

# Measurements of hadron electromagnetic structure at BESIII

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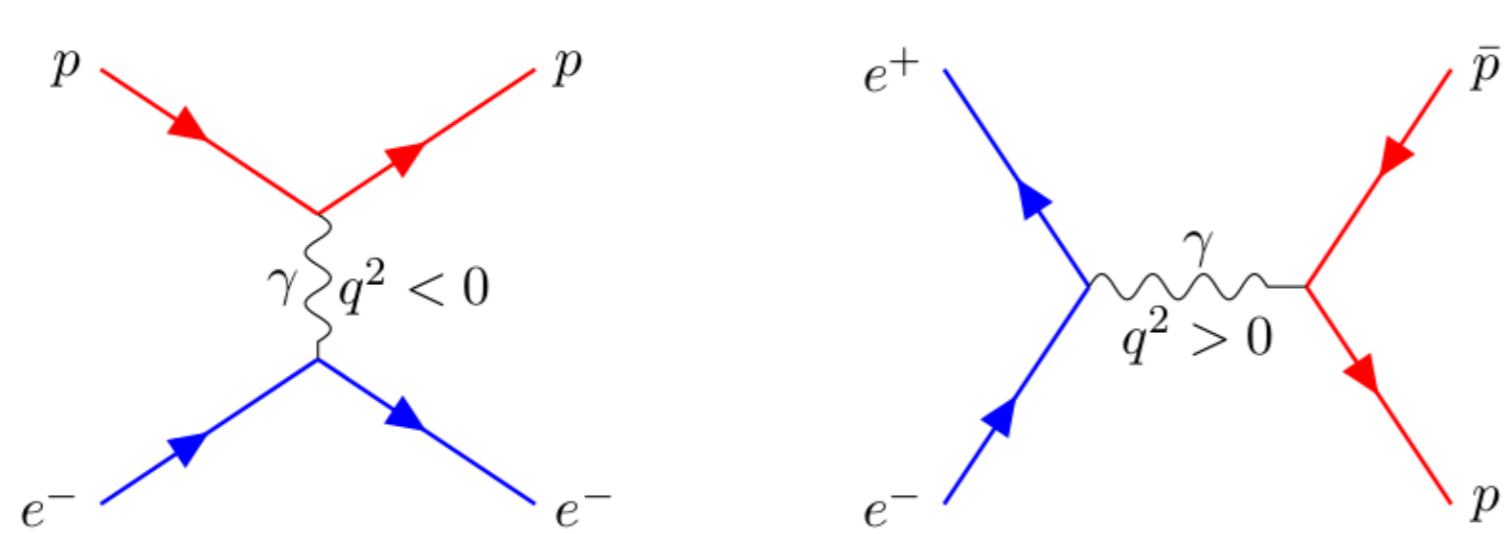


## Form Factors: Why?

- Electromagnetic form factors (FFs) provide fundamental information about the internal electromagnetic structure of hadrons.
- Form Factors are fundamental observables of QCD and each non-pQCD model (Chiral perturbation theory, Lattice QCD, Vector Meson Dominance...) give predictions of FFs as output.
- The structure of light baryons is very difficult, but very important, to understand.
  - For nucleons, FFs give complementary information to Generalized Parton Distributions (GPDs) about the structure.
  - For hyperons, FFs is the only experimentally feasible way to study the structure.
  - Comparing hyperon FFs with nucleon FFs provide a powerful test of SU(3) flavour symmetry of the strong interaction.

## Space/Time-like FFs

- Proton FFs can be measured in space-like (SL) and time-like (TL) region.
- Most of previous experimental data are in the former, while the measurement in the later are scarce and with large errors.



- Feynman diagram of  $ep \rightarrow ep$  elastic scattering at the lowest order (left). The momentum transfer squared,  $q^2$ , is negative and the FFs are real functions of  $q^2$ .
- Feynman diagram of  $e^+e^- \rightarrow p\bar{p}$  annihilation at the lowest order (right). Here,  $q^2$  is positive and the FFs are complex functions of  $q^2$ .

