic Decay of Ds Mesons

B.A. Dobressu and A.S. Kronfeld, PRL100, 241802 (2008)

If no nonstandard leptonic decay of D^+ , one would obtain the same values of $|V_{cd}|$ obtained from the D^+ leptonic decays and D semileptonic decays.

Discussions of $|V_{cd}|$ & $|V_{cs}|$

$$|V_{cs}|_{\text{CKMfitter}} = (0.973 \pm 0.001) \text{ from CKMfitter}$$

$$|V_{cs}|_{D_S^+ \rightarrow l^+ \nu} = (1.019 \pm 0.020) \text{ from } D_S^+ \rightarrow l^+ \nu$$

$|V_{cs}|_{D_S^+ \rightarrow l^+ \nu}$ is $\sim 2.5\sigma$ larger than $|V_{cs}|_{\text{CKMfitter}}$. Does this indicate New Physics effects?

$$|V_{cd}|_{\text{CKMfitter}} = (0.225 \pm 0.001) \text{ from CKMfitter}$$

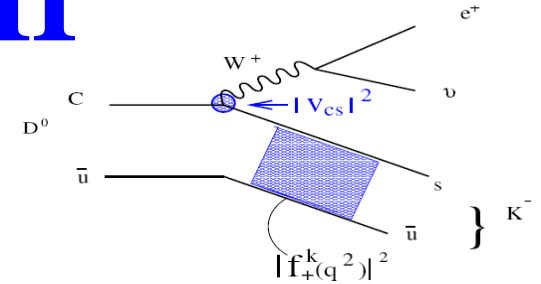
$$|V_{cd}|_{D^+ \rightarrow l^+ \nu} = (0.223 \pm 0.006) \text{ from } D^+ \rightarrow l^+ \nu$$

$|V_{cd}|_{D^+ \rightarrow l^+ \nu}$ is consistent within error with $|V_{cd}|_{\text{CKMfitter}}$.

We need to examine D semileptonic decays to measure $|V_{cd}|$ & $|V_{cs}|$ as well.

$|V_{cd(s)}|$ from D semileptonic decays at BES-III

$$\frac{d\Gamma}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{cs(d)}|^2 |\vec{p}_{K(\pi)}|^2 |f_+^{K(\pi)}(q^2)|^2$$

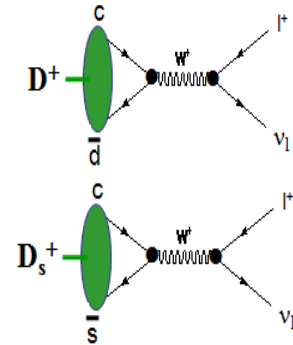


The BES-III can also determine $|V_{cs}|$ and $|V_{cd}|$ from D^0 semileptonic decays. These results will come out soon.

In BES-III Collaboration, two analysis working groups (IHEP and CMU) have been working on extracting $|V_{cs}|$ and $|V_{cd}|$ (see C.L. Liu's talk), as well as some other physical quantities related to these D meson semileptonic decays.

These would be other important results for precise test of the SM and searching for NP.

Summary



- More than 25 years studies of D leptonic decays, over 530 $D^+ \rightarrow \mu^+ \nu$ events have been accumulated. We begin to precisely study hadronic vertex and test LQCD

- BES-III is the most precise results for these to date:

$$\left\{ \begin{array}{l} \text{Br}(D^+ \rightarrow \mu^+ \nu) = (3.74 \pm 0.21 \pm 0.06) \times 10^{-4} \\ f_{D^+} = (203.91 \pm 5.72 \pm 1.97) \text{ MeV} \\ V_{cd} = (0.222 \pm 0.006 \pm 0.005) \end{array} \right.$$

