

Fragmentation Functions at BESIII

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(for the BESIII Collaboration)

The Sixth Workshop on Hadron Physics in China and Opportunities in US

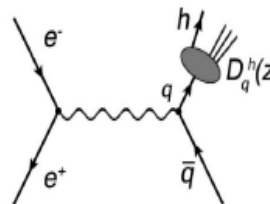
Lanzhou, China 21–24th July 2014

Outline

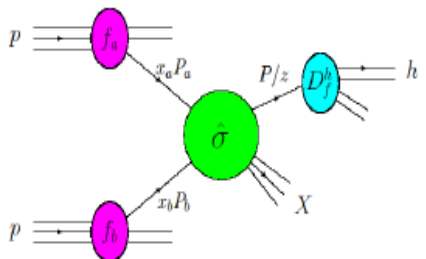
- **Introduction**
 - Fragmentation Function(FF)
 - Motivation
- **BEPCII and BESIII**
- **Physics topics about FF at BESIII:**
 - Inclusive hadron($\pi/\pi^0/K/K_S\dots$) production
 - Double Collins Asymmetries(**DCA**) measurement
- **Summary and Outlook**

Fragmentation Function (FF)

- Fragmentation Functions** (FFs) describe the probability for a parton to fragment into a hadron carrying a certain fraction z of the parton momentum



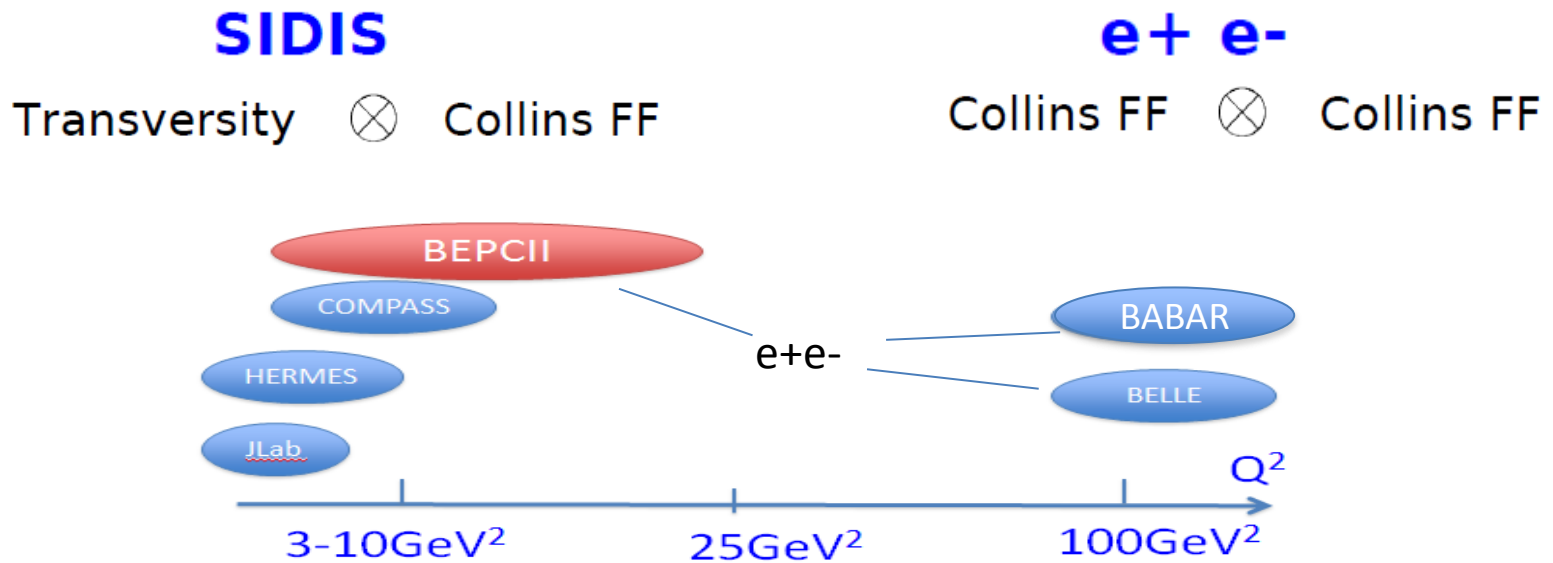
$$\text{LO } \frac{d\sigma}{dz} (e^-e^+ \rightarrow hX) = \sum_q \sigma(e^-e^+ \rightarrow q\bar{q}) [D_q^h(z) + D_{\bar{q}}^h(z)]$$



$$\sigma = \sum_{a,b,c} f_a(x_a, Q^2) \otimes f_b(x_b, Q^2) \otimes \hat{\sigma}(ab \rightarrow cX) \otimes D_c^h(z, Q^2)$$

- FF are nonperturbative in nature, important information in our understanding of hadron production and parton distribution
- Fitting: parametrization & experimental data ($e+e-$, SIDIS, pp)
- Universality:** process independent (SIDIS, pp, ee annihilation)
- Energy evolution:** evolved from a defined energy scale

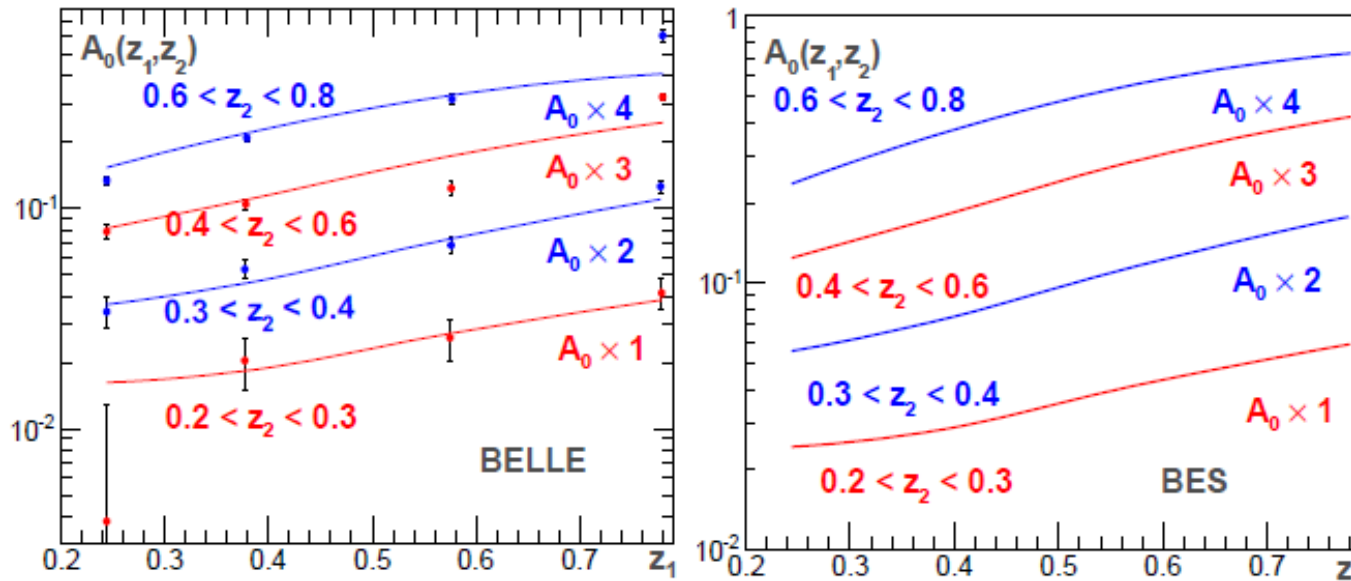
Motivation



- **SIDIS experiments: HERMES, JLab, low Q^2 , to extract PDFs, need FFs from $e+e-$ annihilations.**
- **Existing information of FFs: BABAR, Belle etc., high Q^2 , need energy evolution for SIDIS.**
- **BEPCII: similar energy coverage with SIDIS. Input for extracting the parton distribution **without energy evolution!** Proposed by **PRD 88. 034016 (2013)****
- **Combined efforts to measurement Transversity distribution**

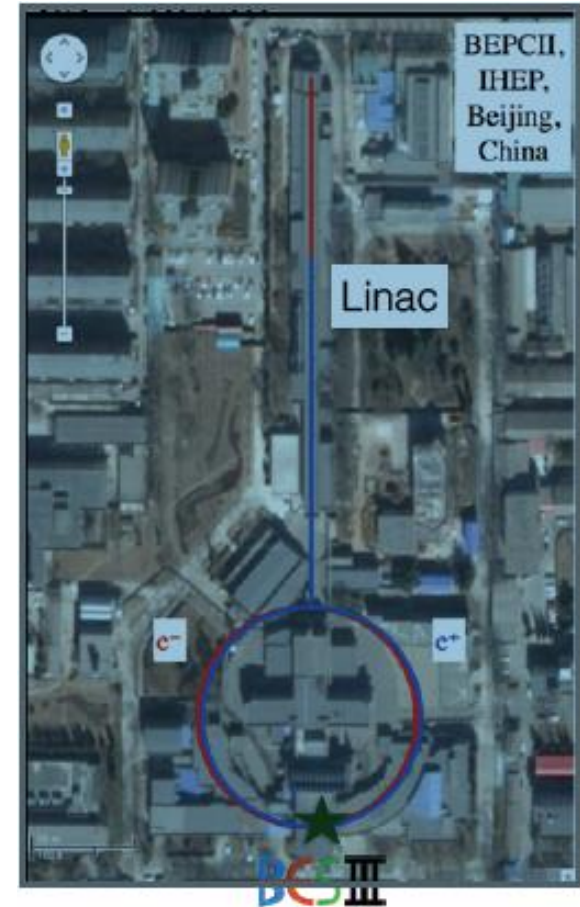
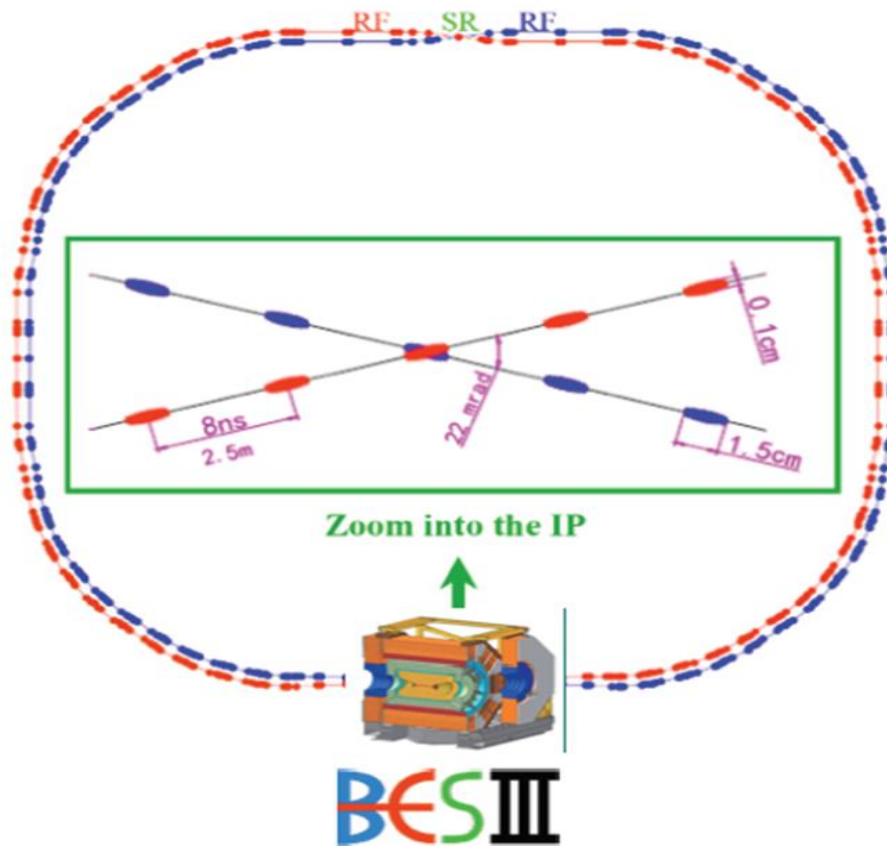
Motivation