## Form factors in the time-like region

- Differential cross section of  $e^+e^- \rightarrow p\bar{p}$  can be written as a function of FFs, electric  $|G_E|$  and magnetic  $|G_M|$ :  

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2 \beta C}{4q^2} [|G_M(q^2)|^2 (1 + \cos^2\theta) + \frac{1}{\tau} |G_E(q^2)|^2 (\sin^2\theta)]$$
- Born cross section:  $\sigma(q^2) = \frac{4\alpha^2 \beta C}{3q^2} [|G_M(q^2)|^2 + \frac{1}{\tau} |G_E(q^2)|^2]$
- Effective FFs:  $|G(q^2)| = \sqrt{\frac{\sigma}{\frac{4\pi\alpha^2 \beta C}{3q^2} (1 + \frac{1}{\tau})}}$  with assumption of  $|G_M(q^2)| = |G_E(q^2)| = |G(q^2)|$ .

- $\theta$  polar angle of the proton in the  $e^+e^-$  c.m. system.
- $q^2$  transferred momentum
- $\tau = q^2 / (4m_p^2)$
- $\alpha$  fine structure constant
- $\beta$  velocity of  $p$
- $C = 1$  coulomb correction

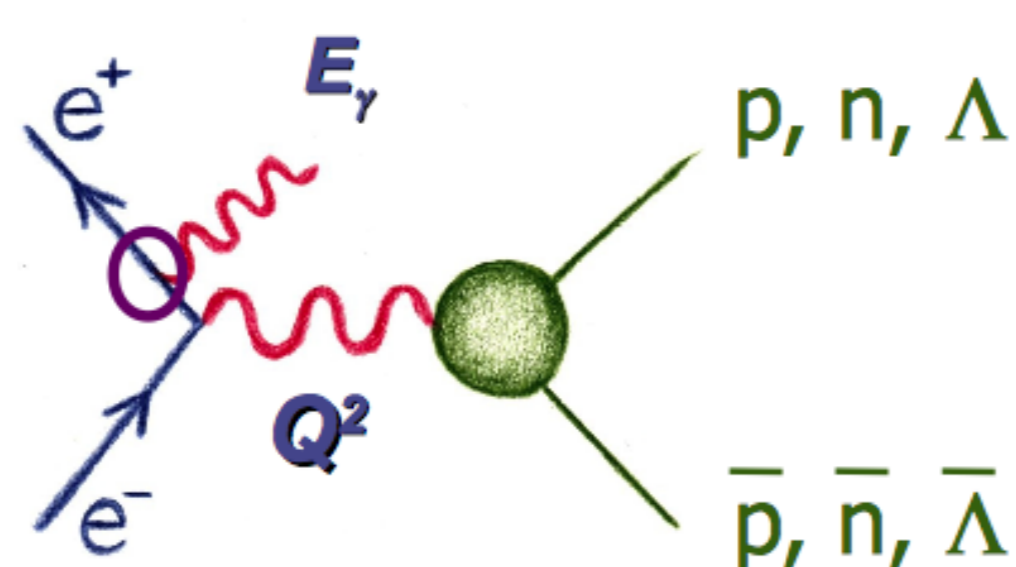
In experiment:  $\sigma_{Born} = \frac{N_{signal}}{L\epsilon(1+\delta)}$ , where  $N_{signal}$  is the number of signal events,  $L$  is the integrated luminosity,  $\epsilon$  is the detection efficiency and the  $1+\delta$  is the radiative correction factor.

Extract Electromagnetic  $R = |G_E/G_M|$  ratio:

- Angular dependence:  $\frac{d\sigma}{d\cos\theta} = N_1 [(1 + \cos^2\theta) + \frac{R^2}{\tau} (1 - \cos^2\theta)]$ ,  $N_1$  is the overall normalization.
- All the formulas are valid for the baryons with spin=1/2.