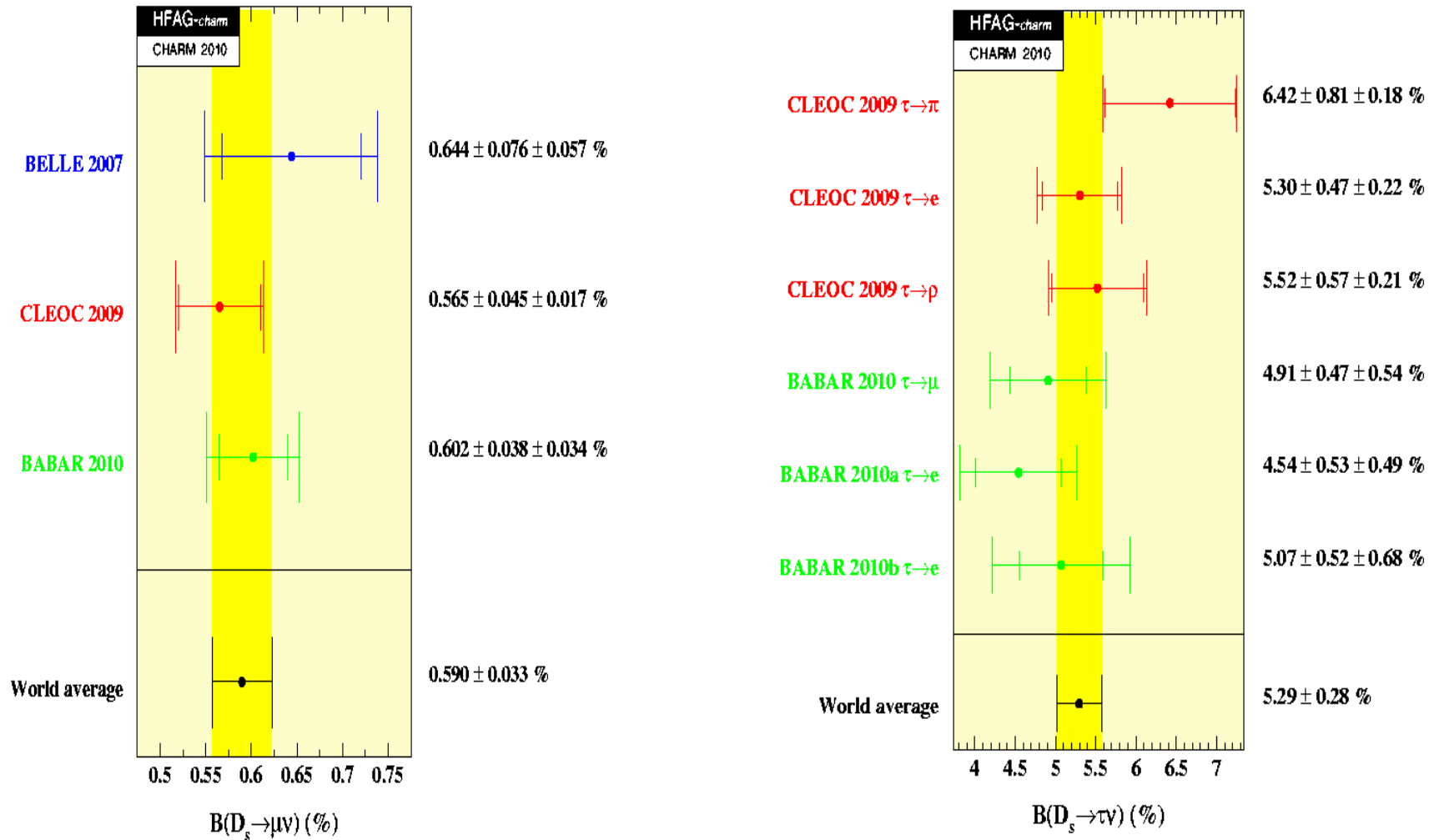
- The world average of decay constants:

$$f_D = (204.5 \pm 5.0) \text{ MeV}, \quad f_{D_s} = (259.1 \pm 5.1) \text{ MeV}$$

- World average f_{D_s}/f_D is 1.267 ± 0.040 , which is $\sim 2.7\sigma$ larger than $f_{D_s}/f_D = 1.156 \pm 0.008$ predicted by theories based on QCD
- Charm decay constants f_D and f_{D_s} can test LQCD, verified LQCD help extract $|V_{td}|$ and $|V_{ts}|$ from $B_{(s)} B_{(s)}$ mixing experiments. These help more precisely test SM and search for New Physics. Charm do play an important role in test of SM of particle physics.

