



Results on $D_{(s)}$ Pure-Leptonic Decays from experiments near DD threshold

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(For BESIII Collaboration)

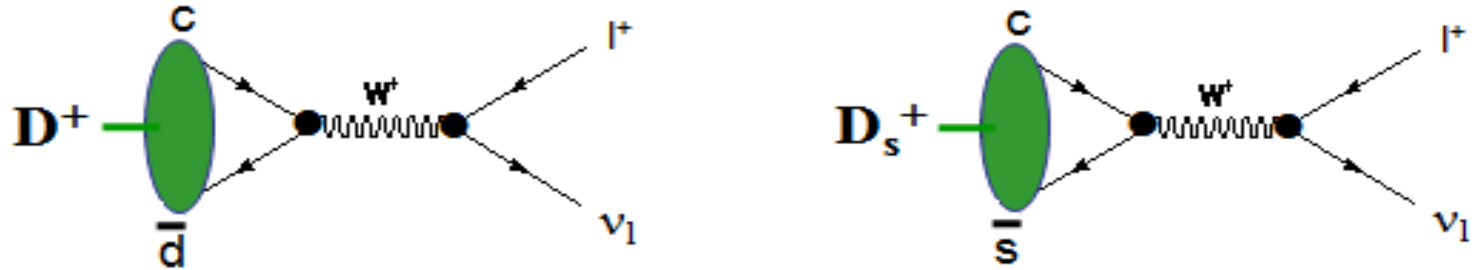
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Outline

- Introduction
- D^+ leptonic decays
- D_s^+ leptonic decays
- Summary

Introduction

Leptonic decays of $D_{(s)}^+$ play an important role in understanding of the SM of particle physics.



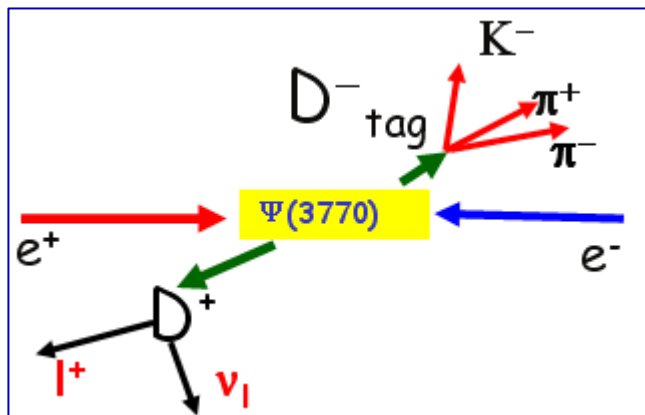
$$B(D_{(s)}^+ \rightarrow l^+ \nu) = \frac{G_F^2}{8\pi} m_l^2 m_{D_{(s)}} \left(1 - \frac{m_l^2}{m_{D_{(s)}}^2}\right)^2 \tau_{D_{(s)}^+} |V_{cd(s)}|^2 f_{D_{(s)}^+}^2$$

f_D can be calculated or measured and measurements of f_D provide critical test of theory to calculate f_B, f_{B_s}

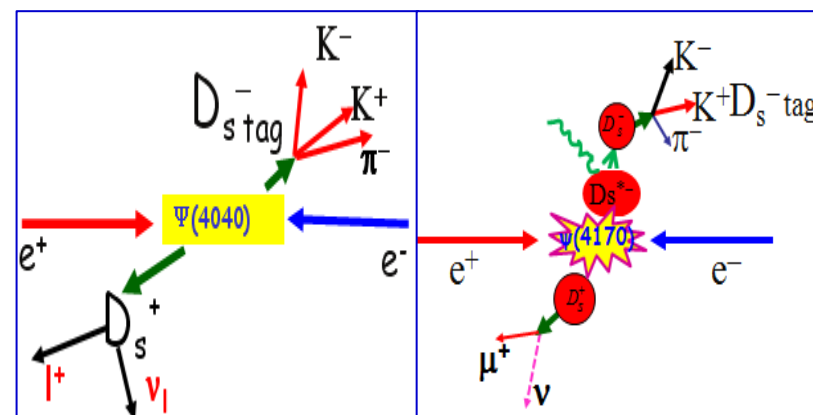
Improve determination of $|V_{td}|, |V_{ts}|$ from $B^0\bar{B}^0, B_s^0\bar{B}_s^0$ mixing experiment needing $f_{B^+}, f_{B_s^+}$ as input.

Experiments near threshold

Taking the advantage of the D^+D^- ($D_s^+D_s^-$) production, one can absolutely measure the branching fraction for $D_{(s)}^+ \rightarrow l^+ \nu$



MARK-III, BES-I, BES-II, CLEO-c and BES-III



BES-I, CLEO-c and BES-III

The neutrino is reconstructed with the missing energy and missing momentum of the D^+

$$M_{\text{miss}}^2 = (E_{\text{beam}} - E_{\mu^+})^2 - (-\vec{p}_{D_{\text{tag}}^-} - \vec{p}_{\mu})^2$$

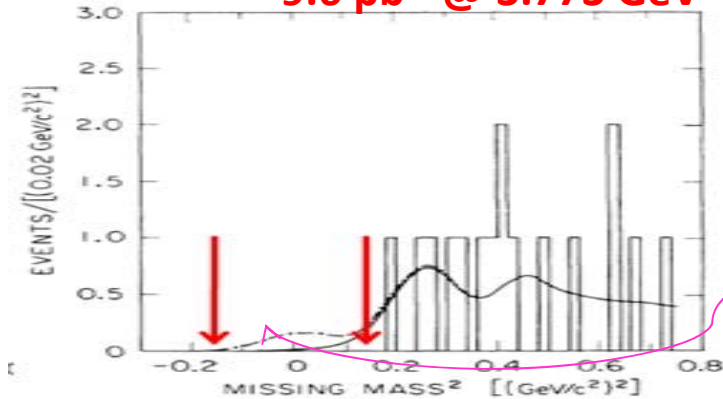
D⁺ leptonic decays

In 1988, MARK-III first searched for the decay of $D^+ \rightarrow \mu^+ \nu_\mu$.