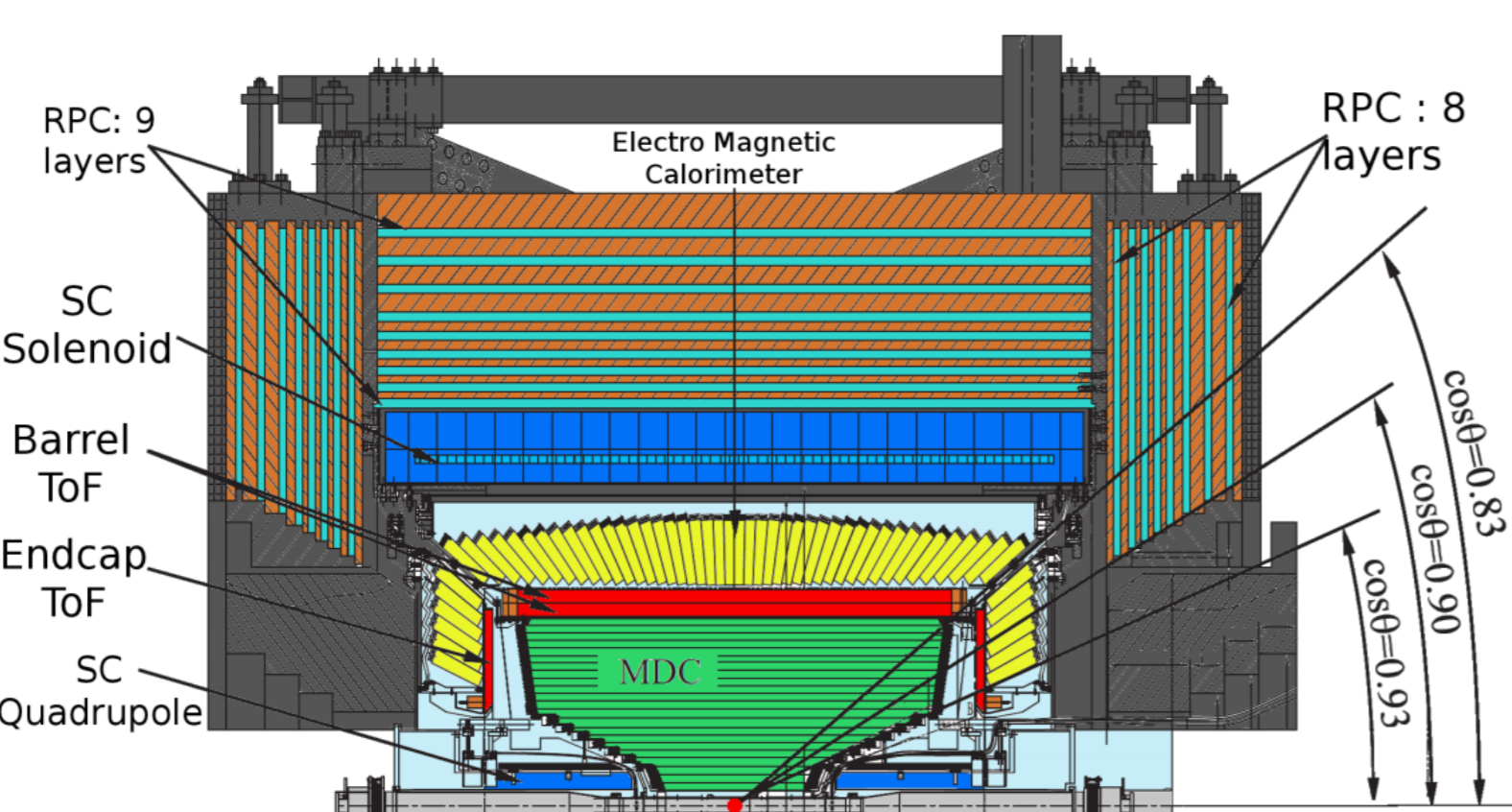
## Experimental measurement of time-like form factors

- In the direct production channel  $e^+e^- \rightarrow p\bar{p}$  (scan method), scanning over several, off-resonance CMS energies.
- In the radiative return channel  $e^+e^- \rightarrow p\bar{p}(\gamma_{ISR})$ , where  $\gamma_{ISR}$  refers to a photon emitted by initial-state radiation (the Radiative Return<sup>1</sup>). Data at a fixed energy collider with high luminosity could be used.