PRD 88. 034016 (2013) P. Sun, F. Yuan



- The Collins asymmetries in di-pion azimuthal angular distributions in e^+e^- annihilation processes, $E_{c.m.} = 4.6\text{GeV}$,
- Because of energy evolution effect, it will be larger than that at Belle by a factor 2
- The experimental results from BEPCII will provide an important test.

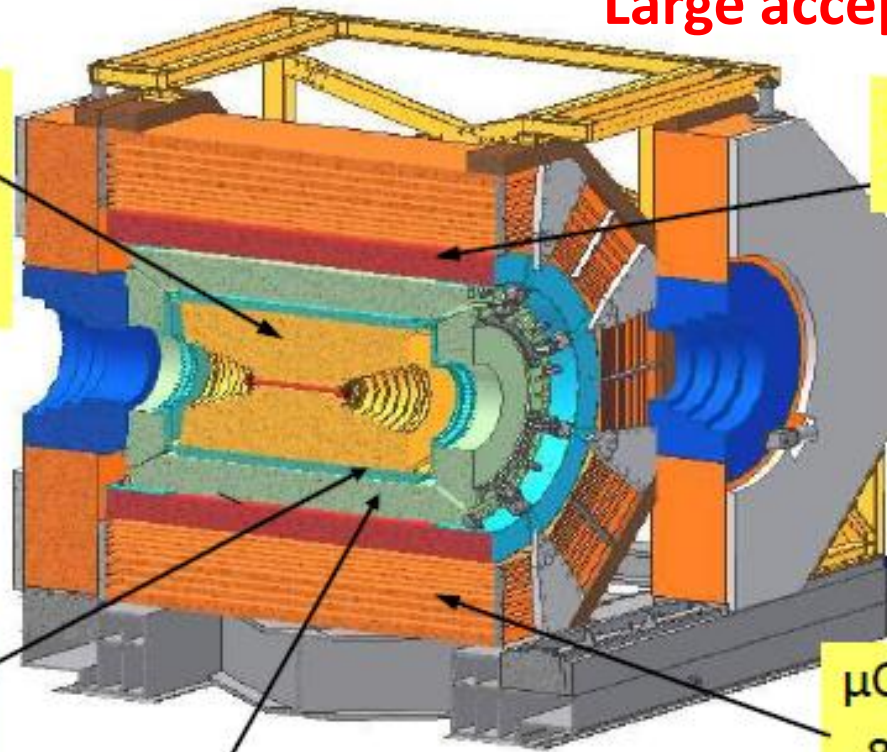
Beijing Electron Positron Collider-II (BEPCII)



- e⁺e⁻ annihilation , **unpolarized** beams, **symmetric** collider,
- Beam energy: 1.0-2.3GeV (**Q: ~2.0-4.6GeV**)
- Achieved luminosity: $0.7 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ @3.770GeV

The BESIII Detector

Large acceptance: $93\% * 4\pi$



Drift Chamber (MDC)
 $\sigma_{P/P} (\%) = 0.5\% (1\text{GeV})$
 $\sigma_{dE/dx} (\%) = 6\%$

- Tracking
- PID

Super-conducting magnet (1.0 tesla)

Time Of Flight (TOF)
 σ_T : 90 ps Barrel
 110 ps endcap

- PID

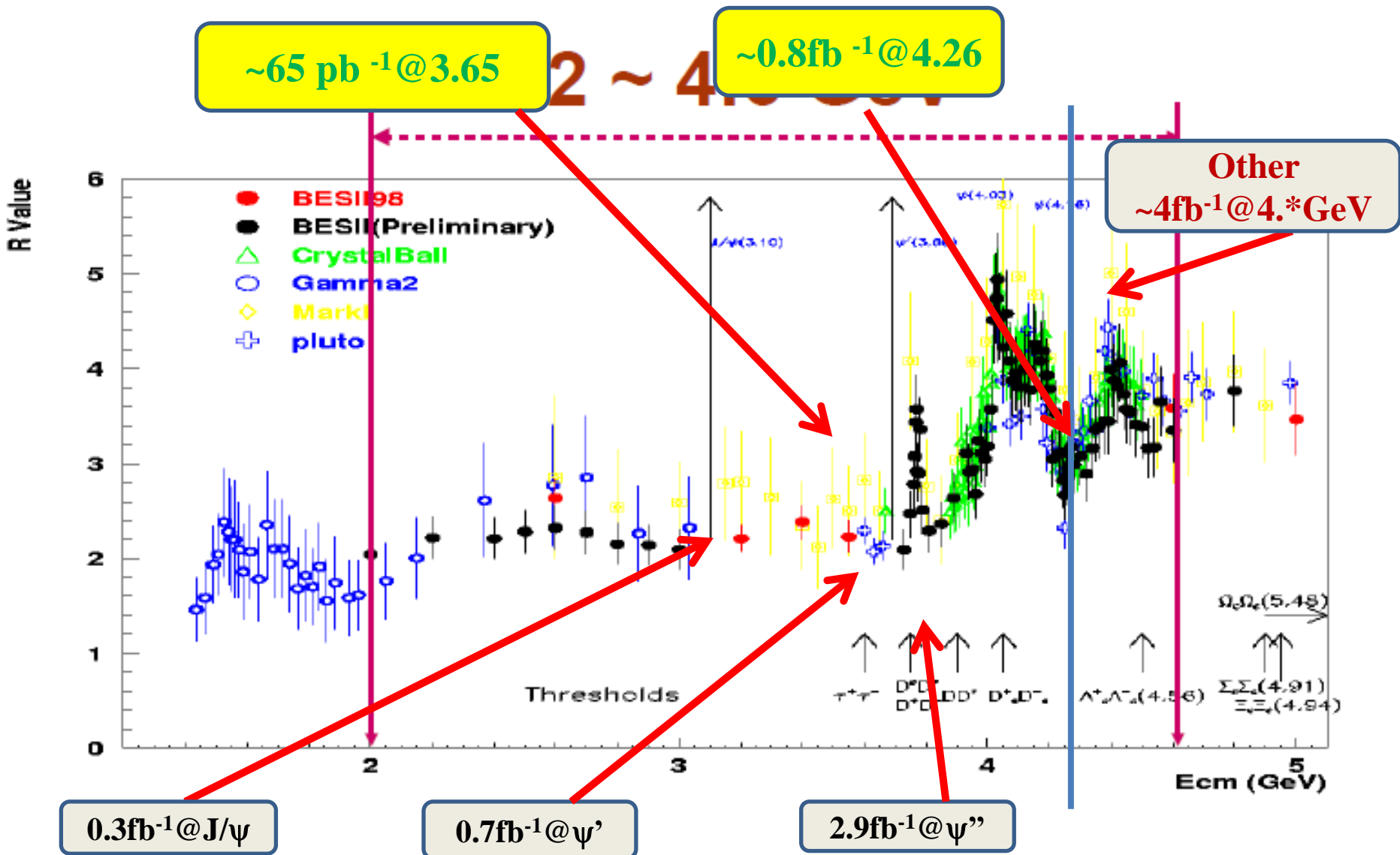
μ Counter
 8- 9 layers RPC
 $\delta R\Phi = 1.4 \text{ cm} \sim 1.7 \text{ cm}$

- muon PID

EMC: $\sigma_{E/\sqrt{E}} (\%) = 2.5\% (1 \text{ GeV})$
 (CsI) $\sigma_{z,\phi} (\text{cm}) = 0.5 - 0.7 \text{ cm}/\sqrt{E}$