MARK-III

9.6 pb⁻¹ @ 3.773 GeV

PRL60, 1375(1988)



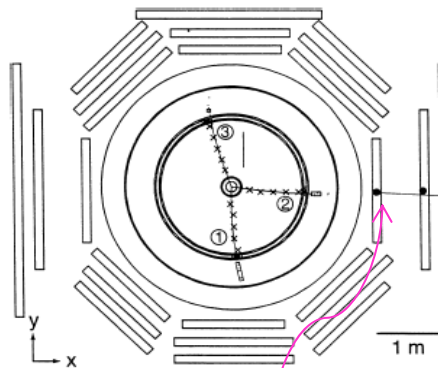
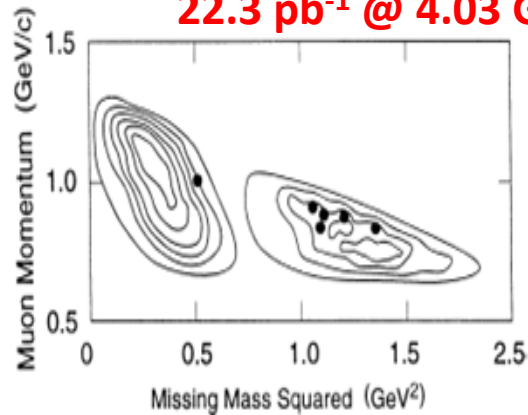
No signal event was found

MARK-III did not observe signal for this decay, they set an upper limit on decay constant $f_{D^+} < 290 \text{ MeV}$

BES-I

22.3 pb⁻¹ @ 4.03 GeV

PLB429, 188 (1998)



$$N_{D^+}^{\text{PRD}} = 10082$$

$$N_{D^+ \rightarrow \mu^+ \nu} = 1$$

$$B(D^+ \rightarrow \mu^+ \nu) = (0.08^{+0.16+0.05}_{-0.05-0.02})\%$$

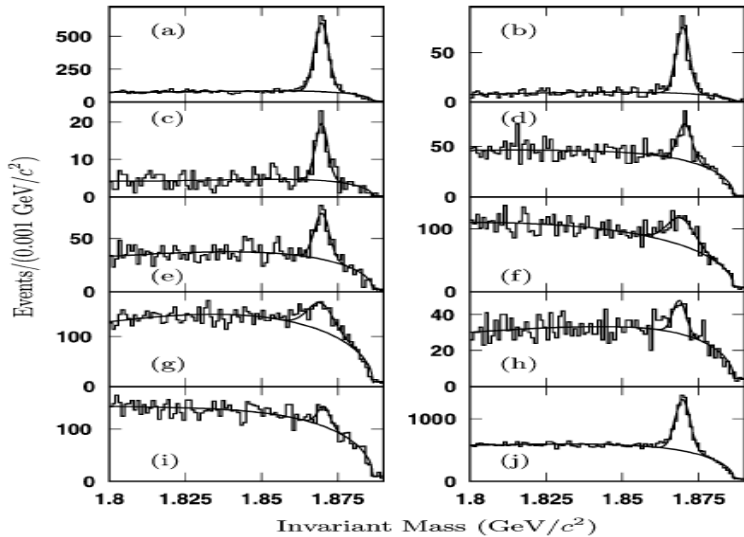
$$f_{D^+} = (300^{+180+80}_{-150-40}) \text{ MeV}$$

One signal event observed

D⁺ leptonic decays @ BES-II

33 pb⁻¹ @ 3.773 GeV

PLB610, 183 (2005)



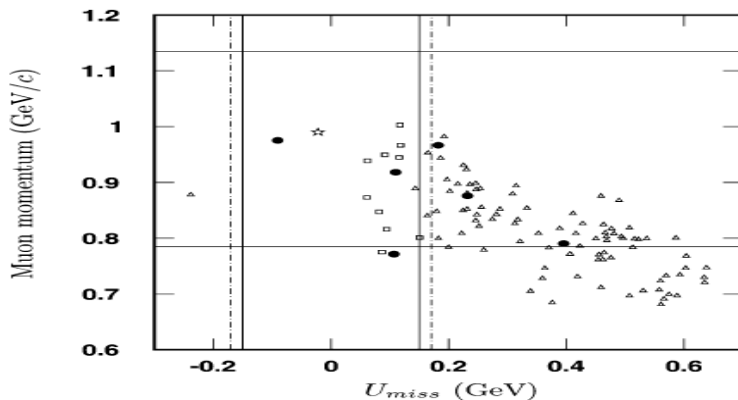
9 single tag modes

$$N_{D_{\text{tag}}^+} = 5321 \pm 149 \pm 160$$

$$N_{D^+ \rightarrow \mu^+ \nu} = 2.7 \pm 1.7$$

$$B(D^+ \rightarrow \mu^+ \nu) = (0.122_{-0.053}^{+0.111} \pm 0.010)\%$$

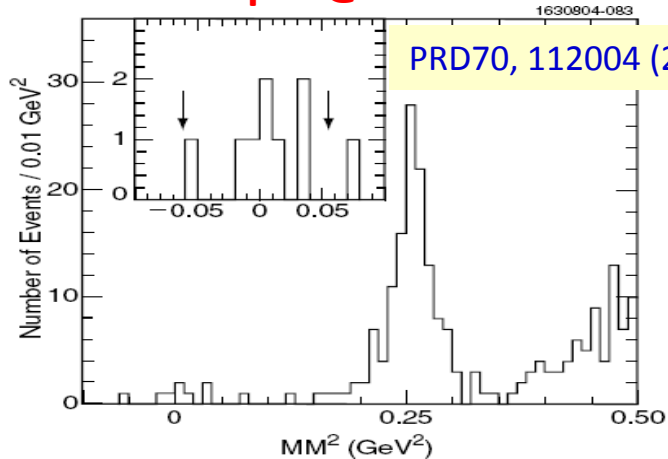
$$f_{D^+} = (371_{-119}^{+129} \pm 25) \text{ MeV}$$



The results were first reported at '04
Electroweak Interactions
& Unified Theories