## The BESIII experiment at BEPCII

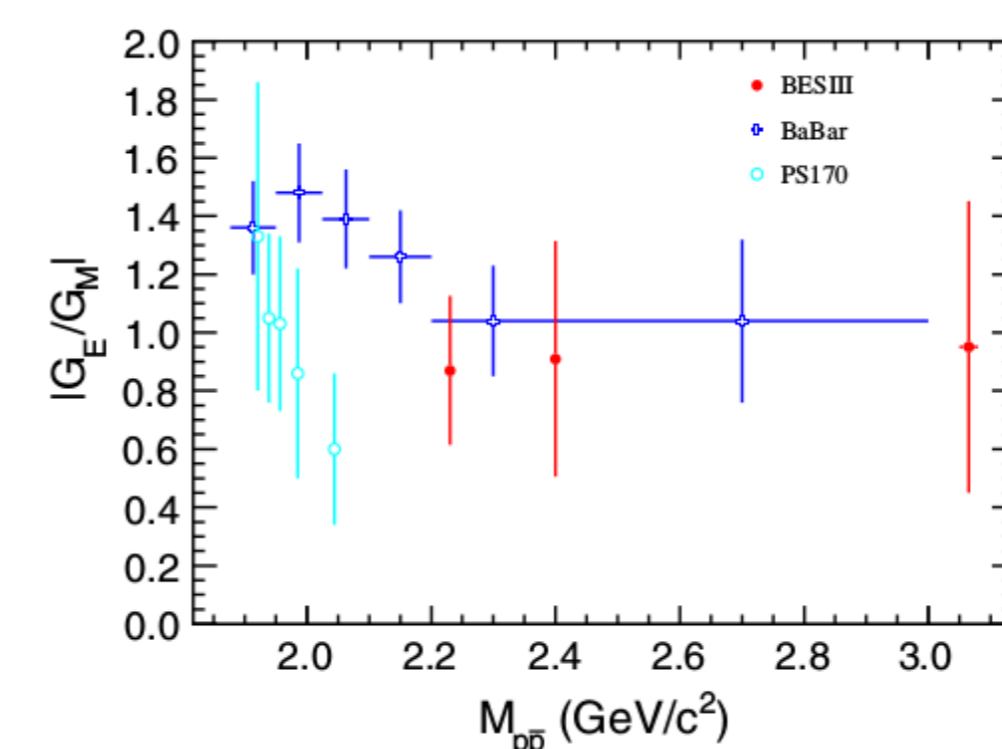
- BEPCII is a double-ring  $e^+e^-$  collider running at c.m. energies between 2.0-4.6 GeV and reaching a peak luminosity of  $0.85 \times 10^{33} \text{cm}^{-2}\text{s}^{-1}$  at a c.m. energy of 3.770 GeV.
- The cylindrical BESIII detector has an effective geometrical acceptance of 93% of  $4\pi$  and is divided into a barrel section and two end caps.



## Results of proton time-like form factors<sup>2</sup>

- Data samples at 12 cms energies from 2232.4 to 3671.0 MeV.
- Scan method are used with those data samples.

$\sqrt{s}$ (MeV)	$ G_E/G_M $	$ G_M  (\times 10^{-2})$	$\chi^2/ndf$
2232.4	$0.87 \pm 0.24 \pm 0.05$	$18.42 \pm 5.09 \pm 0.98$	1.04
2400.0	$0.91 \pm 0.38 \pm 0.12$	$11.30 \pm 4.73 \pm 1.53$	0.74
(3050.0, 3080.0)	$0.95 \pm 0.45 \pm 0.21$	$3.61 \pm 1.71 \pm 0.82$	0.61
Fit on $\cos\theta_p$			
2232.4	$0.83 \pm 0.24$	$18.60 \pm 5.38$	...
2400.0	$0.85 \pm 0.37$	$11.52 \pm 5.01$	...
(3050.0, 3080.0)	$0.88 \pm 0.46$	$3.34 \pm 1.72$	...
Method of moments			