- Neutral showers reconstruction

Data Samples We Have



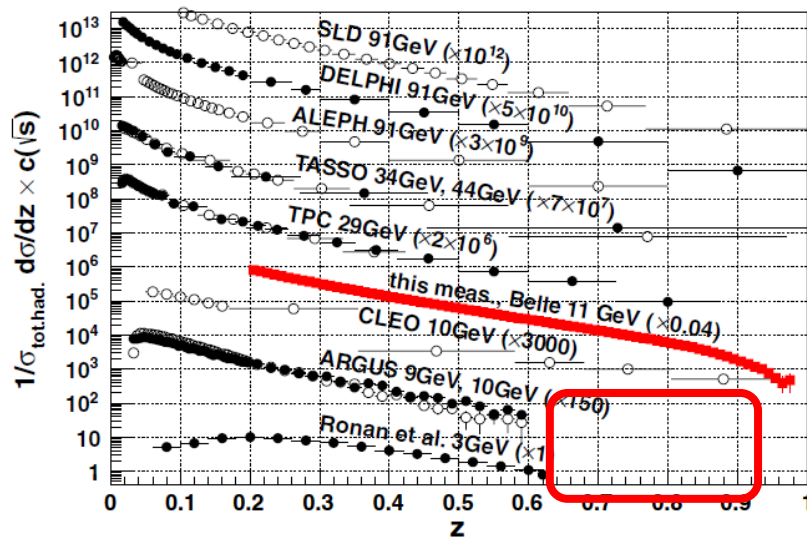
Inclusive Hadron Production

$$e^+e^- \rightarrow \pi/K + X$$

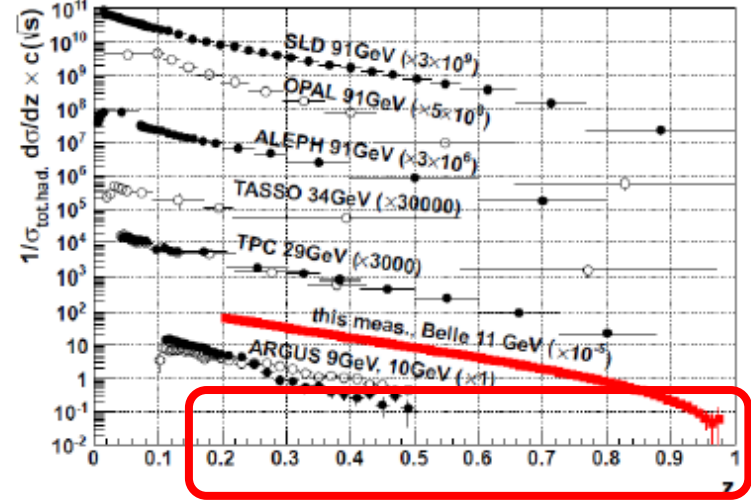
$\pi + X$

$K + X$

World Data (Sel.) for $e^+e^- \rightarrow \pi^+X$ Production



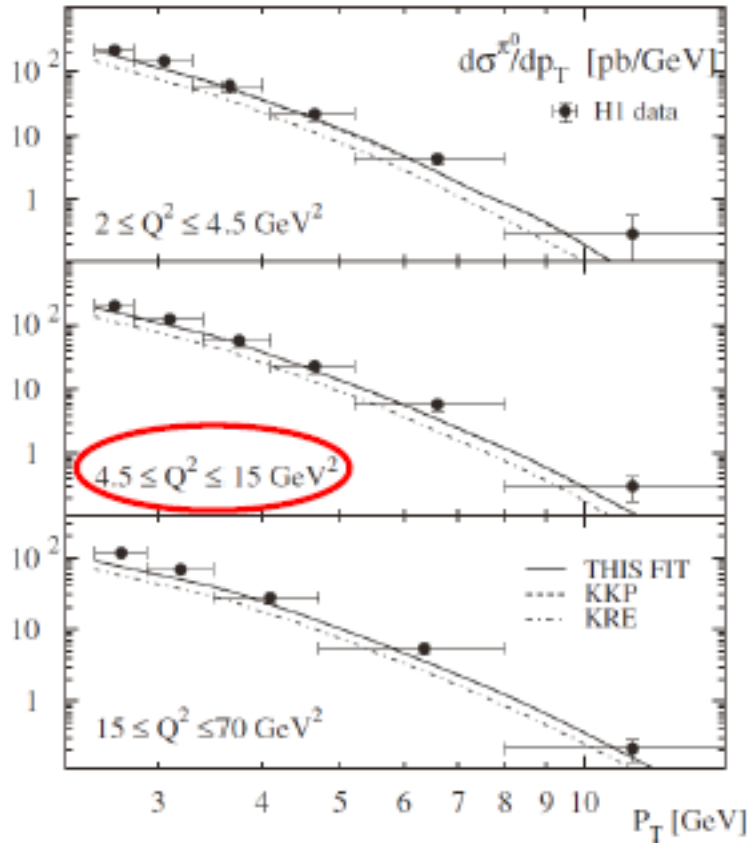
World Data (Sel.) for $e^+e^- \rightarrow K^+X$ Production



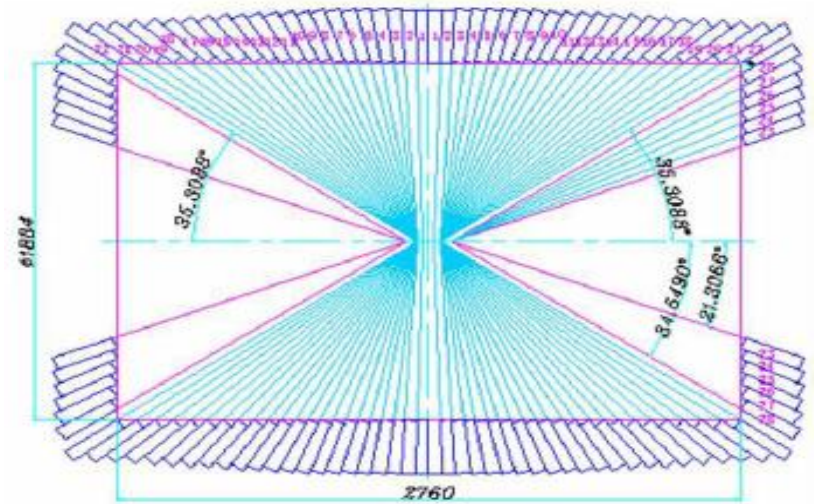
PRL 111 062002 (2013)

- Lack of low energy scale, high z $z=2E_{\text{hadron}}/\sqrt{s}$:
 - BESIII can contribute
- PID problem at high z
 - High error rate of PID for the charged tracks with high momentum.

$$e^+e^- \rightarrow \pi^0 + X$$



PRD 75 114010 (2007)

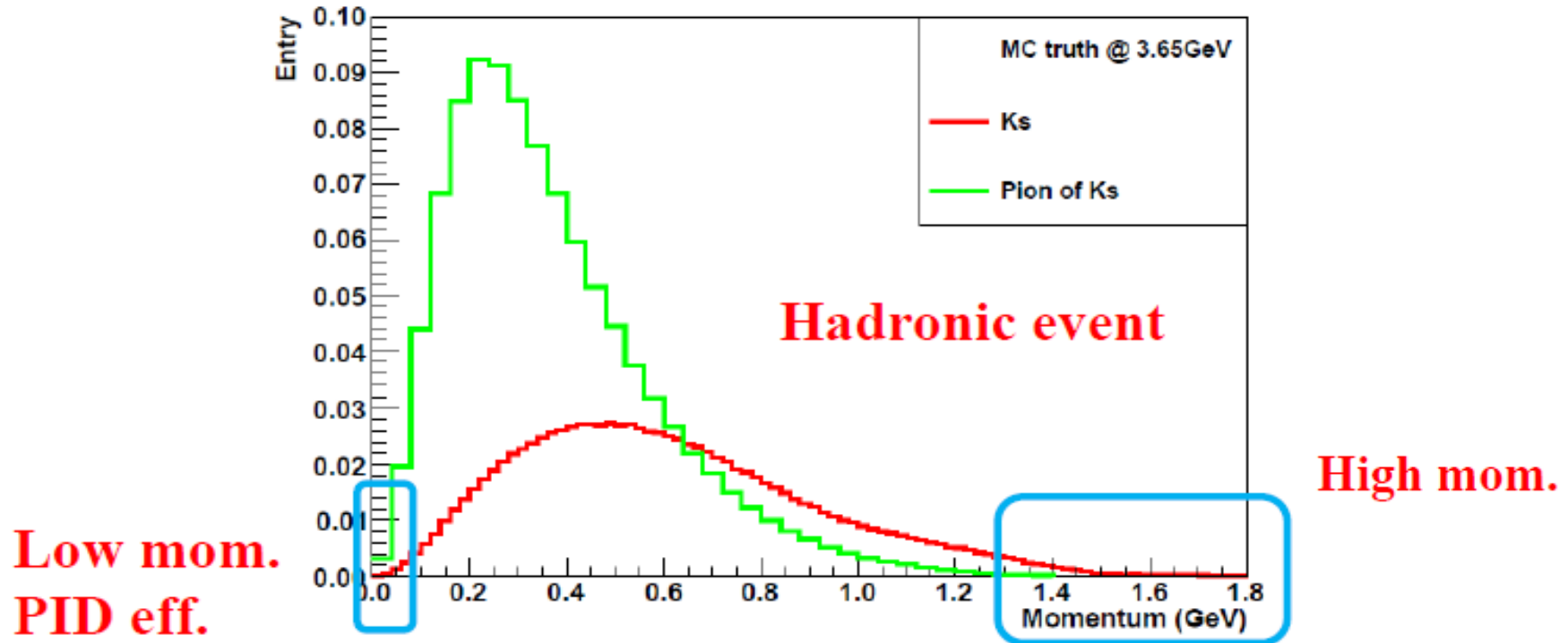


Resolution	Energy	Position
Barrel	2.5%@1GeV	6mm@1GeV
Endcap	5.0%@1GeV	9mm@1GeV

- $\pi^0 \rightarrow 2\gamma$ with EMC
- $e^+e^- \rightarrow \pi^0 + X$ @BESIII

- PID is not needed (crucial issue for charged π/K , especially at high z)
- At BESIII, good performance of EMC on measuring neutral showers