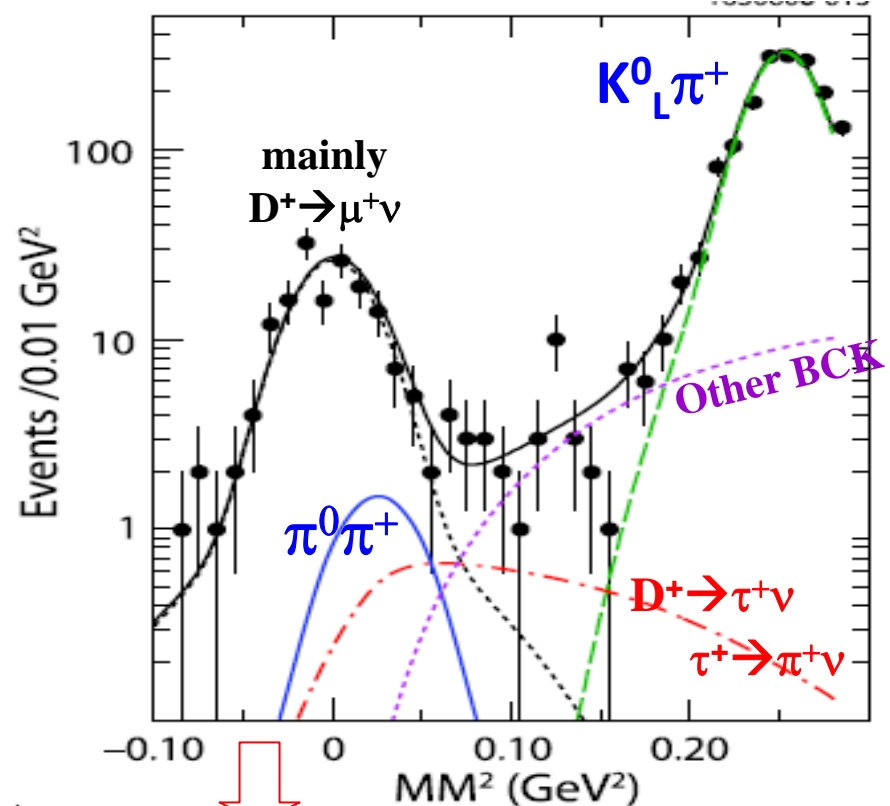
D⁺ leptonic decays @ CLEO-c

60 pb⁻¹ @ 3.773 GeV

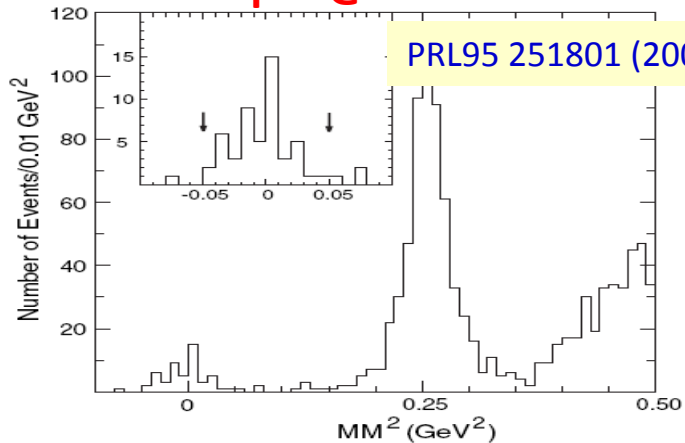


PRD78, 052003(2008)

818 pb⁻¹ @ 3.773 GeV



281 pb⁻¹ @ 3.773 GeV



Superseded the previous results

D⁺ leptonic decays @ CLEO-c

PRD78, 052003(2008)

Results:

$$N(D^+ \rightarrow \mu^+ \nu) = 149.7 \pm 12.0$$

The statistical error is a little bit smaller than squared root of 149.7

$$N(D^+ \rightarrow \tau^+ \nu) = 25.8 \text{ (fixed in fit)}$$

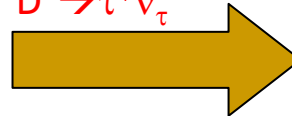
$$N(D^+ \rightarrow \pi^0 \pi^+) = 9.2 \text{ (fixed in fit)}$$

37.4 background Events

$$\text{Other background events : } 2.4 \pm 1.0$$

$$\begin{aligned} Br(D^+ \rightarrow \mu^+ \nu) &= \\ & (0.0382 \pm 0.0032 \pm 0.0009)\% \\ f_{D^+} &= (205.8 \pm 8.5 \pm 2.5) \text{ MeV} \end{aligned}$$

Without fixing the background number from $D^+ \rightarrow \tau^+ \nu_\tau$



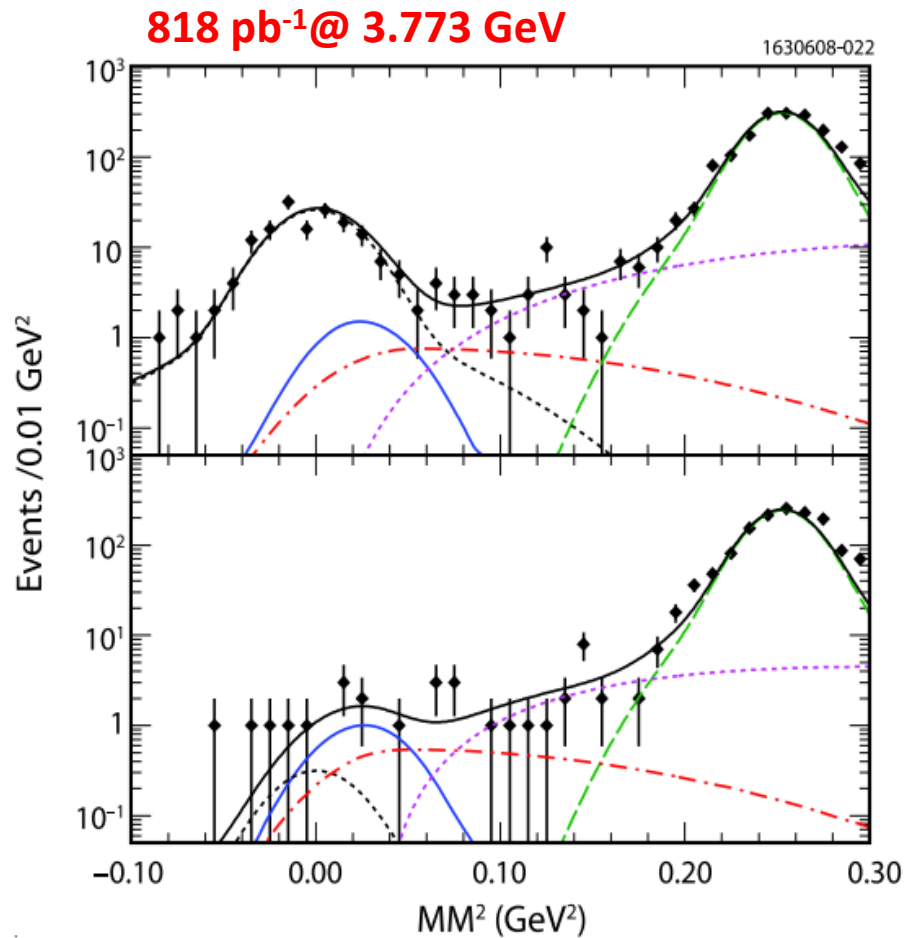
$$\begin{aligned} Br(D^+ \rightarrow \mu^+ \nu) &= \\ & (0.0393 \pm 0.0035 \pm 0.0009)\% \\ f_{D^+} &= (207.6 \pm 9.3 \pm 2.5) \text{ MeV} \end{aligned}$$

More reliable*

*For detail, see arXiv:1209.0085v1[hep-ex]

D^+ leptonic decays @ CLEO-c

PRD78, 052003(2008)