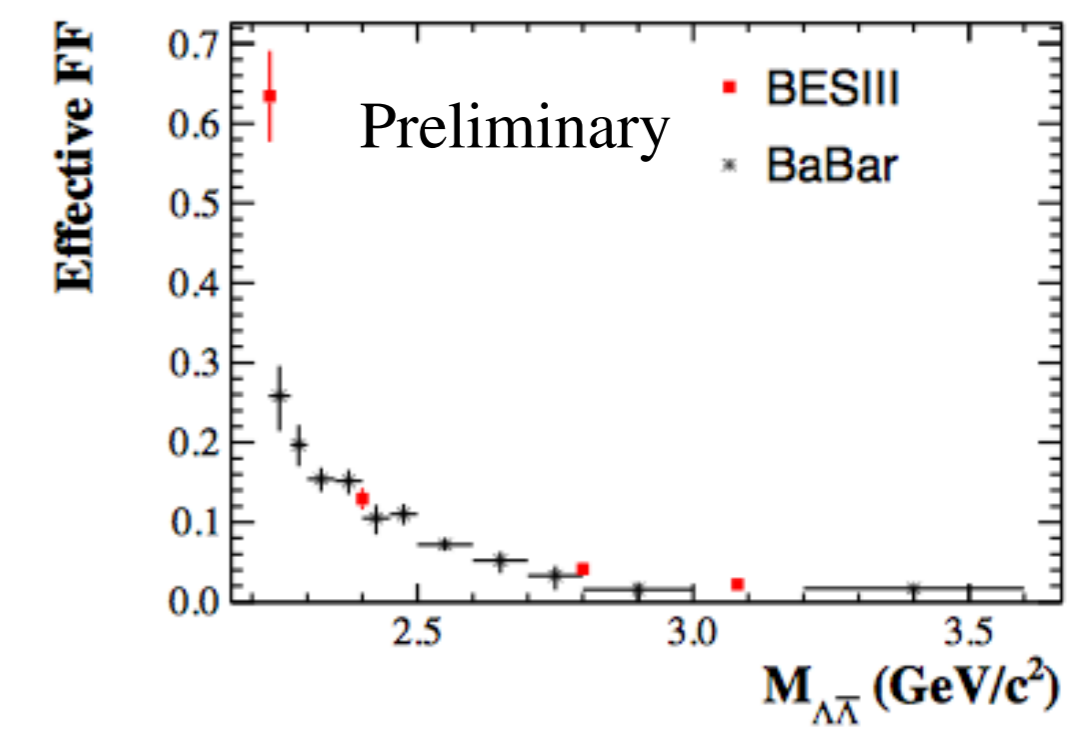
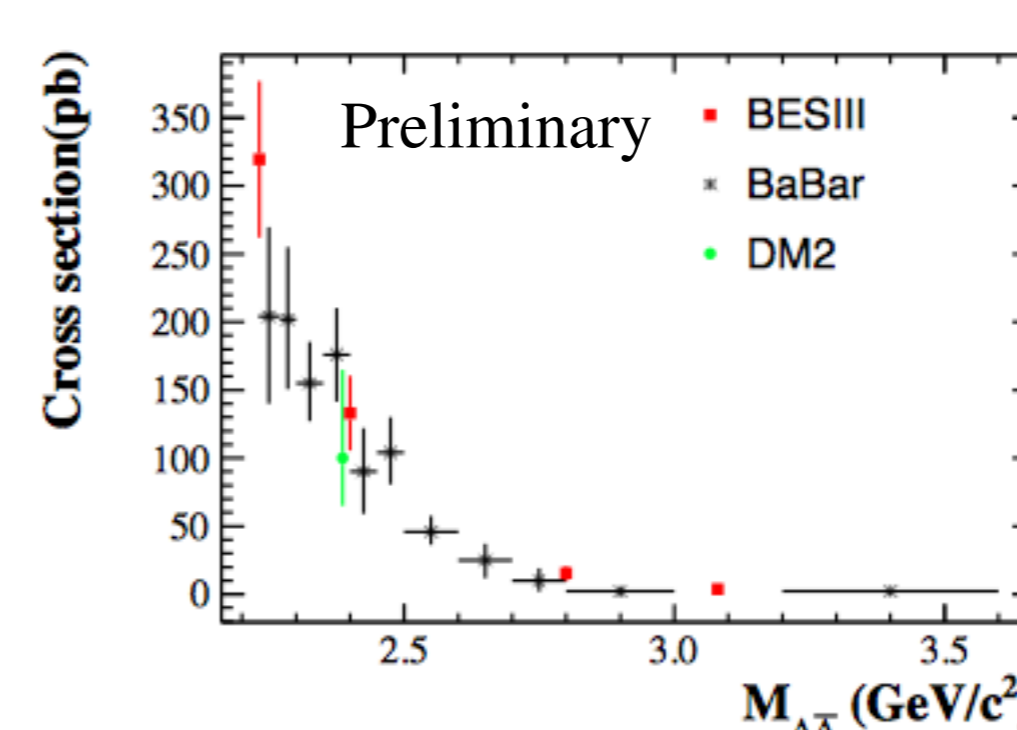