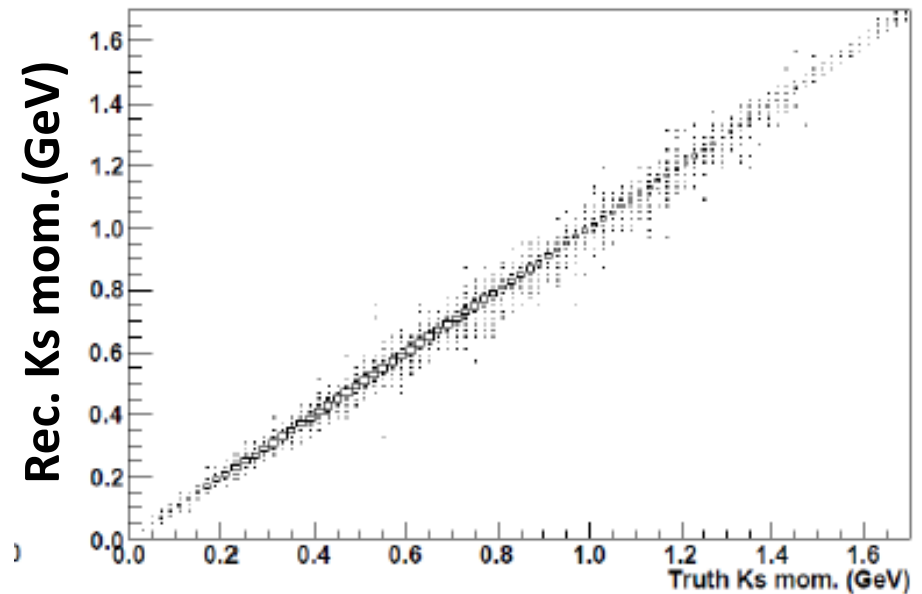
$$e^+e^- \rightarrow K_s + X \rightarrow \pi^+\pi^- + X \quad (\text{in progress})$$



- $K_s + X$: clean process, low backgrounds level
- Second vertex to suppress backgrounds

$$e^+e^- \rightarrow K_s + X \rightarrow \pi^+\pi^- + X \quad (\text{in progress})$$

	Ks candidate no. @[0.47-0.53]
$(\gamma)e^+e^-$	1667/0.56%
$(\gamma)\mu^+\mu^-$	110/0.037%
$(\gamma)\gamma\gamma$	140/0.047%
$(\gamma)\tau^+\tau^-$	4156/1.40%
e^+e^-+X	248/0.084%
Non-phys.	2453/0.83%



Truth Ks mom.(GeV)

- Binning to get the cross section depending on the momentum of Ks
- The resolution of Ks momentum is good enough
- Preliminary data results are not shown
- Data set @3.65GeV

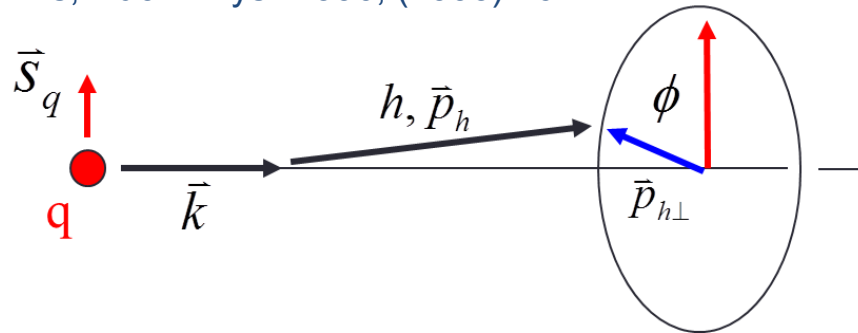
Probe Collins Effect

(in progress)

- We only focus on the di-pion currently.

Collins Fragmentation Function

J. Collins, Nucl. Phys. B396, (1993) 161



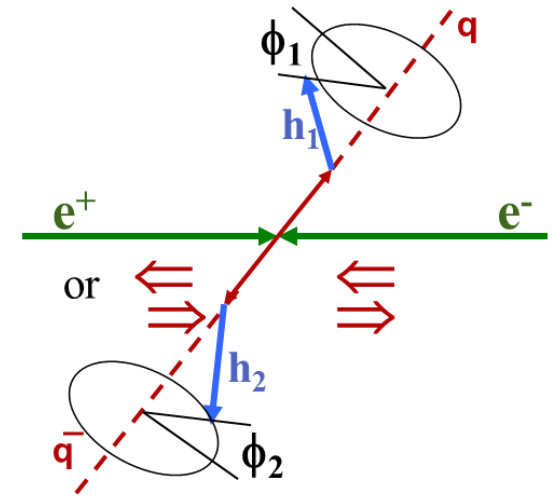
- It describes the relation between the transverse spin of the fragmenting quark and the azimuthal distribution of the final state hadrons around the quark momentum

$$D_{hq^{\uparrow}}(z, P_{h\perp}) = D_1^q(z, P_{h\perp}^2) + H_1^{\perp q}(z, P_{h\perp}^2) \frac{(\hat{\mathbf{k}} \times \mathbf{P}_{h\perp}) \cdot \mathbf{S}_q}{zM_h},$$

- H : Collins Fragmentation Function
- z : fractional energy of hadron $z = 2E_h/\sqrt{s}$,
- $\mathbf{P}_{h\perp}$: transverse momentum of the hadron

Probe Collins Effect in e^+e^- Annihilation

- In e^+e^- annihilation, γ^* (spin-1) \rightarrow spin-1/2 q and \bar{q}
 - In a given event, the spin directions are unknown, but they must be parallel
 - Exploit this correlation by using hadrons in opposite jets



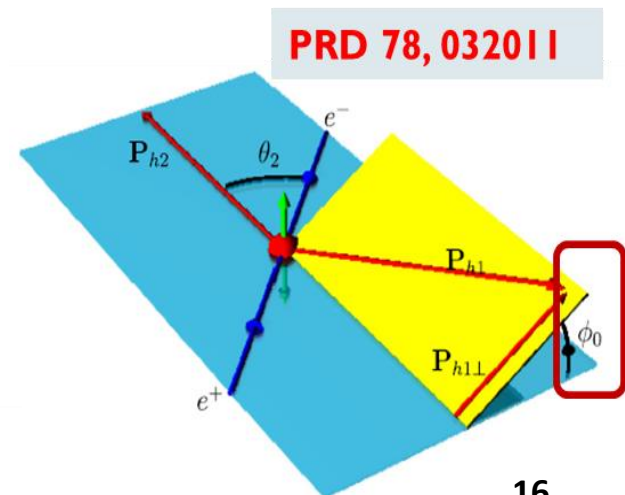
- The correlation of quark and anti-quark Collins functions give a product of $\cos(2\phi_0)$ modulation

$$e^+e^- \rightarrow q\bar{q} \rightarrow h_1 h_2 X \quad (q=u, d, s) \implies$$

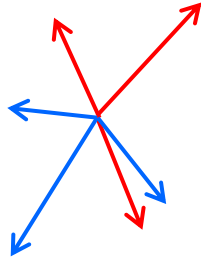
$$\sigma \propto \cos(2\phi_0) H_1^\perp(z_1) \otimes H_1^\perp(z_2),$$

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d^2\mathbf{q}_T} = \frac{3\alpha^2}{Q^2} z_1^2 z_2^2 \left\{ A(y) \mathcal{F}[D_1 \bar{D}_2] + B(y) \right.$$

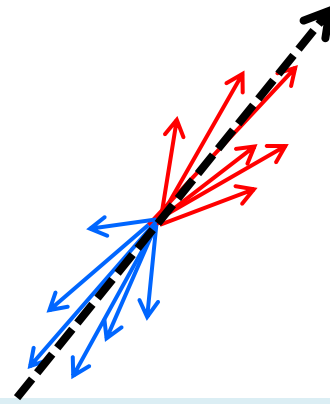
$$\left. \times \cos(2\phi_0) \mathcal{F} \left[(2\hat{\mathbf{h}} \cdot \mathbf{k}_T \hat{\mathbf{h}} \cdot \mathbf{p}_T - \mathbf{k}_T \cdot \mathbf{p}_T) \frac{H_1^\perp \bar{H}_2^\perp}{M_1 M_2} \right] \right\},$$



Event Shape



BEPCII energy



High energy scale

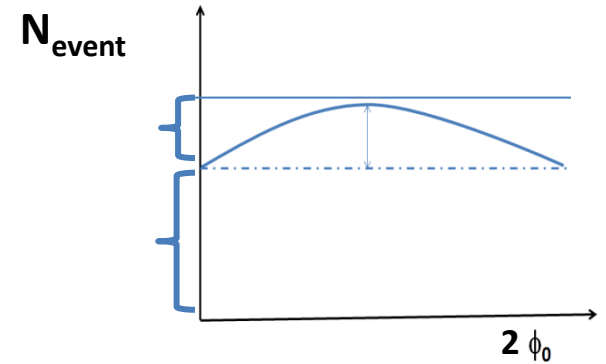
$$T \equiv \frac{\sum_h |P_h^{\text{CMS}} \cdot \hat{n}|}{\sum_h |P_h^{\text{CMS}}|},$$

- ✓ At Belle/BABAR, with two-jets events
 - ✓ High Thrust value is useful to suppress backgrounds.
 - ✓ Thrust axis is used to separate the hadrons from opposite jets (h_1 and h_2)
- ✓ At BESIII, different situation
 - Low energy, low multiplicity, $q \bar{q}$ event shape is not jetty!
 - **Mis-combination problem:** $h_1 h'_1$ or $h_2 h'_2$ combination from same quark which are not of interest. **Dilute the measured asymmetries.**
 - Require large **Open Angle(OA)** of π -pair to suppress mis-combination;
Choosing the leading hadrons
 - Mis.com. could be suppressed, but still be a problem

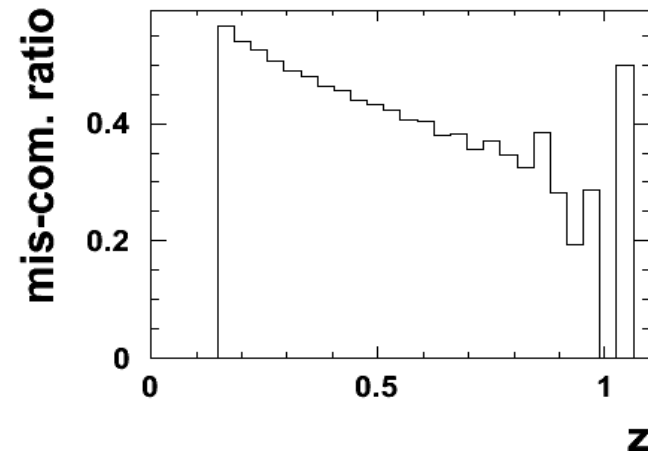
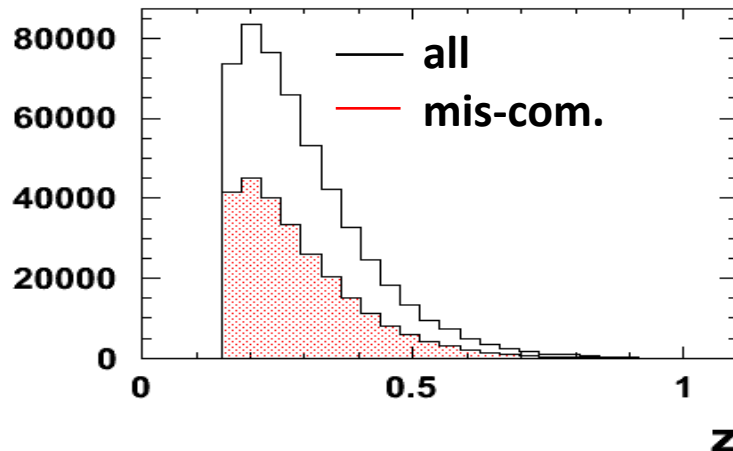
Estimation of Mis-combination Rate