$$N_{D_{\text{tag}}^-} = 460055 \pm 787$$

$$N_{D^+ \rightarrow \tau^+ \nu} = 27.8 \pm 16.4$$

$$\text{Br}(D^+ \rightarrow \tau^+ \nu_\tau) < 1.2 \times 10^{-3}$$

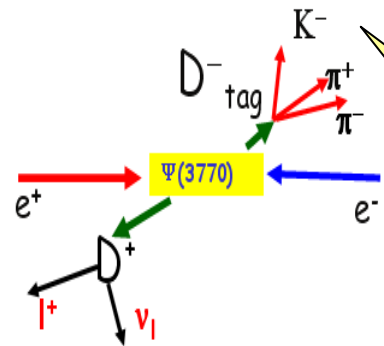
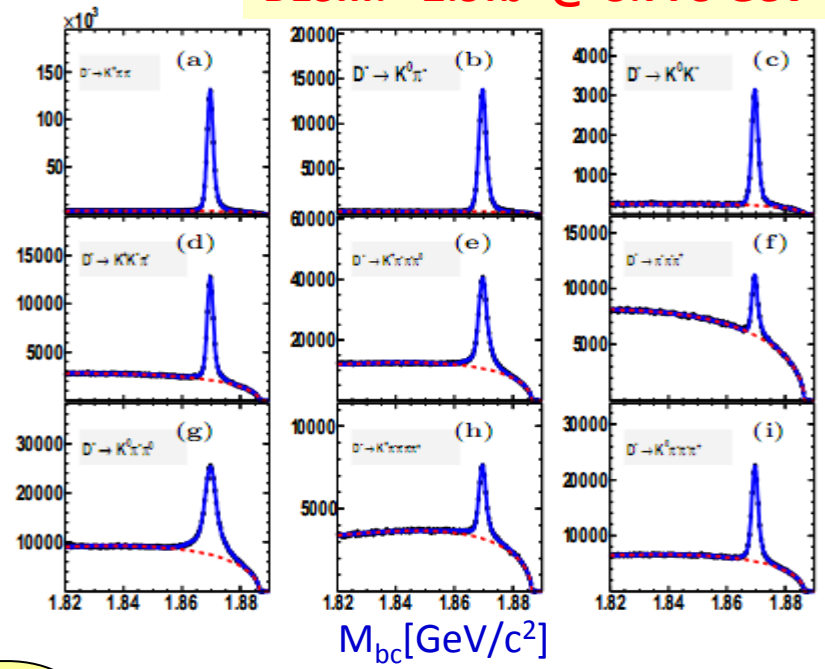
$$\text{Br}(D^+ \rightarrow e^+ \nu_e) < 8.8 \times 10^{-6}$$

D⁺ leptonic decays @ BES-III

The selected single tag channels:

$$\begin{aligned}
 D^- &\rightarrow K^+ \pi^- \pi^- & D^- &\rightarrow K^- \pi^+ \pi^+ \pi^0 \\
 D^- &\rightarrow K^0 \pi^- & D^- &\rightarrow \pi^- \pi^- \pi^+ \\
 D^- &\rightarrow K^0 K^- & D^- &\rightarrow K^0 \pi^- \pi^0 \\
 D^- &\rightarrow K^+ K^- \pi^- & D^- &\rightarrow K^+ \pi^- \pi^- \pi^- \pi^+ \\
 & & D^- &\rightarrow K^0 \pi^+ \pi^- \pi^-
 \end{aligned}$$

BESIII: $\sim 2.9 \text{ fb}^{-1}$ @ 3.773 GeV

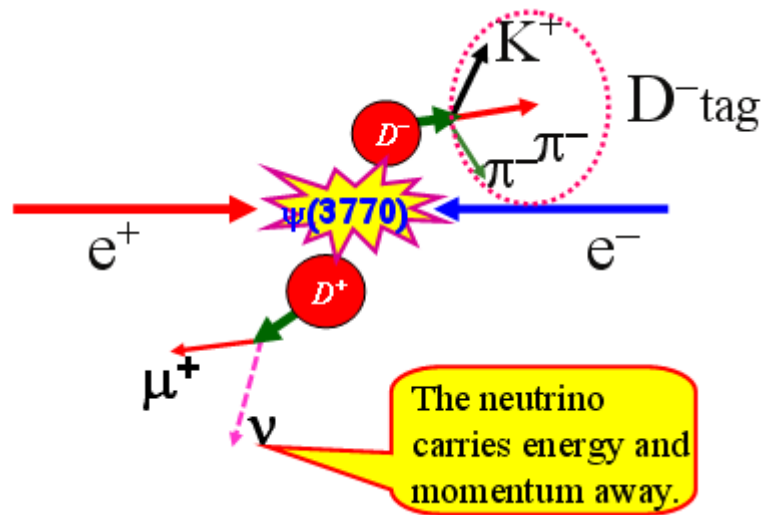


9 singly tagged D⁻ modes are used to accumulate the D⁺D⁻ events

$$N_{D_{tag}^-} = 1565953 \pm 2327$$

Selection of $D^+ \rightarrow \mu^+ \nu$ @ BES-III

In the side recoiling against the singly tagged D^- , BES-III select the purely leptonic decay events for $D^+ \rightarrow \mu^+ \nu$



they require:

One identified charged μ^+

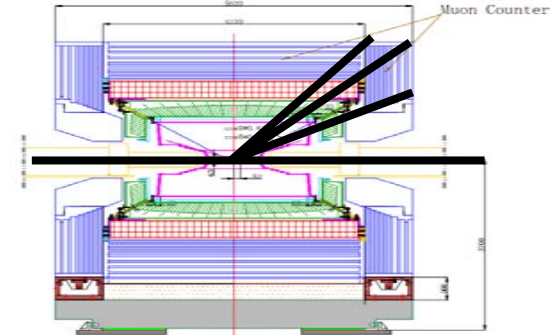
No isolated photon

$$E_{\text{miss}} = E_{\text{cms}} - \sum_i E_i$$
$$\vec{P}_{\text{miss}} = -\sum_i \vec{P}_i$$
$$M_{\text{miss}}^2 = E_{\text{miss}}^2 - P_{\text{miss}}^2$$

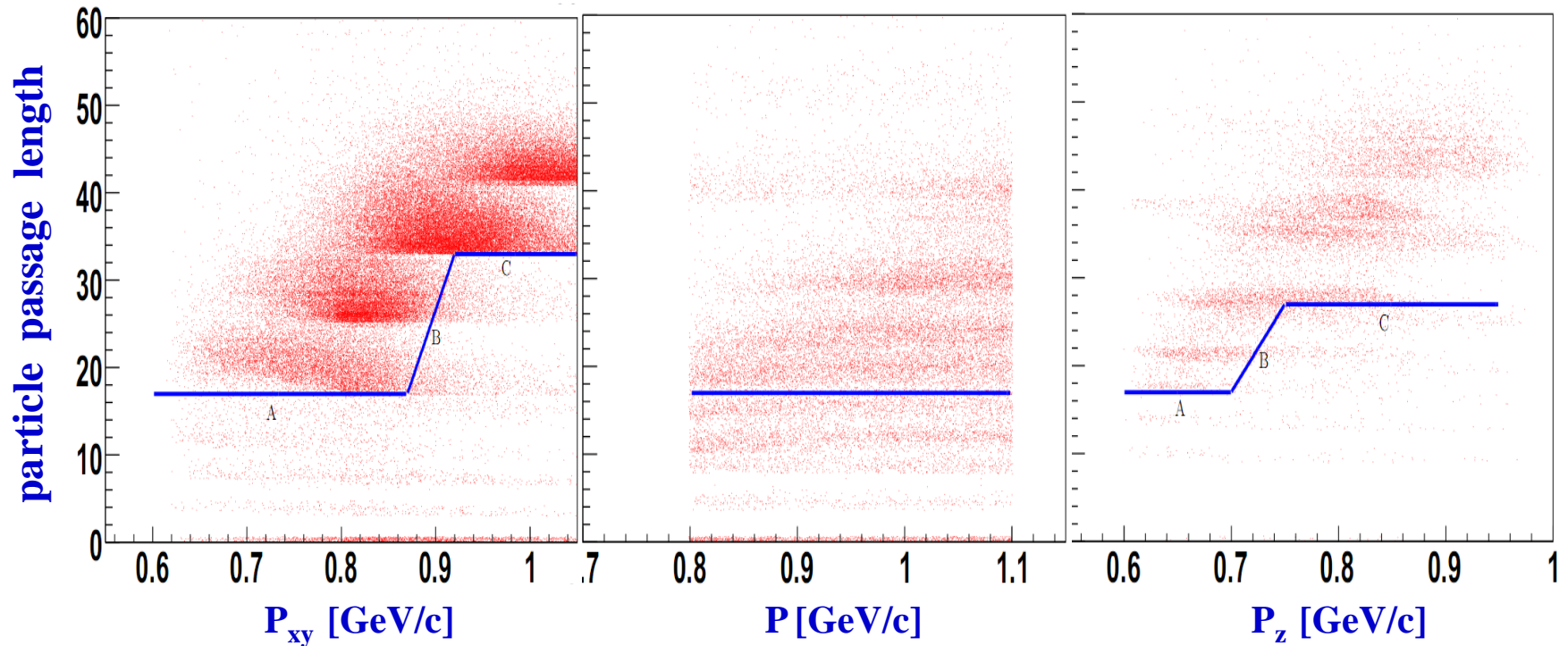
The expected value of M_{miss}^2 for the events of the singly tagged D^- v.s. $D^+ \rightarrow \mu^+ \nu$ should be ~ 0