- The proton effective FFs are measured at 12 c.m. energies.
- The Born cross sections and effective FFs are in good agreement with previous experiments, improving the overall uncertainty by 30%.
- $|G_E/G_M|$  ratio are extracted at three energy points, with uncertainty in 25% and 50% (dominated by statistics).
- $|G_E/G_M|$  ratio are close to unity and consistent with BaBar results in the same  $q^2$  region, indicates the data are consistent with the assumption  $|G_E| = |G_M|$  within uncertainties.

The new scan data at 2015 will provide more precise data on the ratio and the effective FFs.

## Results of $\Lambda$ time-like form factors

- Data sets collected at 2.2324 GeV, 2.40 GeV, 2.80 GeV and 3.08 GeV
- The same scan method used to  $e^+e^- \rightarrow p\bar{p}$ .



- Surprisingly, large cross section near threshold! The data points from BESIII give an important contribution to world data.
- Data sample is too small to extract angular distributions.
- The coming scan data will provide precise measurements on ratio and effective FFs.

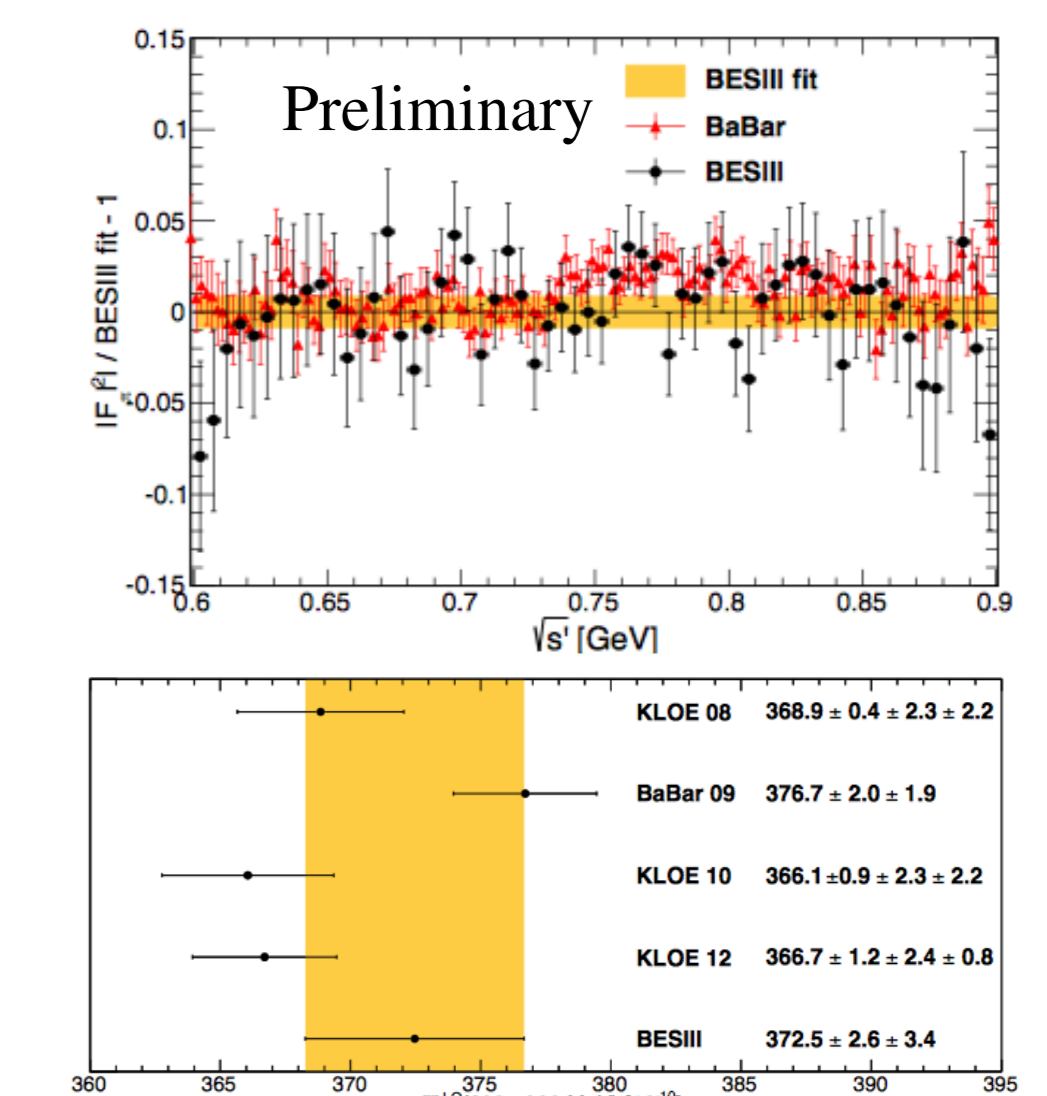
## The anomalous magnetic moment of the muon $a_\mu$

- $a_\mu \equiv (g - 2)_\mu / 2$ , a famous precision observable of the standard model (SM).
- It's accuracy is entirely limited by the knowledge of the hadronic vacuum polarization contribution, which is obtained in a dispersive framework by using experimental data on  $\sigma(e^+e^- \rightarrow \text{hadrons})$ .
- The cross section  $\sigma_{\pi\pi}$  contributes to more than 70% to this dispersion relation.