- ▶ The rate of the mis-combination ($R_{mis.}$) need to be known

$$A_{ture} = (1 + R_{mis.})A_{mea.}$$

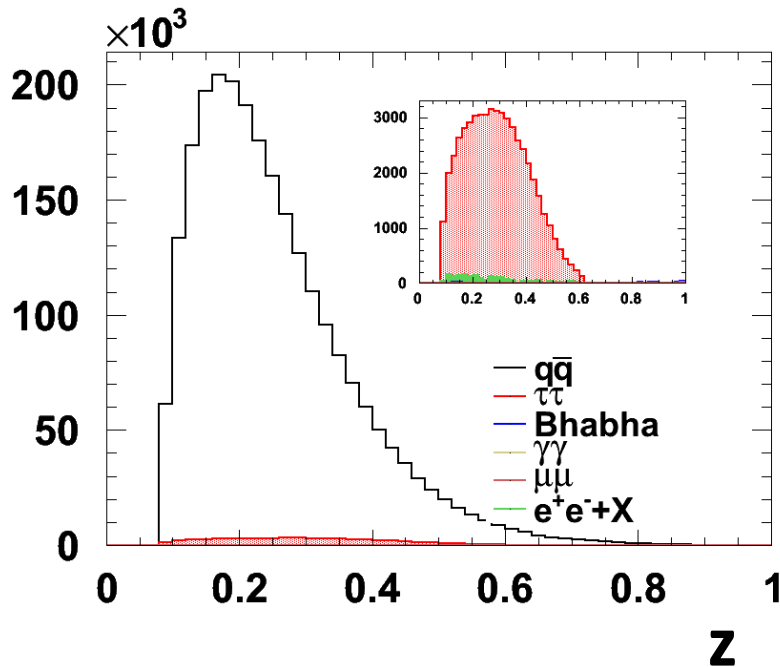


- This estimation **relies on MC**
 - We trace the final hadrons back to the initial parton in Pythia to find π -pair that come from the same quark .
 - Need more check and will be used to correct asymmetries measured in data

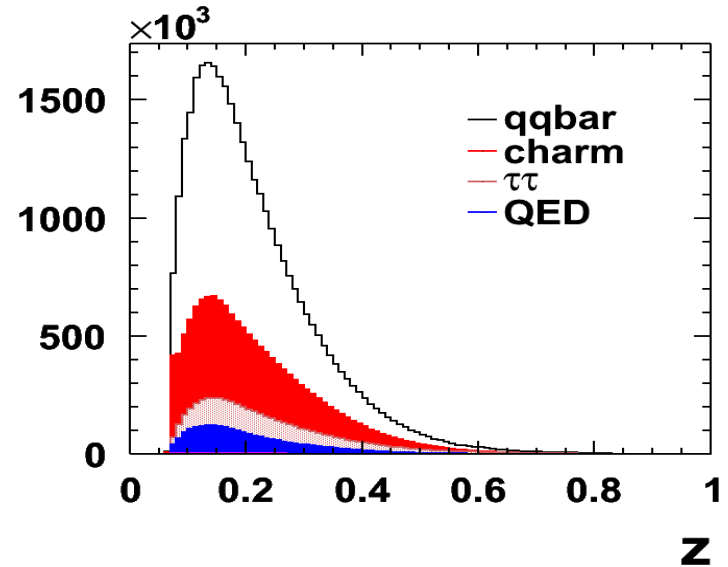


Backgrounds

@3.65GeV



@4.26GeV



✓ Need to check asymmetries contributed by background.

$$A_{\alpha}^{\text{meas}} = \left(1 - \sum_i F_i\right) \cdot A_{\alpha} + \sum_i F_i \cdot A_{\alpha}^i$$

Fraction of background

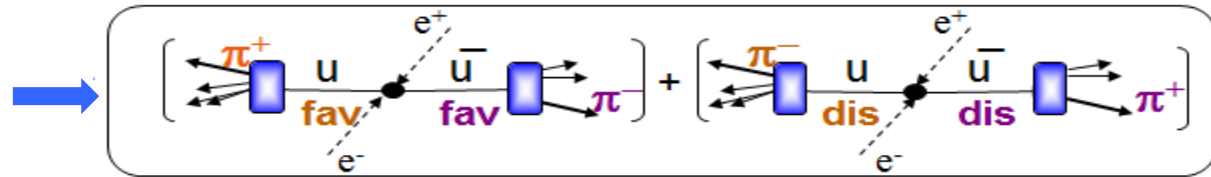
The true asymmetries

Asymmetries from background

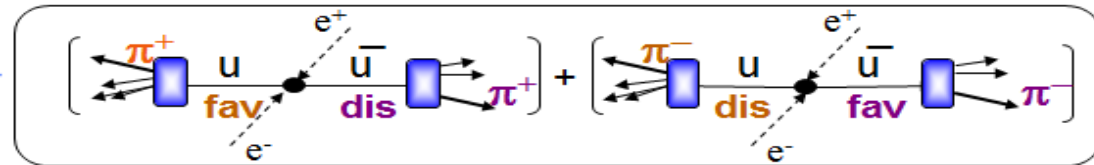
Double Ratio

- **Favored** fragmentation process describes the fragmentation of a quark of flavor q into a hadron with a valence quark of the same flavor: i.e.: $u \rightarrow \pi^+$, $d \rightarrow \pi^-$
- **Disfavored** for $d \rightarrow \pi^+$, $u \rightarrow \pi^-$

Unlike-sign pion pair = **U**:
 $\pi^{\mp}\pi^{\pm}$: (**fav** x **fav**) + (**dis** x **dis**)



Like-sign pion pair = **L**:
 $\pi^{\pm}\pi^{\pm}$: (**fav** x **dis**) + (**dis** x **fav**)



– Normalized Ratio **R**

$$R_0(2\phi_0) = \frac{N(2\phi_0)}{\langle N_0 \rangle}$$

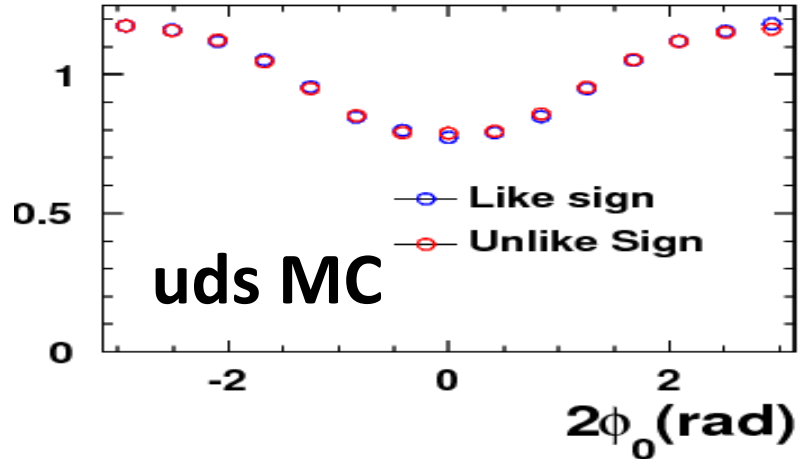
– Double Ratio (**DR**) (R^U/R^L) to cancel **detector effects** and **QCD radiative effects** which are charged independent



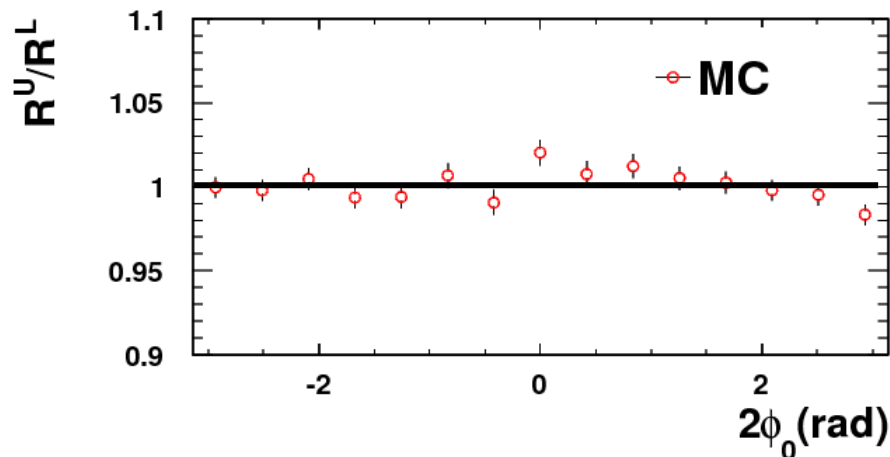
$$R_0^U / R_0^L = 1 + \boxed{\cos(2\phi_0)} \frac{\sin^2\theta}{1 + \cos^2\theta} \times \left\{ \frac{f(H_1^{\perp, \text{fav}} \bar{H}_1^{\perp, \text{fav}} + H_1^{\perp, \text{dis}} \bar{H}_1^{\perp, \text{dis}})}{(D_1^{\text{fav}} \bar{D}_1^{\text{fav}} + D_1^{\text{dis}} \bar{D}_1^{\text{dis}})} - \frac{f(H_1^{\perp, \text{fav}} \bar{H}_1^{\perp, \text{dis}})}{(D_1^{\text{fav}} \bar{D}_1^{\text{dis}})} \right\}$$