μ ID for $D^+ \rightarrow \mu^+ \nu_\mu$ @ BES-III

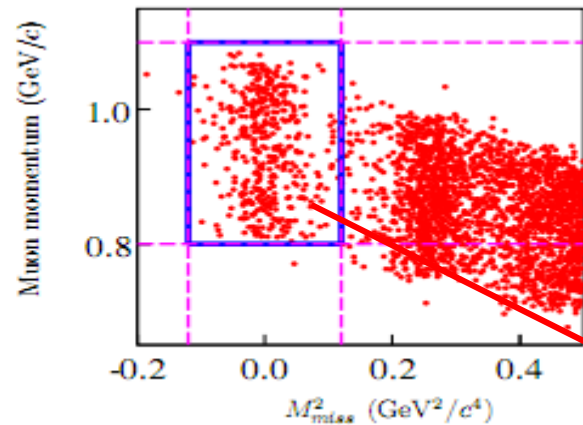
Muon can be well identified with the passage length of a particle going through the MUC at the BES-III experiment



Particle passage length in MUC VS momentum

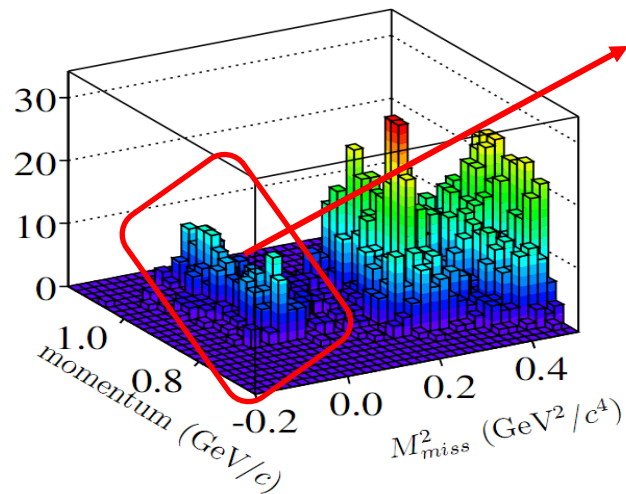


Selection of $D^+ \rightarrow \mu^+ \nu$ @ BES-III



The remained bg are estimated by MC simulation.

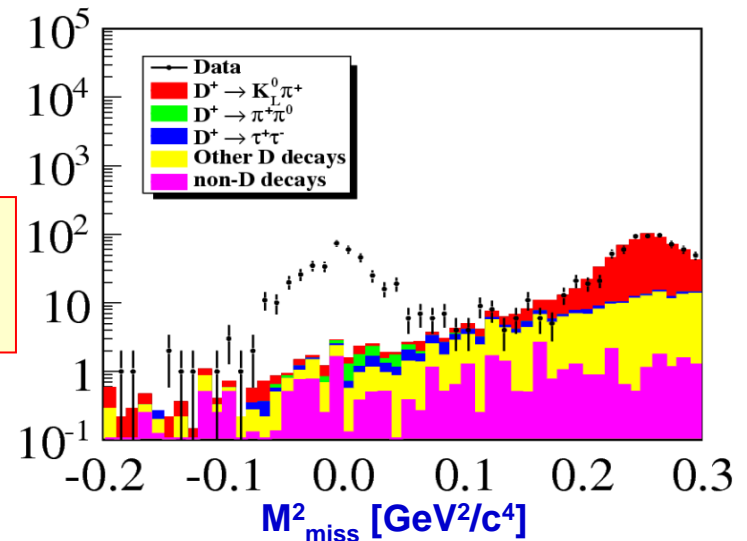
425 Candidates for $D^+ \rightarrow \mu^+ \nu$



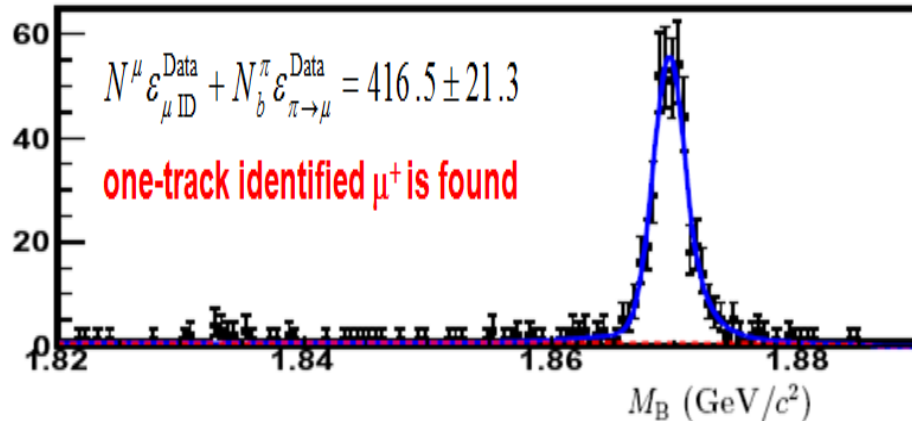
The remained bg are estimated by MC simulation.