- Currently, a discrepancy of 3.6 standard deviations is found between the direct measurement of  $a_\mu$  and its SM prediction.

## Measurement of the $e^+e^- \rightarrow \pi^+\pi^-$

- Data at a cms energy  $\sqrt{s} = 3.773 \text{ GeV}$
- Signal process  $e^+e^- \rightarrow \pi^+\pi^-\gamma$ 
  - photon emitted in the initial state
  - nominal energy lowered by the energy of the emitted photon
  - measurements at different energies possible (600-900 MeV)
- A deviation of more than  $3\sigma$  between the SM prediction of  $a_\mu$  and its direct measurement is confirmed.
- Currently a systematic uncertainty of 1.3% is reached.
- We want to redo the luminosity measurement to decrease this error.

Comparisons of results:



## Outlook

New scan data at c.m. energy from 2.0 GeV to 3.1 GeV is coming:

- improve precision measurement of proton form factor,  $|G_E/G_M|$  ratio uncertainty
- measurement of neutron form factor is ongoing
- to measure Hyperons ( $\Lambda$ ,  $\Sigma$ ) TL FFs
  - measure effective FFs,  $|G_E/G_M|$  ratio and  $\Lambda$  polarization
  - in the time-like region, the FFs are complex numbers, i.e.  $G_E$  and  $G_M$  have a relative phase
  - the phase has polarisation effects even if the initial state is unpolarised
  - thanks to the self-analysing decay of hyperons, the polarisation and thus the phase is accessible for hyperons
  - the Uppsala group is responsible

<sup>1</sup>Phys. Lett. B 459, 279(1999)  
<sup>2</sup>Phys. Rev. D 91, 112004(2015)