$2\phi_0$ Distributions (MC)

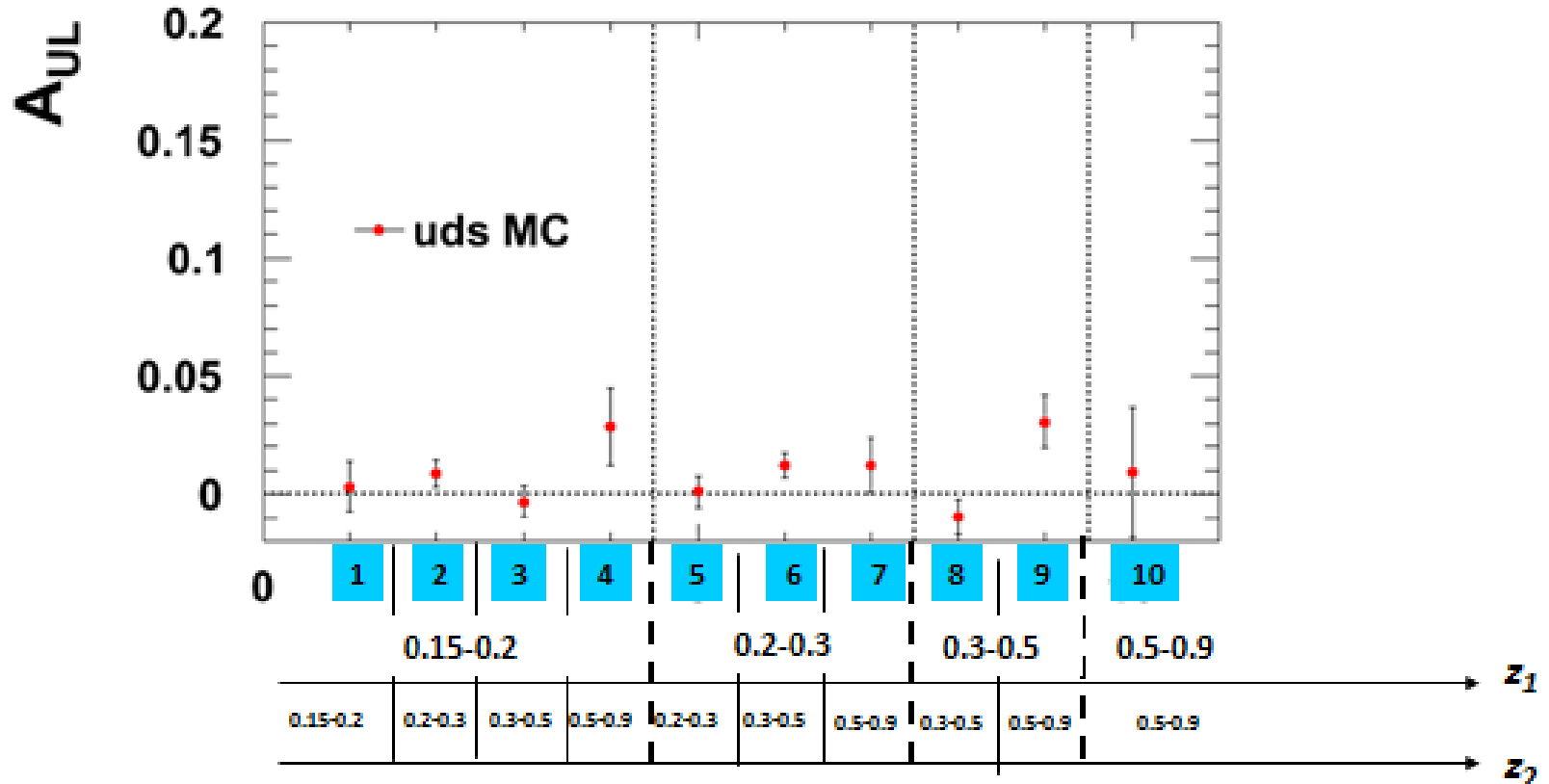
- Normalized Raw distribution:



- Double Ratio:



MC Validation



- **Statistic uncertainties only. Consistent with zero as expected.**
- **In the last z bin, assume 15% asy. ,sensitivity > 3 sigma**

Summary and Outlook

- **BESIII data can provide:**
 - Data at low energy scale
 - Test energy evolution effect of FF
 - Combined effort to measurement Transversity distribution
- **What we are working on:**
 - $K_s + X$ cross section
 - Double Collins asymmetries in inclusive charged π production
- **Outlook**
 - Spin 2014 Conference
 - $\sim 0.36\text{fb}^{-1}$ off-resonance data, 2015/2016

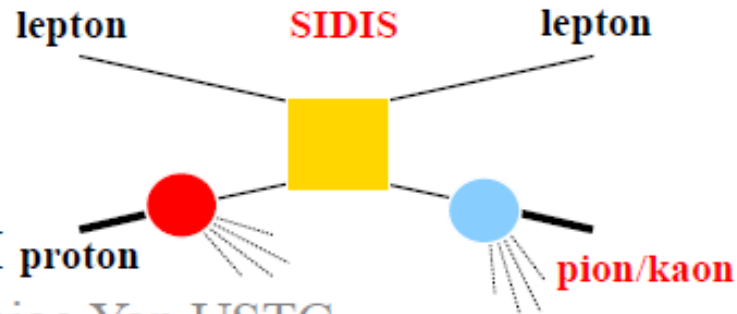
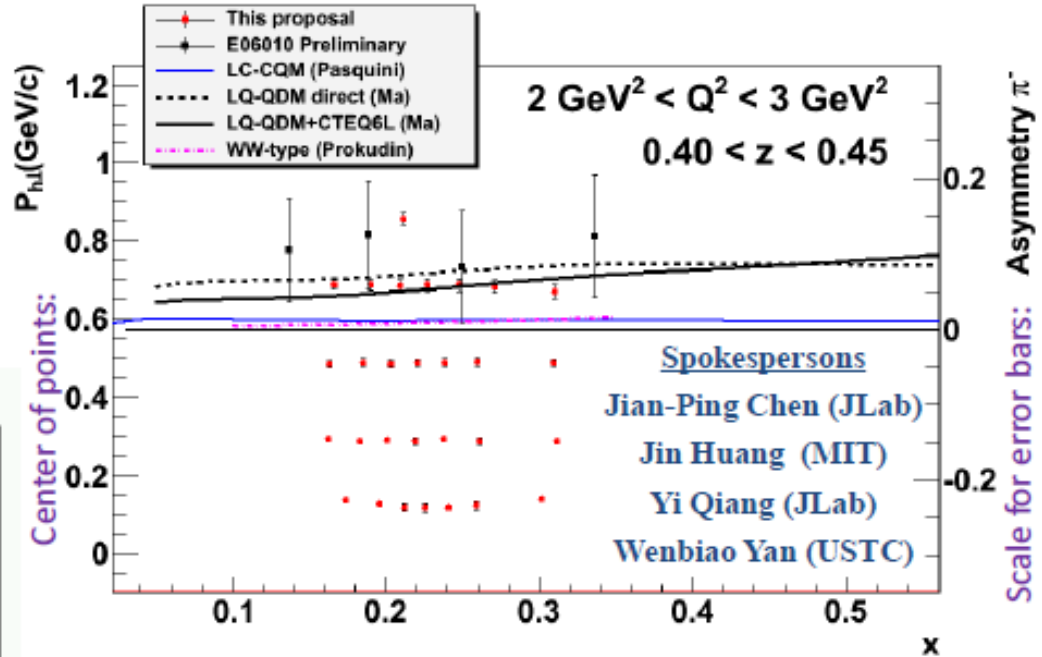
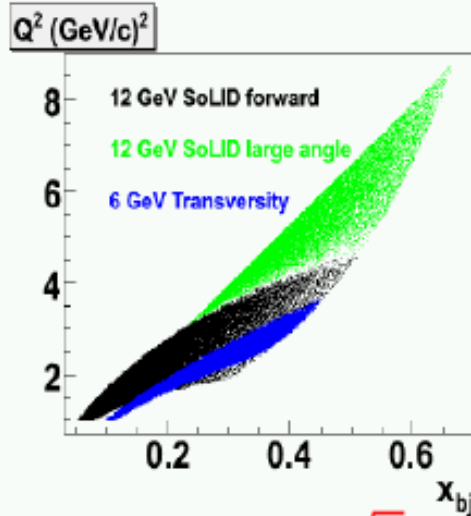
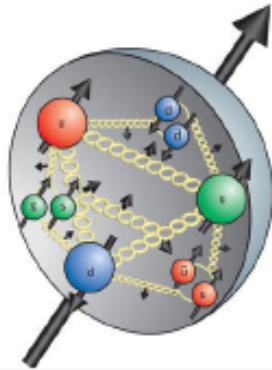
THANKS!