Estimated with Monte Carlo

Source mode	Number of events
$D^+ \rightarrow K_L^0 \pi^+$	7.9 ± 0.8
$D^+ \rightarrow \pi^+ \pi^0$	3.8 ± 0.5
$D^+ \rightarrow \tau^+ \nu_\tau$	6.9 ± 0.7
Other decays of D mesons	17.9 ± 1.1
$e^+ e^- \rightarrow \gamma \psi(3686)$	0.2 ± 0.2
$e^+ e^- \rightarrow \gamma J/\psi$	0.0 ± 0.0
$e^+ e^- \rightarrow \text{light hadron (continuum)}$	8.2 ± 1.4
$e^+ e^- \rightarrow \tau^+ \tau^-$	1.9 ± 0.5
$\psi(3770) \rightarrow \text{non-} D\bar{D}$	0.9 ± 0.4
Total	47.7 ± 2.3

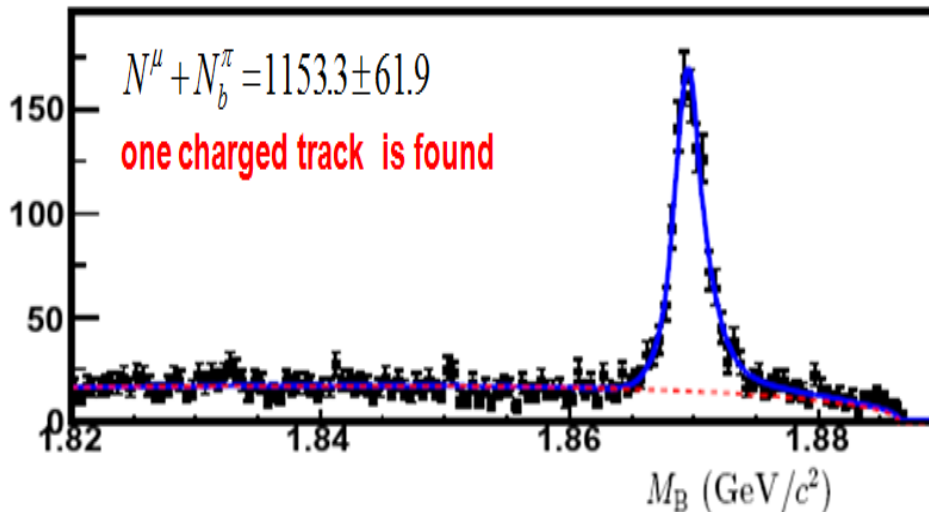


Backgrounds for $D^+ \rightarrow \mu^+ \nu_\mu$



The number of backgrounds are also estimated with data.

By examining number of events with only one charged track in recoil side of the D^- tags, one can estimate number of background events as well.



$$N_b^{D \text{ Decays}} = 29.0 \pm 3.4$$

$$N_b^{\text{cmb}} = 19.9 \pm 3.4$$

$$N_b^{\text{tot}} = 48.9 \pm 4.8$$

Br. & f_{D^+} & V_{cd} at BES-III

Based on the observed number of $D^+ \rightarrow \mu^+ \nu_\mu$, the branching fraction is measured to be

$$BF(D^+ \rightarrow \mu^+ \nu) = (3.74 \pm 0.21 \pm 0.06) \times 10^{-4}$$

Which is related to f_{D^+} and V_{cd} by

$$B(D_{(s)}^+ \rightarrow l^+ \nu) = \frac{G_F^2}{8\pi} m_l^2 m_{D_{(s)}} \left(1 - \frac{m_l^2}{m_{D_{(s)}}^2}\right)^2 \tau_{D_{(s)}^+} |V_{cd(s)}|^2 f_{D_{(s)}^+}$$

$$f_{D^+} = (203.91 \pm 5.72 \pm 1.97) \text{ MeV} (|V_{cd}| = |V_{us}| = 0.2252 \pm 0.0007)$$

$$|V_{cd}| = 0.2249 \pm 0.0060 \pm 0.0044 (f_{D^+} = 207 \pm 4 \text{ MeV (from LQCD)})$$

Those results were first reported at Charm2012.

Average of Br. & f_D

Experiment	$B(D^+ \rightarrow \mu^+ \nu_\mu) (\times 10^{-4})$	Average
CLEO-c	$(3.93 \pm 0.35 \pm 0.09)^*$	(3.79 ± 0.19)
BES-III(PRLMNR)	$(3.74 \pm 0.21 \pm 0.06)$	

Experiment	f_D (MeV)	Average
CLEO-c	$(207.6 \pm 9.3 \pm 2.5)$	(205.3 ± 5.1)
BES-III(PRLMNR)	$(203.91 \pm 5.72 \pm 1.97)$	

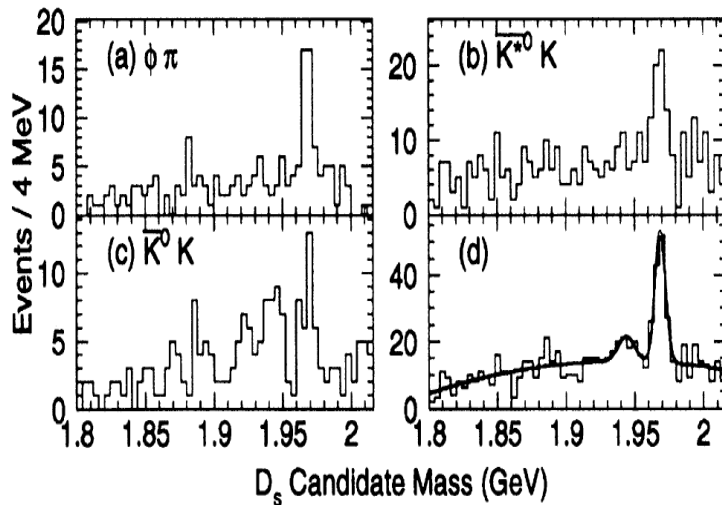
At present, the error is still dominated by statistics, needing more data to be taken at 3.773 GeV to reduce the error.

*For detail, see [arXiv:1209.0085v1\[hep-ex\]](https://arxiv.org/abs/1209.0085v1)

$D_s^+ \rightarrow l^+ \nu$ at BES-I

22.3 pb⁻¹ @4.03 GeV

PRL74, 4599 (1995)