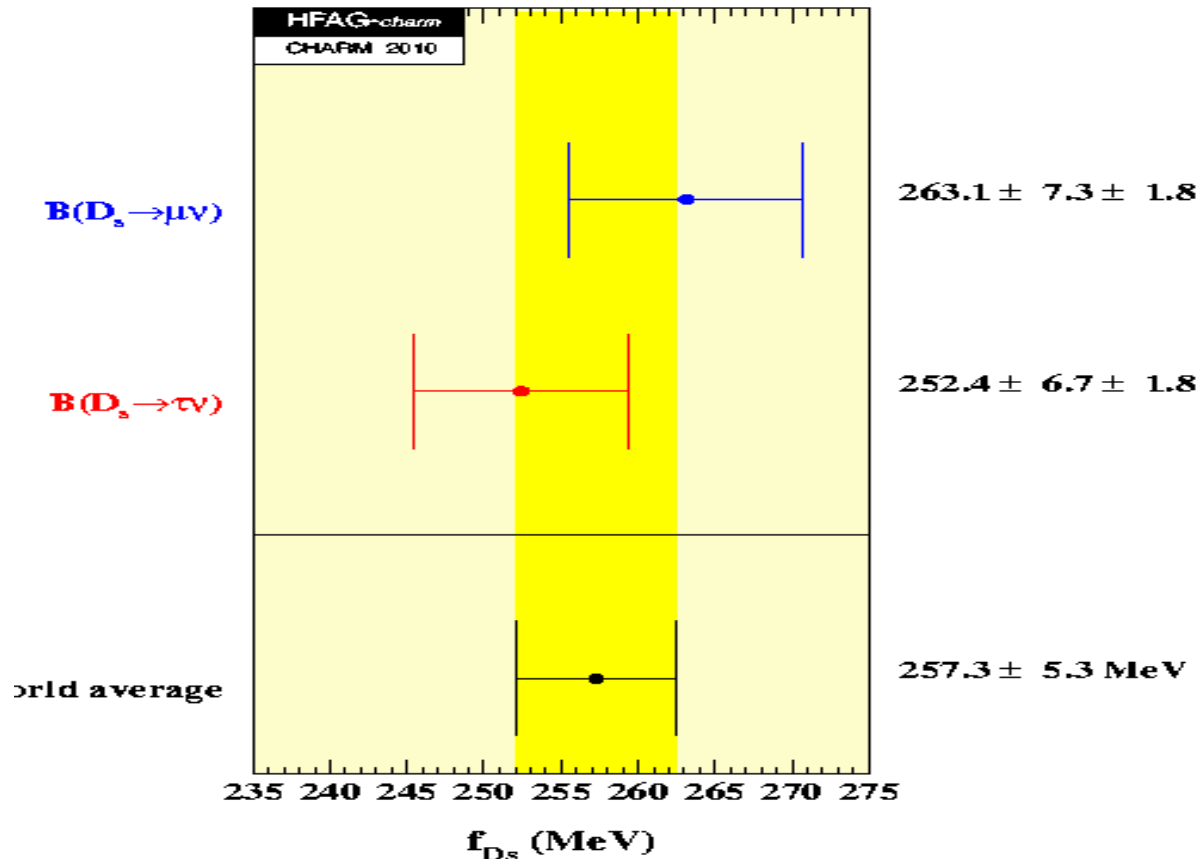
The end!

Summary for $B(D_s^+ \rightarrow l^+ \nu)$



These are taken from HFAG web page

Summary for $f_{D_{S^+}}$



The World Average is: $f_{D_{S^+}} = (257.3 \pm 5.3)$ MeV

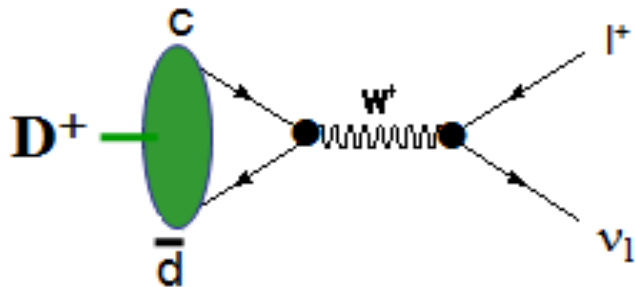
This plot is taken from HFAG web page

Decay rates & $f_{D(D_s)}$

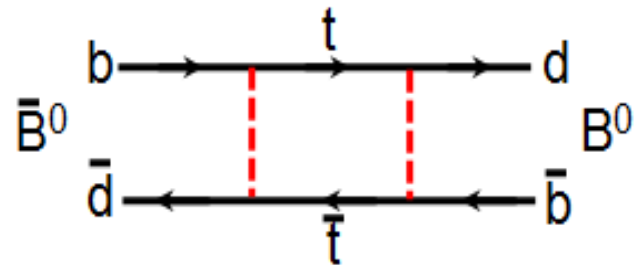
➤ **Measurements of branching fractions probe the hadronic vertex**

$$\Gamma_{\text{SM}}(D_{(s)}^+ \rightarrow l^+ \nu) = \frac{G_F^2}{8\pi} m_l^2 m_{D_{(s)}} \left(1 - \frac{m_l^2}{m_{D_{(s)}}^2} \right)^2 |V_{cd(s)}|^2 f_{D_{(s)}^+}$$

- **Non-perturbative QCD effects are absorbed into $f_{D(D_s)}$, $f_{D(D_s)}$ can be calculated or measured**
- **Measurements of $f_{D(D_s)}$ provide critical test of theory to calculate f_B, f_{B_s}**