BACKUP

TMD-PFFs

$D_1(z) = \left[\bullet \rightarrow \bigcirc \right]$	$D_1(z, \mathbf{k}_T^2) = \left[\bullet \rightarrow \bigcirc \right]$ $D_{1T}^{\perp}(z, \mathbf{k}_T^2) = \left[\bullet \rightarrow \bigcirc \right]$
$G_1(z) = \left[\bullet \rightarrow \bigcirc \right] - \left[\bullet \leftarrow \bigcirc \right]$	$G_{1L}(z, \mathbf{k}_T^2) = \left[\bullet \rightarrow \bigcirc \right] - \left[\bullet \leftarrow \bigcirc \right]$ $G_{1T}(z, \mathbf{k}_T^2) = \left[\bullet \rightarrow \bigcirc \right] - \left[\bullet \rightarrow \bigcirc \right]$
$H_1(z) = \left[\uparrow \bullet \rightarrow \bigcirc \right] - \left[\downarrow \bullet \rightarrow \bigcirc \right]$	$H_{1T}(z, \mathbf{k}_T^2) = \left[\uparrow \bullet \rightarrow \bigcirc \right] - \left[\downarrow \bullet \rightarrow \bigcirc \right]$ $H_{1L}^{\perp}(z, \mathbf{k}_T^2) = \left[\uparrow \bullet \rightarrow \bigcirc \right] - \left[\downarrow \bullet \rightarrow \bigcirc \right]$ $H_{1T}^{\perp}(z, \mathbf{k}_T^2) = \left[\uparrow \bullet \rightarrow \bigcirc \right] - \left[\downarrow \bullet \rightarrow \bigcirc \right]$ $H_{1\perp}^{\perp}(z, \mathbf{k}_T^2) = \left[\uparrow \bullet \rightarrow \bigcirc \right] - \left[\downarrow \bullet \rightarrow \bigcirc \right]$

Spin structure of nucleon



Born level $Q \sim \sqrt{s}$ @ BESIII

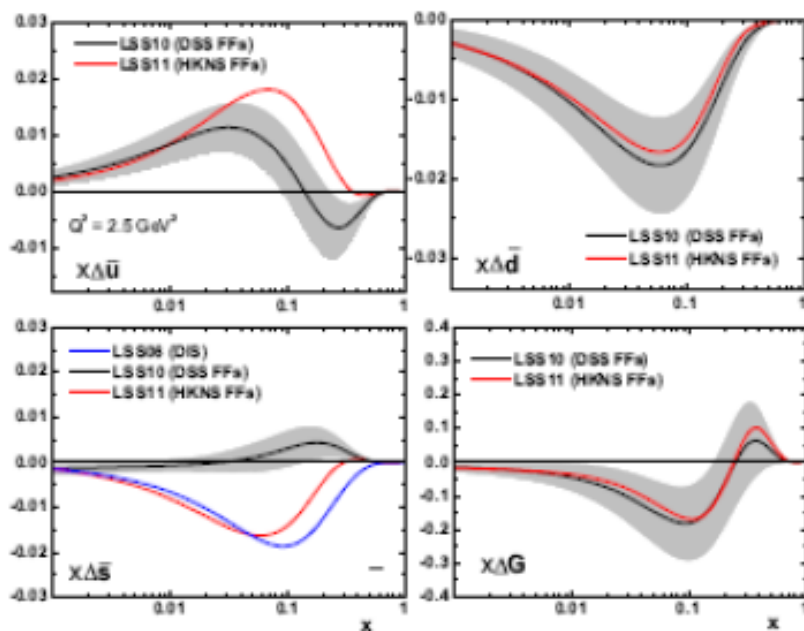
2014/6/6

Wenbiao Yan USTC

5

Strange quark polarization puzzle

- sum of polarization strange parton PDFs: $\Delta s(x) + \Delta \bar{s}(x)$
 - polarized inclusive DIS: **negative** for all values of x
 - Semi-inclusive DIS: **positive** for most of measured x
- PRD 84 014002 (2011) : **HKNS FF, negative for SIDIS**



PRD 84 014002 (2011)

- Inclusive DIS: $e+N \rightarrow e'+X$
 - parton density function PDF
- Semi-inclusive DIS: $e+N \rightarrow e'+h+X$
 - PDF and FF

Inclusive kaon production

Motivation

SIDIS

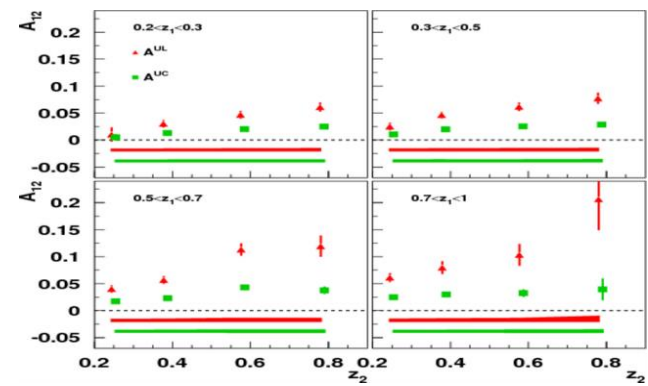
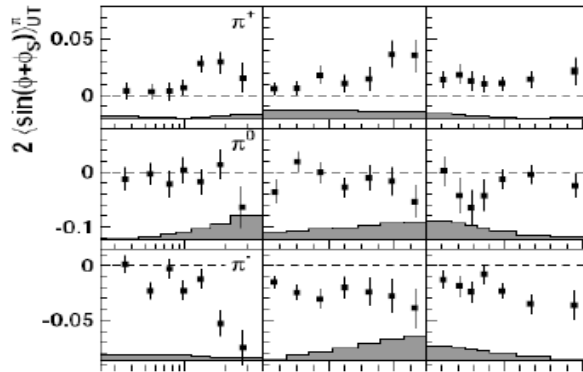
e^+e^-

Transversity \otimes Collins FF

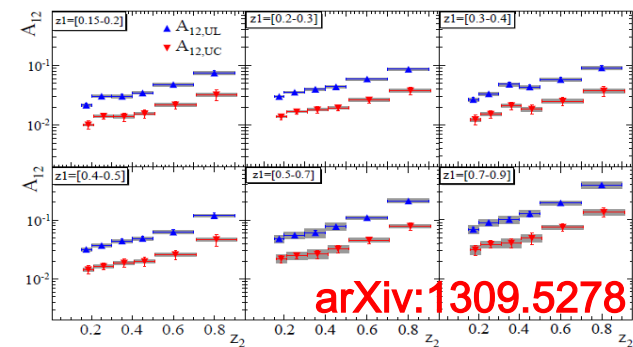
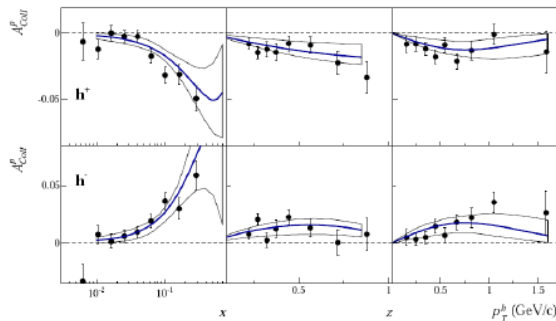
Collins FF \otimes Collins FF

PRL 94: 012002, PLB693,11-16

PRL96: 232002, PRD 78:032011



COMPASS, PLB 2012



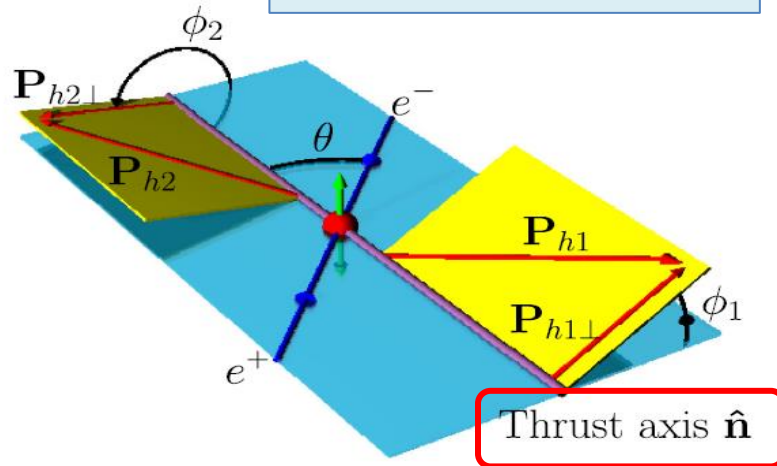
BABAR

arXiv:1309.5278

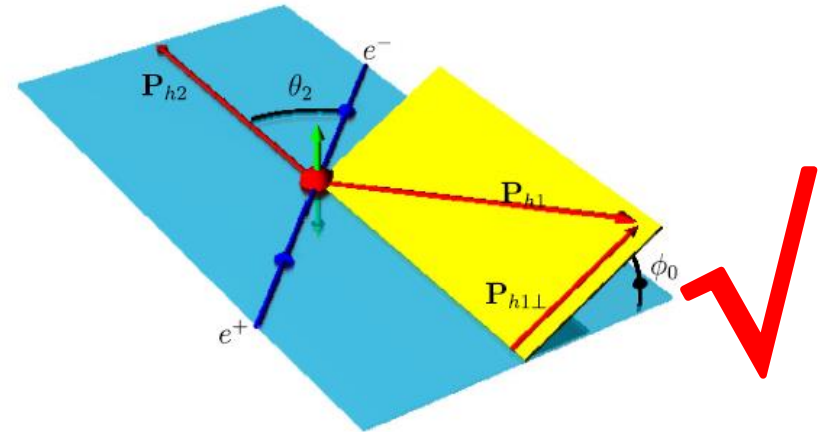
- FF from e^+e^- as input for extracting the parton distribution

Double Collins Asymmetries(DCA)