$e^+e^- \rightarrow D_s^+ D_s^-$

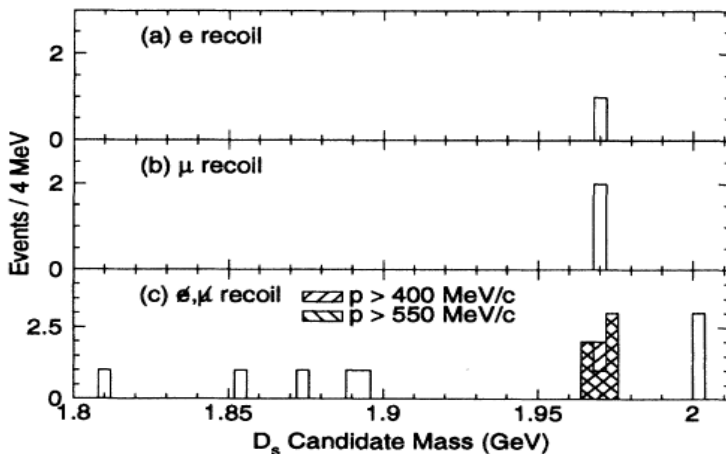
3 singly tagged D_s^- modes

94 singly tagged D_s^-

3 events for $D_s^- \rightarrow l^+ \nu$

$$B(D_S^+ \rightarrow \mu^+ \nu) = (1.5_{-0.6-0.2}^{+1.3+0.3})\%$$

$$f_{D_S^+} = 430_{-130-0.40}^{+150+40} \text{ MeV}$$

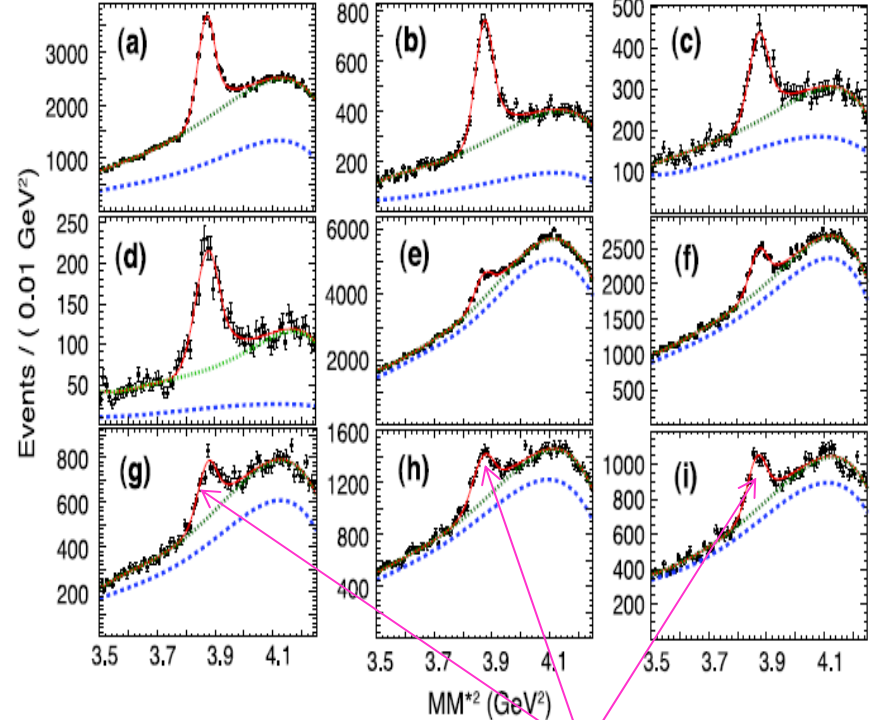
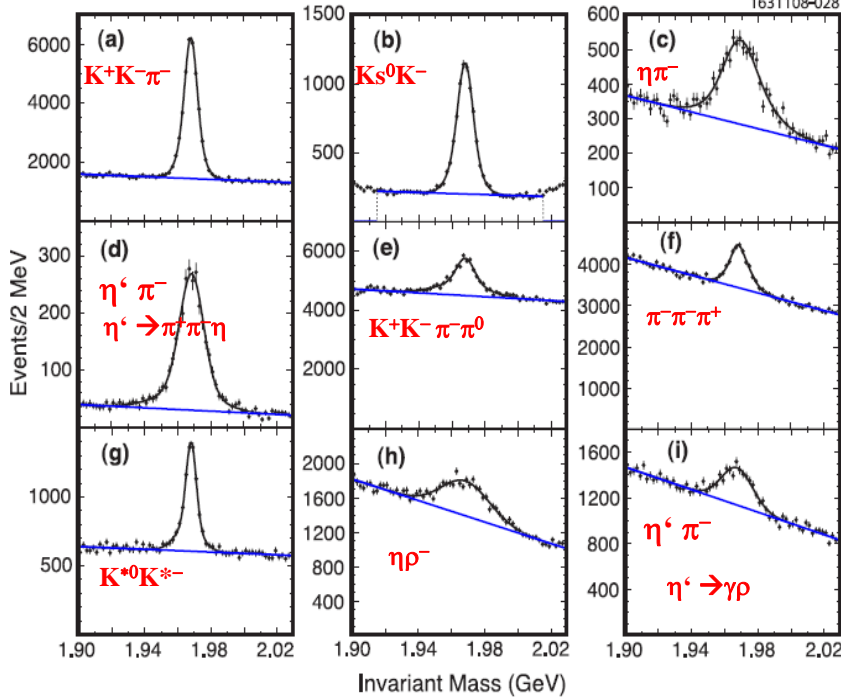


It was the first absolute measurement.

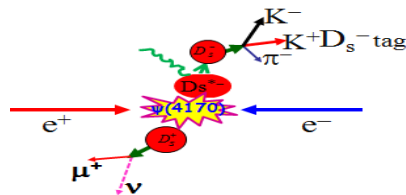
$Ds^+ \rightarrow l^+ \nu$ at CLEO-c

PRD79, 052001 (2009)

600 pb⁻¹ @ 4.170 GeV



These peaks indicate that the Ds^* - are well reconstructed



$$e^+e^- \rightarrow Ds^+ Ds^{*-}, Ds^{*-} \rightarrow \gamma Ds^-$$

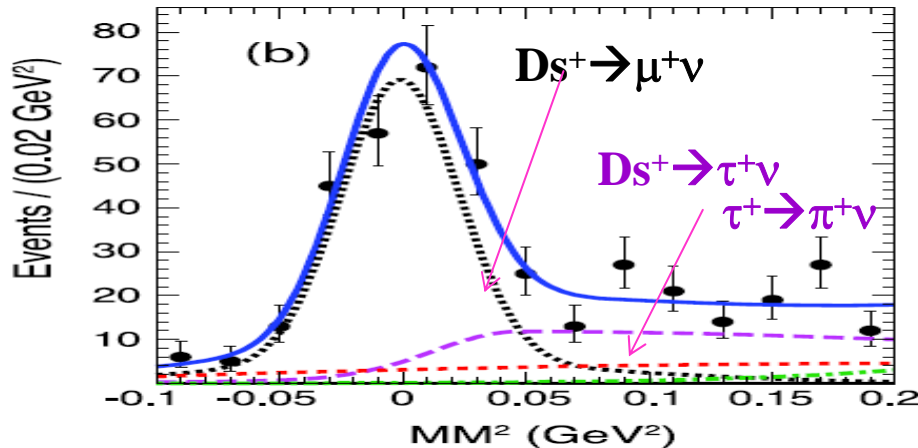
$$MM^2 = (E_{CM} - E_{D_s^-} - E_\gamma)^2 - (-\vec{P}_{CM} - \vec{P}_{D_s^-} - \vec{P}_\gamma)^2$$

MM^{*2} is the missing mass-squared recoiling against the γDs^-

$N_{tag} = 43859 \pm 436$

$D_s^+ \rightarrow l^+ \nu$ at CLEO-c

600 pb⁻¹ @4.17GeV

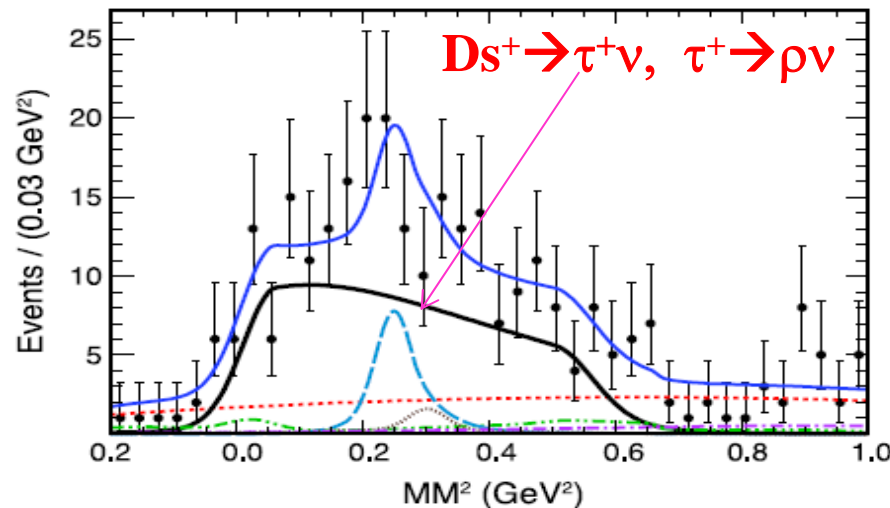


PRD79, 052001 (2009)