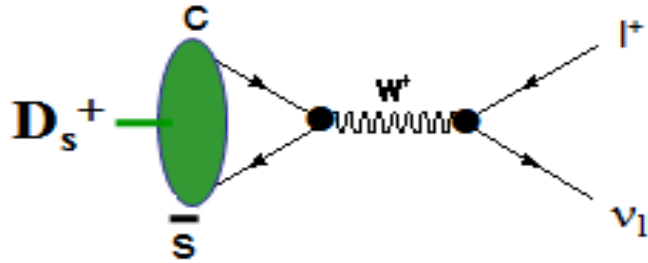


Measured f_{D^+} tests LQCD f_{D^+}
 → better calculated f_{B^+}

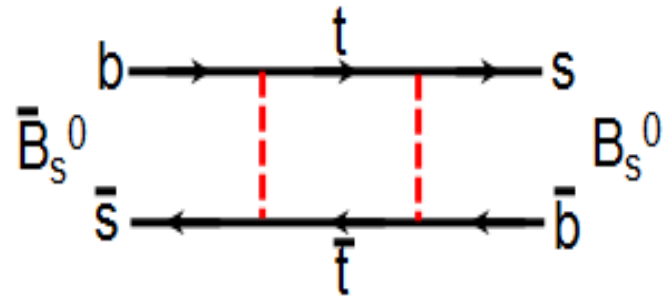


Improve determination of $|V_{td}|$
 from $B^0\bar{B}^0$ mixing experiment,
 needing f_{B^+} as input

Decay rates & $f_{D(D_s)}$



Similarly, measured $f_{D_{S^+}}$ tests LQCD calculated $f_{D_{S^+}}$
 → better calculated $f_{B_{S^+}}$



Improve determination of $|V_{ts}|$ from $B_s^0 B_s^0$ mixing experiment, needing $f_{B_{S^+}}$ as input

Two decay constants ($f_{D(D_s)} \rightarrow f_{B(B_s)}$) affect

- $|V_{ub}|$ extracted from $B^+ \rightarrow l^+ \nu$
- $|V_{td}|$ extracted from Δm_d in $B^0 B^0$ mixing
- $|V_{ts}|$ extracted from Δm_s in $B_s^0 B_s^0$ mixing

These are used to constraint the unitary triangle

➤ **Two decay branching fractions determine**

- $|V_{cd}|$ extracted from $D^+ \rightarrow l^+ \nu$
- $|V_{cs}|$ extracted from $D_s^+ \rightarrow l^+ \nu$

➤ New Physics in $D_{(s)}^+$ leptonic decays

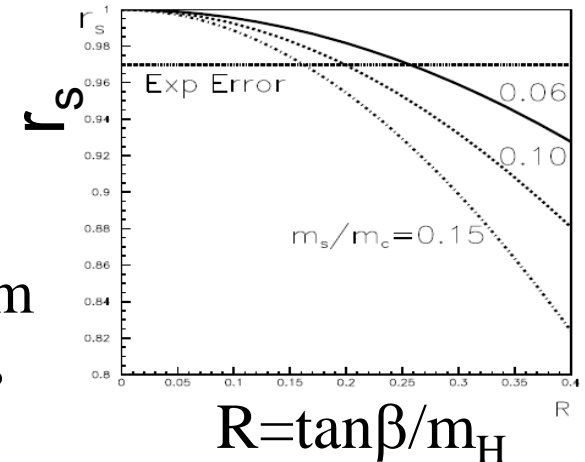
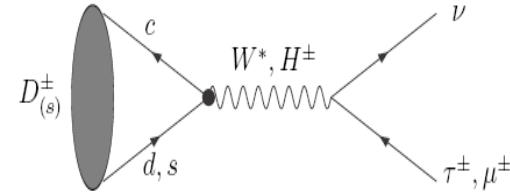
Interference between W^\pm and H^\pm suppresses $D_s^+ \rightarrow l^+ \nu$, but it does not suppress $D^+ \rightarrow l^+ \nu$

$$\Gamma(D_{(s)}^+ \rightarrow l^+ \nu) = \Gamma_{\text{SM}}(D_{(s)}^+ \rightarrow l^+ \nu) r_s$$

$$r_s = \left[1 - m_{D_{(s)}^+}^2 R^2 \left(\frac{m_{d(s)}}{m_{d(s)} + m_c} \right) \right]^2$$

$R = \tan\beta / m_H$, where $\tan\beta$ is the ratio of vacuum expectation values of the two Higgs doublets

J.L. Hewett, hep-ph/9505246;
A.G. Akeroyd, hep-ph/0308260



➤ If $\tan\beta$ is large, it is possible to observe deviation from lepton universality in these decays

Wei-Shu Hou, PRD48,
2342(1993)

$$\frac{\Gamma(D_{(s)}^+ \rightarrow \tau^+ \nu)}{\Gamma(D_{(s)}^+ \rightarrow \mu^+ \nu)} = \frac{m_{\tau^+}^2 (1 - m_{\tau^+}^2 / m_{D_{(s)}^+}^2)^2}{m_{\mu^+}^2 (1 - m_{\mu^+}^2 / m_{D_{(s)}^+}^2)^2}$$



Ratio expected to be
2.67 (9.76) from SM