The Thrust frame



The second hadron frame



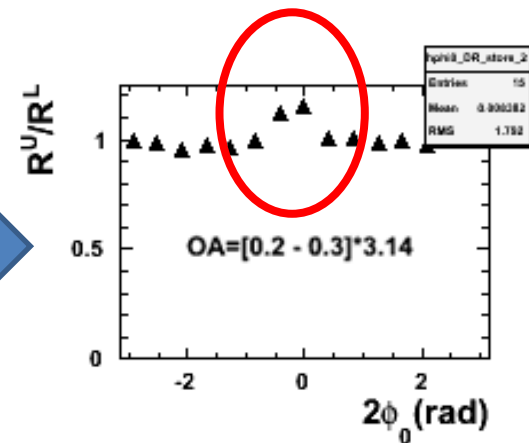
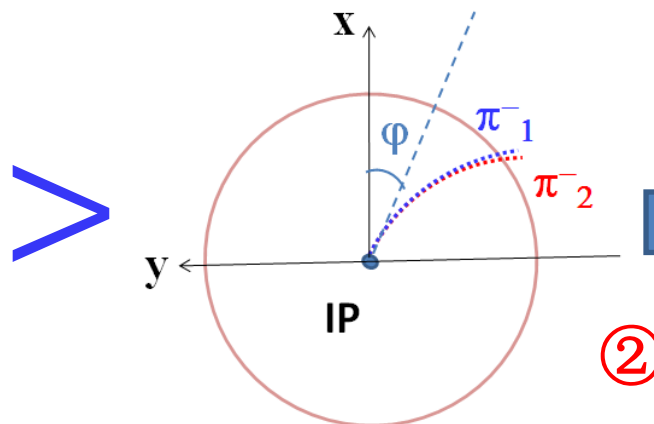
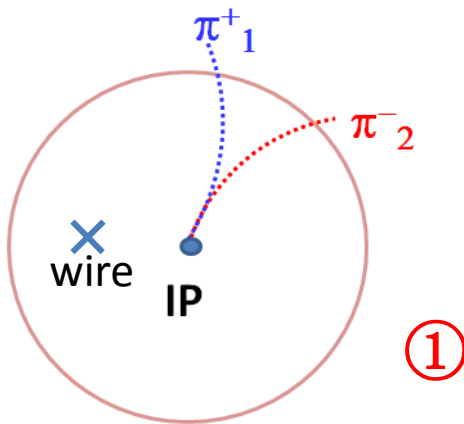
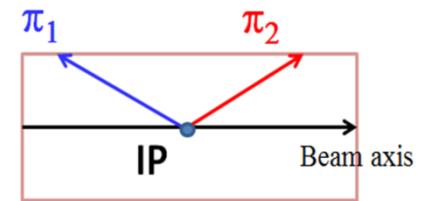
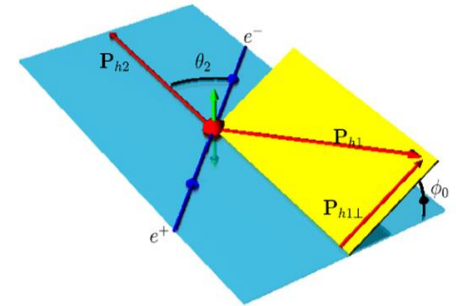
$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d\phi_1 d\phi_2} = \sum_{q,\bar{q}} \frac{3\alpha^2}{Q^2} \frac{e_q^2}{4} z_1^2 z_2^2 \{ (1 + \cos^2\theta) D_1^{q,[0]}(z_1) \bar{D}_1^{q,[0]}(z_2) + \sin^2\theta \cos(\phi_1 + \phi_2) H_1^{\perp,[1],q}(z_1) \bar{H}_1^{\perp,[1],q}(z_2) \},$$

$$\frac{d\sigma(e^+e^- \rightarrow h_1 h_2 X)}{d\Omega dz_1 dz_2 d^2\mathbf{q}_T} = \frac{3\alpha^2}{Q^2} z_1^2 z_2^2 \left\{ A(y) \mathcal{F}[D_1 \bar{D}_2] + B(y) \times \cos(2\phi_0) \mathcal{F} \left[(2\hat{\mathbf{h}} \cdot \mathbf{k}_T \hat{\mathbf{h}} \cdot \mathbf{p}_T - \mathbf{k}_T \cdot \mathbf{p}_T) \frac{H_1^\perp \bar{H}_2^\perp}{M_1 M_2} \right] \right\},$$

- The correlation of quark and anti-quark Collins Functions
- By looking the two hadrons in opposite jets
- Only the second method could be performed at BESIII

Detector Effects(1)

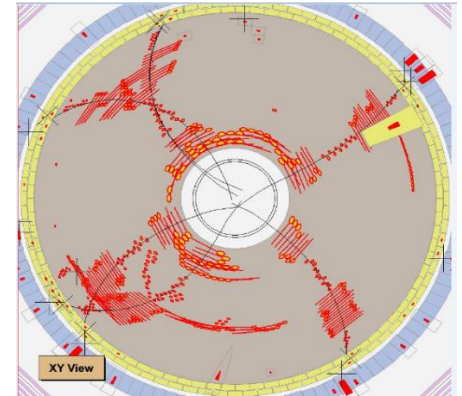
- From MC, we confirmed two kinds of detector effects which can not be cancelled out in Double Ratio:
 - Case 1.** when the azimuthal angle in the detector (φ) of two π are very close, opposite-charged $\pi^+ \pi^-$ have higher efficiencies than same-charged $\pi^- \pi^-$ (or $\pi^+ \pi^+$)



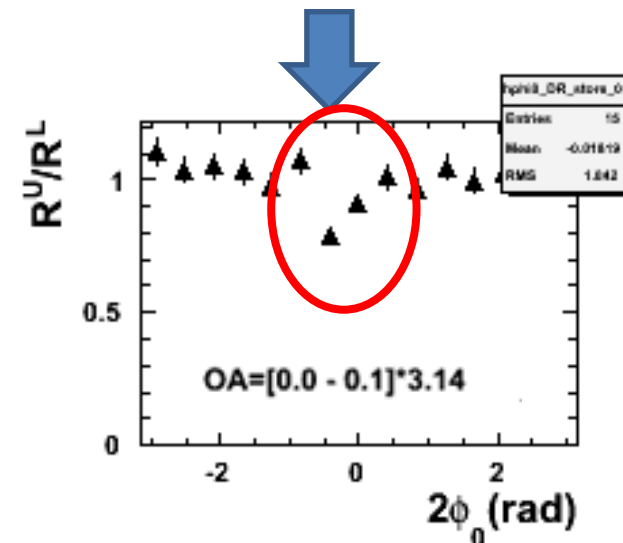
Note that , ϕ_0 is calculated in C.M.S frame. φ is defined in lab. frame.

Detector Effects(2)

- **Case 2.** Ghost tracks produce extra same-charged π pairs ($\pi^- \pi^-$ or $\pi^+ \pi^+$)
- These two detectors effects:
 - contaminate the $2\phi_0$ distribution, especially in **small open angle**
 - require **large open angle** of the two π
 - these effects can be suppressed, **but still there**, assumed as systematic errors



Ghost tracks



Event Selection

- ◆ Charged tracks :

- $|V_r| < 1.0\text{cm}$, $|V_z| < 10.0\text{cm}$
- $|\cos\theta| < 0.93$
- $n_{\text{Good}} \geq 3$

- ◆ Further requirements:

- $N_{\text{electron}} == 0$ to suppress Bhabha
- The total visible energy $E_{\text{vis}} > 1.5\text{GeV}$ to suppress $\tau\tau$

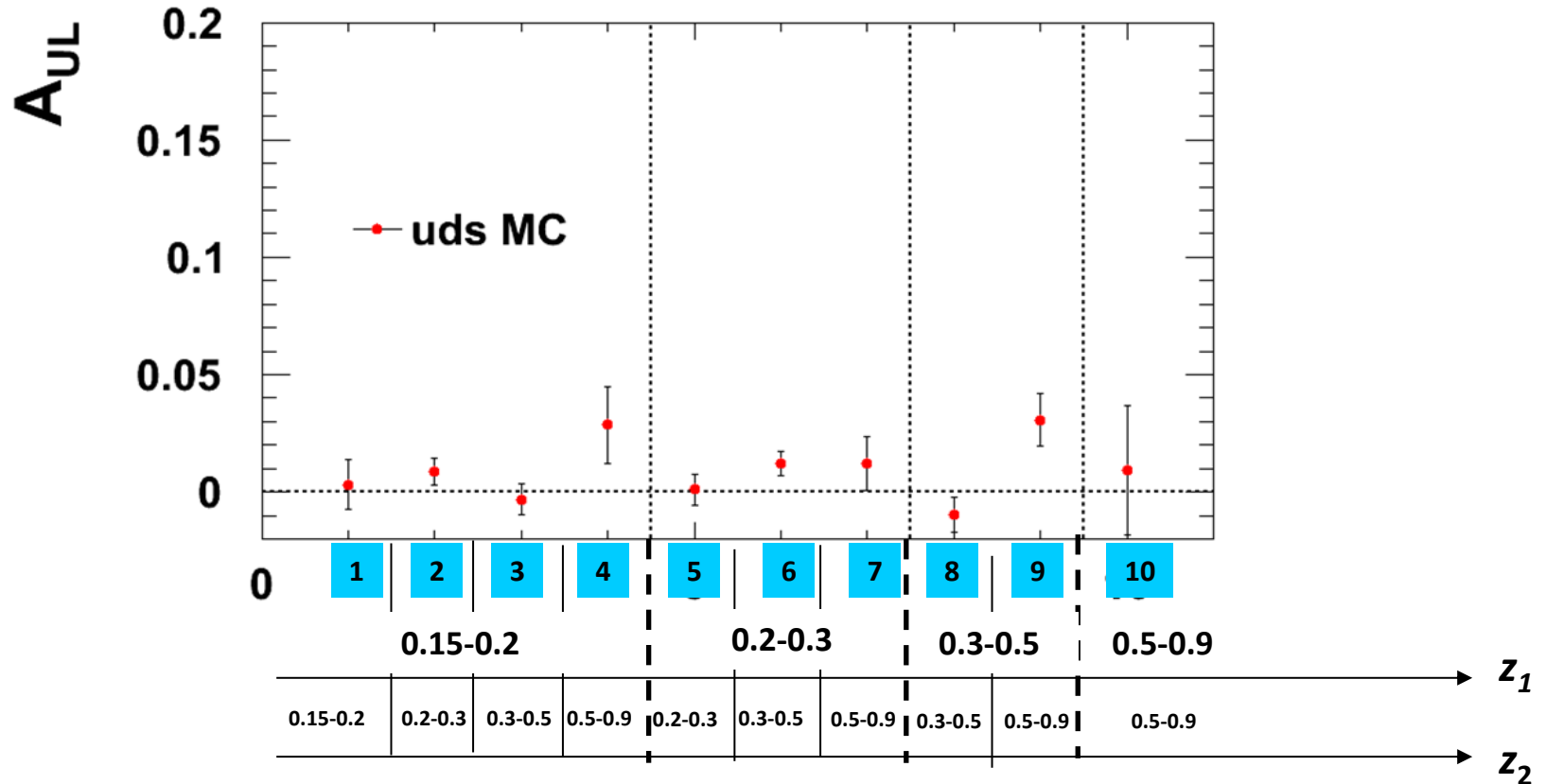
- ◆ PID of π

- dE/dx , TOF1, TOF2
- $\text{Prob}(\pi) > 0 \&\& \text{Prob}(\pi) > \text{Prob}(K)$

- ◆ $N_{\pi} \geq 2$

- ◆ open angle of the π -pair: $OA > 120^\circ$

MC Validation



- **Statistic uncertainties only. Consistent with zero as expected.**
- **Assume 15% asy. in the last z bin, sensitivity > 3 sigma.**