$$B(D_s^+ \rightarrow \mu^+ \nu) = (0.591 \pm 0.037 \pm 0.018)\%$$

$$B(D_s^+ \rightarrow \tau^+ \nu) = (6.42 \pm 0.81 \pm 0.18)\%$$

$$f_{D_s^+} = 263.3 \pm 8.2 \pm 3.9 \text{ MeV}$$



PRD80, 112004 (2009)

$$B(D_s^+ \rightarrow \tau^+ \nu) = (5.52 \pm 0.57 \pm 0.21)\%$$

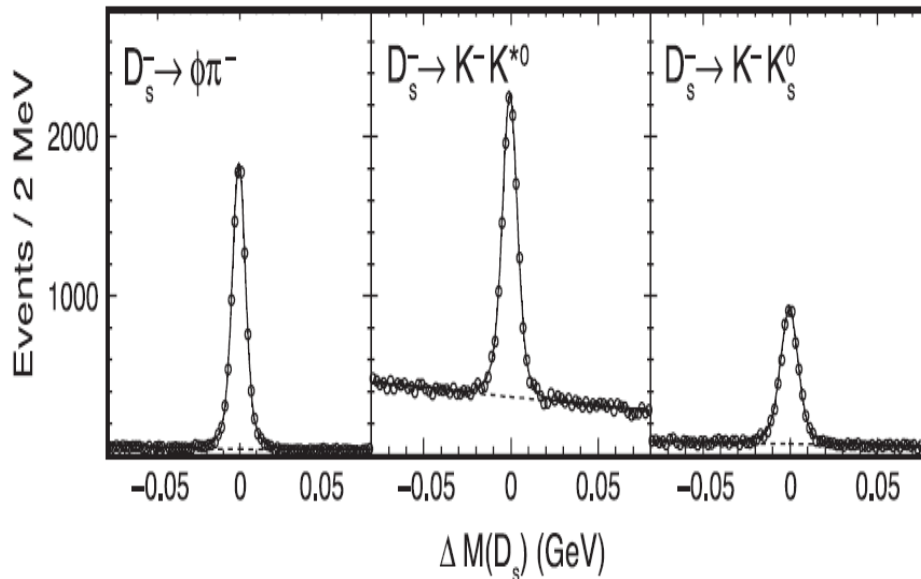
$$f_{D_s^+} = 257.8 \pm 13.3 \pm 5.2 \text{ MeV}$$

Absolute measurement.

$D_s^+ \rightarrow l^+ \nu$ at CLEO-c

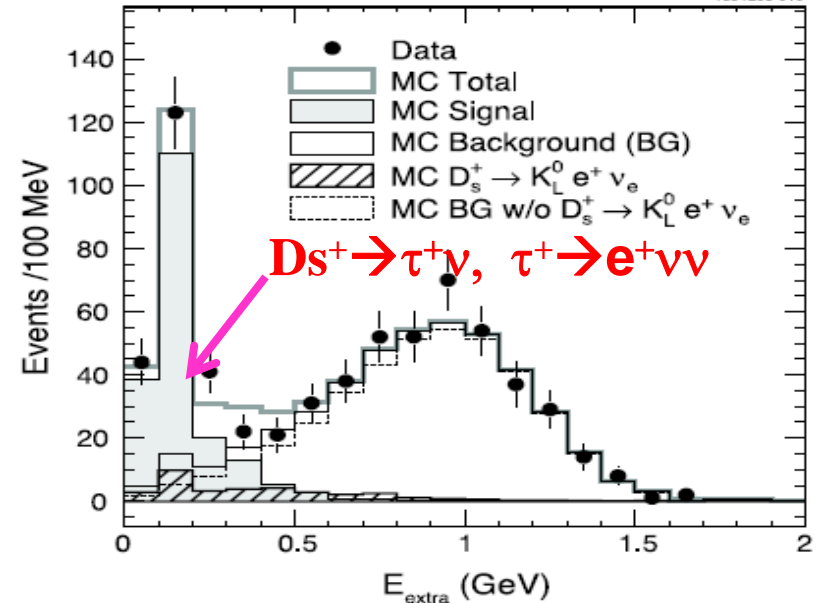
600 pb⁻¹ @4.17GeV

PRD79, 052002 (2009)



Three cleanest single tag D_s mode were used

Tag mode	n_{ST}^S	n_{ST}^B	s	n_{ST}
$D_s^- \rightarrow \phi\pi^-$	10459	807	0.980	9668.1 ± 106.1
$D_s^- \rightarrow K^- K^{*0}$	18319	7381	1.000	10938.0 ± 160.3
$D_s^- \rightarrow K^- K_s^0$	7135	1409	0.999	5727.8 ± 92.4
Total				26333.9 ± 213.3



E_{extra} is the total energy of rest of the event measured in the electromagnetic calorimeter

$$f_{D_s^+} = 252.5 \pm 11.1 \pm 5.2 \text{ MeV}$$

Absolute measurement.

Summary and Future Perspective

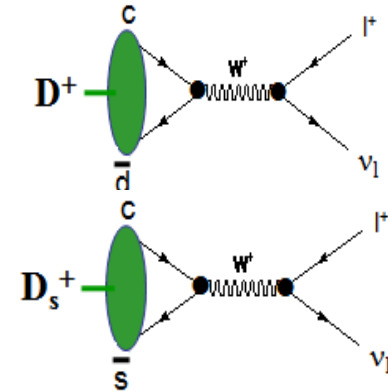
➤ MARK-III, BES-I, BES-II, CLEO-c and BES-III have measured the $f_{D(s)}$.

➤ The best precise measurement from **BES-III**:

$$\text{Br}(D^+ \rightarrow \mu^+ \nu) = (3.74 \pm 0.21 \pm 0.06) \times 10^{-4}$$

$$f_{D^+} = (203.91 \pm 5.72 \pm 1.97) \text{ MeV}$$

$$|V_{cd}| = (0.222 \pm 0.006 \pm 0.005)$$



➤ Experimental value of f_D is with precision of 2.5%. More data is needed.

➤ **In future,**

- The results of pure-leptonic decay for $D^+ \rightarrow \tau^+ \nu_\tau$ and $D^+ \rightarrow e^+ \nu_e$ will be presented with the largest $\psi(3770)$ data in the world.
- The results of pure-leptonic decay for $D_s^+ \rightarrow \mu^+ \nu_\mu$ and $D^+ \rightarrow \tau^+ \nu_\tau$ will be presented with the data taken with BESIII @ 4.01 GeV.

The end!